and  $r_\pi$  is 2.5 k $\Omega$ . Draw the complete amplifier model using the hybrid- $\pi$  BJT equivalent circuit. Calculate the overall voltage gain  $(v_c/v_s)$ . What is the value of BJT  $\beta$  implied by the values of the model parameters? To what value must  $\beta$  be increased to double the overall voltage gain?

**5.115** For the circuit shown in Fig. P5.115, draw a complete small-signal equivalent circuit utilizing an appropriate T model for the BJT (use  $\alpha$ =0.99). Your circuit should show the values of all components, including the model parameters. What is the input resistance  $R_{\rm in}$ ? Calculate the overall voltage gain  $(v_{\rm o}/v_{\rm sig})$ .

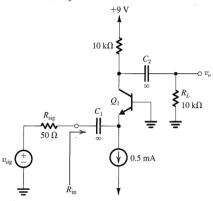


FIGURE P5.115

**5.116** In the circuit shown in Fig. P5.116, the transistor has a  $\beta$  of 200. What is the dc voltage at the collector? Find the input resistances  $R_{th}$  and  $R_{in}$  and the overall voltage gain

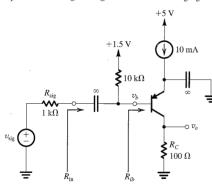


FIGURE P5.116

 $(v_o/v_{\rm sig})$ . For an output signal of  $\pm 0.4$  V, what values of  $v_{\rm sig}$  and  $v_b$  are required?

**5.117** Consider the augmented hybrid- $\pi$  model shown in Fig. 5.58(a). Disregarding how biasing is to be done, what is the largest possible voltage gain available for a signal source connected directly to the base and a very-high-resistance load? Calculate the value of the maximum possible gain for  $V_A = 25$  V and  $V_A = 250$  V.

**5.118** Reconsider the amplifier shown in Fig. 5.53 and analyzed in Example 5.14 under the condition that  $\beta$  is not well controlled. For what value of  $\beta$  does the circuit begin to saturate? We can conclude that large  $\beta$  is dangerous in this circuit. Now, consider the effect of reduced  $\beta$ , say, to  $\beta$  = 25. What values of  $r_e$ ,  $g_m$ , and  $r_\pi$  result? What is the overall voltage gain? (*Note:* You can see that this circuit, using basecurrent control of bias, is very  $\beta$ -sensitive and usually *not recommended.*)

**5.119** Reconsider the circuit shown in Fig. 5.55(a) under the condition that the signal source has an internal resistance of  $100 \Omega$ . What does the overall voltage gain become? What is the largest input signal voltage that can be used without output-signal clipping?

**D5.120** Redesign the circuit of Fig. 5.55 by raising the resistor values by a factor n to increase the resistance seen by the input  $v_i$  to 75  $\Omega$ . What value of voltage gain results? Grounded-base circuits of this kind are used in systems such as cable TV, in which, for highest-quality signaling, load resistances need to be "matched" to the equivalent resistances of the interconnecting cables.

**5.121** Using the BJT equivalent circuit model of Fig. 5.52(a), sketch the equivalent circuit of a transistor amplifier for which a resistance  $R_e$  is connected between the emitter and ground, the collector is grounded, and an input signal source  $v_b$  is connected between the base and ground. (It is assumed that the transistor is properly biased to operate in the active region.) Show that:

(a) the voltage gain between base and emitter, that is,  $v_e/v_b$ , is given by

$$\frac{v_e}{v_b} = \frac{R_e}{R_e + r_e}$$

(b) the input resistance,

$$R_{\rm in} \equiv \frac{v_b}{i_b} = (\beta + 1)(R_e + r_e)$$

Find the numerical values for  $(v_e/v_b)$  and  $R_{\rm in}$  for the case  $R_e=1~{\rm k}\Omega,~\beta=100$ , and the emitter bias current  $I_F=1~{\rm mA}$ .

**5.122** When the collector of a transistor is connected to its base, the transistor still operates (internally) in the active region because the collector-base junction is still in effect reverse biased. Use the simplified hybrid- $\pi$  model to find the

incremental (small-signal) resistance of the resulting twoterminal device (known as a diode-connected transistor.)

