

7.4 Is the two-band subband coding filter bank containing filters $h_0(n) = \{1/\sqrt{2}, 1/\sqrt{2}\}$, $h_1(n) = \{-1/\sqrt{2}, 1/\sqrt{2}\}$, $g_0(n) = \{1/\sqrt{2}, 1/\sqrt{2}\}$, $g_1(n) = \{1/\sqrt{2}, -1/\sqrt{2}\}$ orthonormal, biorthonormal, or both?

7.9 (a) Compute the Haar transform of the 2×2 image

$$F = \begin{bmatrix} 3 & -1 \\ 6 & 2 \end{bmatrix}$$

(b) The inverse Haar transform is $F = H^T T H$, where T is the Haar transform of F and H^T is the matrix inverse of H . Show that $H_2^{-1} = H_2^T$ and use it to compute the inverse Haar transform of the result in (a).

7.12 Write an expression for scaling space V_3 as a function of scaling function $\phi(x)$. Use the Haar scaling function definition of Eq. (7.2-10) to draw the Haar V_3 scaling functions at translations $k = \{0, 1, 2\}$.

7.20 The computational complexity of an M -point FWT is $O(M)$. That is, the number of operations is proportional to M . What determines the constant of proportionality?

7.23 Compute the two-dimensional wavelet transform with respect to Haar wavelets of the 2×2 image in Problem 7.9. Draw the required filter bank and label all inputs and outputs with the proper arrays.