

## Homework #3 Due October 3, 2007

5.1 Determine the decimal values of the following unsigned numbers:

- (a)  $(0111011110)_2$
- (b)  $(1011100111)_2$
- (c)  $(3751)_8$
- (d)  $(A25F)_{16}$
- (e)  $(F0F0)_{16}$

5.3 Determine the decimal values of the following 2's complement numbers:

- (a) 0111011110
- (b) 1011100111
- (c) 1111111110

5.5 Perform the following operations involving eight-bit 2's complement numbers and indicate whether arithmetic overflow occurs. Check your answers by converting to decimal sign-and-magnitude representation.

$$\begin{array}{r} 00110110 \\ +01000101 \\ \hline \end{array} \qquad \begin{array}{r} 01110101 \\ +11011110 \\ \hline \end{array} \qquad \begin{array}{r} 11011111 \\ +10111000 \\ \hline \end{array}$$

$$\begin{array}{r} 00110110 \\ -00101011 \\ \hline \end{array} \qquad \begin{array}{r} 01110101 \\ -11010110 \\ \hline \end{array} \qquad \begin{array}{r} 11011111 \\ -11101100 \\ \hline \end{array}$$

5.7 Show that the circuit in Fig. 5.5 implements the full-adder specified in Fig. 5.4a.

5.10 In section 5.5.4 we stated that a carry-out signal,  $c_k$ , from bit position  $k-1$  of an adder circuit can be generated as  $c_k = x_k \oplus y_k \oplus s_k$ , where  $x_k$  and  $y_k$  are inputs and  $s_k$  is the sum bit. Verify the correctness of this statement.

5.14 In Fig. 5.18 we presented the structure of a hierarchical carry-lookahead adder. Show the complete circuit for a four-bit version of this adder, built using 2 two-bit blocks.

5.22 Suppose that we want to determine how many of the bits in a six-bit unsigned number are equal to 1. Design the simplest circuit that can accomplish this task.

5.24 Show a graphical interpretation of three-digit decimal numbers, similar to Fig. 5.12. The left-most digit is 0 for positive numbers and 9 for negative numbers. Verify the validity of your answer by trying a few examples of addition and subtraction.

5.27 consider the subtractions  $26-27=99$  and  $18-34=84$ . Using the concepts presented in section 5.3.4, explain how these answers (99 and 84) can be interpreted as the correct signed results of these subtractions.