\*\*D5.123 Design an amplifier using the configuration of Fig. 5.55(a). The power supplies available are  $\pm 10$  V. The input signal source has a resistance of 100  $\Omega$ , and it is required that the amplifier input resistance match this value. (Note that  $R_{\rm in} = r_e$ ,  $I/R_E \simeq r_e$ .) The amplifier is to have the greatest possible voltage gain and the largest possible output signal but retain small-signal linear operation (i.e., the signal component across the base–emitter junction should be limited to no more than 10 mV). Find appropriate values for  $R_E$  and  $R_C$ . What is the value of voltage gain realized?

\*5.124 The transistor in the circuit shown in Fig. P5.124 is biased to operate in the active mode. Assuming that  $\beta$  is very large, find the collector bias current  $I_C$ . Replace the transistor with the small-signal equivalent circuit model of Fig. 5.52(b) (remember to replace the dc power supply with a short circuit). Analyze the resulting amplifier equivalent circuit to show that

$$\frac{v_{o1}}{v_i} = \frac{R_E}{R_E + r_e}$$

$$\frac{v_{o2}}{v_i} = \frac{-\alpha R_C}{R_E + r_e}$$

Find the values of these voltage gains (for  $\alpha = 1$ ). Now, if the terminal labeled  $v_{o1}$  is connected to ground, what does the voltage gain  $v_{o2}/v_l$  become?

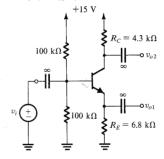


FIGURE P5.124

## SECTION 5.7: SINGLE-STAGE BJT AMPLIFIERS

**5.125** An amplifier is measured to have  $R_i=10~\mathrm{k}\Omega,~A_{vo}=100~\mathrm{V/V},~\mathrm{and}~R_o=100~\Omega.$  Also, when a load resistance  $R_L$  of 1 k $\Omega$  is connected between the output terminals, the input resistance is found to decrease to 8 k $\Omega$ . If the amplifier is fed with a signal source having an internal resistance of 2 k $\Omega$ , find  $G_m, A_v, G_{vo}, G_v, R_{out},~\mathrm{and}~A_i$ .

**5.126** Figure P5.126 shows an alternative equivalent circuit for representing *any* linear two-port network including voltage

amplifiers. This non-unilateral equivalent circuit is based on the *g*-parameter two-port representation (see Appendix B).

(a) Using the values of  $R_{\rm h}$ ,  $A_{\rm por}$ , and  $R_{\rm o}$  found in Example 5.17 together with the measured value of  $R_{\rm in}$  of 400 k $\Omega$  obtained when a load  $R_{\rm L}$  of 10 k $\Omega$  is connected to the output, determine the value of the feedback factor f.

(b) Now, use the equivalent circuit of Fig. P5.126 to determine the value of  $R_{\rm out}$  obtained when the amplifier is fed with a signal generator having  $R_{\rm sig}=100~k\Omega.$  Check your result against that found in Example 5.17.

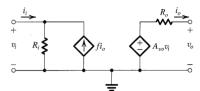


FIGURE P5.126

**5.127** Refer to Table 5.5. By equating the expression for  $G_v$  obtained from Equivalent Circuit A to that obtained from Equivalent Circuit C with  $G_{vo} = [R_i/(R_i + R_{\rm sig})]A_{vo}$ , show that

$$\frac{R_{\rm in}}{R_i} \frac{R_{\rm sig} + R_i}{R_{\rm cir} + R_{\rm in}} = \frac{R_L + R_o}{R_I + R_{\rm out}}$$

Now, use this expression to:

- (a) Show that for  $R_L = \infty$ ,  $R_{in} = R_i$ .
- (b) Show that for  $R_{\text{sig}} = 0$ ,  $R_{\text{out}} = R_o$ .
- (c) Find  $R_{\text{out}}$  when  $R_{\text{sig}} = \infty$  (i.e., the amplifier input is open-circuited), and evaluate its value for the amplifier specified in Example 5.17.

**5.128** A common-emitter amplifier of the type shown in Fig. 5.60(a) is biased to operate at  $I_C=0.2$  mA and has a collector resistance  $R_C=24$  k $\Omega$ . The transistor has  $\beta=100$  and a large  $V_A$ . The signal source is directly coupled to the base, and  $C_{C1}$  and  $R_B$  are eliminated. Find  $R_{\rm in}$ , the voltage gain  $A_{vo}$ , and  $R_{o'}$ . Use these results to determine the overall voltage gain when a 10-k $\Omega$  load resistor is connected to the collector and the source resistance  $R_{vir}=10$  k $\Omega$ .

