

## FIGURE P5.99

\***D5.100** For the circuit in Fig. P5.100, assuming all transistors to be identical with  $\beta$  infinite, derive an expression for the output current  $I_O$ , and show that by selecting

$$R_1 = R_2$$

and keeping the current in each junction the same, the current  $I_{\mathcal{O}}$  will be

$$I_O = \frac{\alpha V_{CC}}{2R_E}$$

which is independent of  $V_{BE}$ . What must the relationship of  $R_E$  to  $R_1$  and  $R_2$  be? For  $V_{CC}=10$  V and assuming  $\alpha=1$  and  $V_{BE}=0.7$  V, design the circuit to obtain an output current of

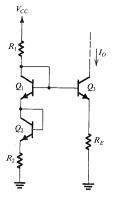


FIGURE P5.100

0.5 mA. What is the lowest voltage that can be applied to the collector of  $Q_3$ ?

**D5.101** For the circuit in Fig. P5.101 find the value of R that will result in  $I_O \simeq 2$  mA. What is the largest voltage that can be applied to the collector? Assume  $|V_{BE}| = 0.7 \text{ V}$ .



FIGURE P5.101

## SECTION 5.6: SMALL-SIGNAL OPERATION AND MODELS

**5.102** Consider a transistor biased to operate in the active mode at a dc collector current  $I_C$ . Calculate the collector signal current as a fraction of  $I_C$  (i.e.,  $i_c/I_C$ ) for input signals  $v_{be}$  of +1 mV, -1 mV, +2 mV, -2 mV, +5 mV, -5 mV, +8 mV, -8 mV, +10 mV, -10 mV, +12 mV, and -12 mV. In each case do the calculation two ways:

- (a) using the exponential characteristic, and
- (b) using the small-signal approximation.

Present your results in the form of a table that includes a column for the error introduced by the small-signal approximation. Comment on the range of validity of the small-signal approximation.

**5.103** An npn BJT with grounded emitter is operated with  $V_{BE}$  = 0.700 V, at which the collector current is 1 mA. A 10-kΩ resistor connects the collector to a +15-V supply. What is the resulting collector voltage  $V_c$ ? Now, if a signal applied to the base raises  $v_{BE}$  to 705 mV, find the resulting total collector current  $i_C$  and total collector voltage  $v_C$  using the exponential  $i_C$ - $v_{BE}$  relationship. For this situation, what are  $v_{be}$  and  $v_c$ ? Calculate the voltage gain  $v_c$ / $v_{be}$ . Compare with the value obtained using the small-signal approximation, that is,  $-g_m R_C$ .

**5.104** A transistor with  $\beta = 120$  is biased to operate at a dc collector current of 1.2 mA. Find the values of  $g_m$ ,  $r_{\pi}$ , and  $r_e$ . Repeat for a bias current of 120  $\mu$ A.

**5.105** A pnp BJT is biased to operate at  $I_C = 2.0$  mA. What is the associated value of  $g_m$ ? If  $\beta = 50$ , what is the value of

the small-signal resistance seen looking into the emitter  $(r_e)$ ? Into the base  $(r_\pi)$ ? If the collector is connected to a 5-k $\Omega$  load, with a signal of 5-mV peak applied between base and emitter, what output signal voltage results?

**D5.106** A designer wishes to create a BJT amplifier with a  $g_m$  of 50 mA/V and a base input resistance of 2000  $\Omega$  or more. What emitter-bias current should he choose? What is the minimum  $\beta$  he can tolerate for the transistor used?

**5.107** A transistor operating with nominal  $g_m$  of 60 mA/V has a  $\beta$  that ranges from 50 to 200. Also, the bias circuit, being less than ideal, allows a  $\pm 20\%$  variation in  $I_C$ . What are the extreme values found of the resistance looking into the base?

**5.108** In the circuit of Fig. 5.48,  $V_{BE}$  is adjusted so that  $V_C = 2$  V. If  $V_{CC} = 5$  V,  $R_C = 3$  kC2, and a signal  $v_{be} = 0.005$  sin  $\omega r$  volts is applied, find expressions for the total instantaneous quantities  $i_C(t)$ ,  $v_C(t)$ , and  $i_B(t)$ . The transistor has  $\beta = 100$ . What is the voltage gain?

\*D5.109 We wish to design the amplifier circuit of Fig. 5.48 under the constraint that  $V_{CC}$  is fixed. Let the input signal  $v_{be} = \hat{V}_{be}$  sin  $\omega t$ , where  $\hat{V}_{be}$  is the maximum value for acceptable linearity. For the design that results in the largest signal at the collector, without the BJT leaving the active region, show that

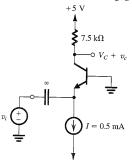
$$R_C I_C = (V_{CC} - 0.3 - \hat{V}_{be}) / (1 + \frac{\hat{V}_{be}}{V_T})$$

and find an expression for the voltage gain obtained. For  $V_{CC} = 5 \text{ V}$  and  $\hat{V}_{be} = 5 \text{ mV}$ , find the dc voltage at the collector, the amplitude of the output voltage signal, and the voltage gain.

**5.110** The following table summarizes some of the basic attributes of a number of BJTs of different types, operating as amplifiers under various conditions. Provide the missing entries.

**5.111** A BJT is biased to operate in the active mode at a dc collector current of 1.0 mA. It has a  $\beta$  of 120. Give the four small-signal models (Figs. 5.51 and 5.52) of the BJT complete with the values of their parameters.

**5.112** The transistor amplifier in Fig. P5.112 is biased with a current source I and has a very high  $\beta$ . Find the dc voltage at the collector,  $V_C$ . Also, find the value of  $g_m$ . Replace the transistor with the simplified hybrid- $\pi$  model of Fig. 5.51(a) (note that the dc current source I should be replaced with an open circuit). Hence find the voltage gain  $v_L/v_L$ .



## FIGURE P5.112

**5.113** For the conceptual circuit shown in Fig. 5.50,  $R_C = 2 \text{ kG}$ ,  $g_m = 50 \text{ mA/V}$ , and  $\beta = 100$ . If a peak-to-peak output voltage of 1 V is measured at the collector, what ac input voltage and current must be associated with the base?

**5.114** A biased BJT operates as a grounded-emitter amplifier between a signal source, with a source resistance of 10  $\Omega$ C, connected to the base and a 10- $\Omega$ C load connected as a collector resistance  $R_C$ . In the corresponding model,  $g_m$  is 40 mA/V

Transistor	a	b	c	d	e	f	g
α	1.000					0.90	
β		100		00		*	
$I_C(\text{mA})$	1.00		1.00				
$I_C$ (mA) $I_E$ (mA)		1.00				5	
$I_B$ (mA) $g_m$ (mA/V)			0.020				1.10
$g_m  (\text{mA/V})$							700
$r_e(\Omega)$ $r_{\pi}(\Omega)$				25	100		
$r_{\pi}(\Omega)$					$10.1 \text{ k}\Omega$		

(Note: Isn't it remarkable how much two parameters can reveal?)