**5.129** Repeat Problem 5.128 with a 125-Ω resistance included in the signal path in the emitter. Furthermore, contrast the maximum amplitude of the input sine wave that can be applied with and without  $R_v$  assuming that to limit distortion the signal between base and emitter is not to exceed 5 mV.

**5.130** For the common-emitter amplifier shown in Fig. P5.130, let  $V_{CC}=9$  V,  $R_1=27$  k $\Omega$ ,  $R_2=15$  k $\Omega$ ,  $R_E=1.2$  k $\Omega$ , and  $R_C=2.2$  k $\Omega$ . The transistor has  $\beta=100$  and  $V_A=100$  V.



Calculate the dc bias current  $I_E$ . If the amplifier operates between a source for which  $R_{\rm sig}=10~{\rm k}\Omega$  and a load of  $2~{\rm k}\Omega$ , replace the transistor with its hybrid- $\pi$  model, and find the values of  $R_{\rm in}$ , the voltage gain  $v_o/v_{\rm sig}$ , and the current gain  $i_o/i_t$ .

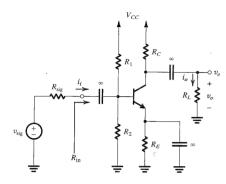


FIGURE P5.130

- **D5.131** Using the topology of Fig. P5.130, design an amplifier to operate between a 10-kΩ source and a 2-kΩ load with a gain  $v_o/v_{\rm sig}$  of -8 V/V. The power supply available is 9 V. Use an emitter current of approximately 2 mA and a current of about one-tenth of that in the voltage divider that feeds the base, with the de voltage at the base about one-third of the supply. The transistor available has  $\beta = 100$  and  $V_A = 100$  V. Use standard 5% resistor (see Appendix G).
- **5.132** A designer, having examined the situation described in Problem 5.130 and estimating the available gain to be approximately -8 V/V, wishes to explore the possibility of improvement by reducing the loading of the source by the amplifier input. As an experiment, the designer varies the resistance levels by a factor of approximately 3:  $R_1$  to  $82 \text{ k}\Omega$ ,  $R_2$  to  $47 \text{ k}\Omega$ ,  $R_E$  to  $3.6 \text{ k}\Omega$ , and  $R_C$  to  $6.8 \text{ k}\Omega$  (standard values of 5%-tolerance resistors). With  $V_{CC} = 9 \text{ V}$ ,  $R_{\text{sig}} = 10 \text{ k}\Omega$ ,  $R_L = 2 \text{ k}\Omega$ ,  $\beta = 100$ , and  $V_A = 100$  V, what does the gain become? Comment.
- **D5.133** Consider the CE amplifier circuit of Fig. 5.60(a). It is required to design the circuit (i.e., find values for I,  $R_B$ , and  $R_C$ ) to meet the following specifications:
- (a)  $R_{in} \cong 5 \text{ k}\Omega$ .
- (b) the dc voltage drop across  $R_B$  is approximately 0.5 V.
- (c) the open-circuit voltage gain from base to collector is the maximum possible, consistent with the requirement that the collector voltage never falls by more than approximately  $0.5\,\mathrm{V}$

below the base voltage with the signal between base and emitter being as high as  $5\ mV$ .

Assume that  $u_{\rm sig}$  is a sinusoidal source, the available supply  $V_{CC}=5$  V, and the transistor has  $\beta=100$  and a very large Early voltage. Use standard 5%-resistance values, and specify the value of I to one significant digit. What base-to-collector open-circuit voltage gain does your design provide? If  $R_{\rm sig}=R_L=10~{\rm k}\Omega$ , what is the overall voltage gain?

- **D5.134** In the circuit of Fig. P5.134,  $v_{\rm sig}$  is a small sinewave signal with zero average. The transistor  $\beta$  is 100.
- (a) Find the value of  $R_E$  to establish a dc emitter current of about 0.5 mA.
- (b) Find  $R_C$  to establish a dc collector voltage of about +5 V. (c) For  $R_C=10~\mathrm{k}\Omega$  and the transistor  $r_o=200~\mathrm{k}\Omega$ , draw the small-signal equivalent circuit of the amplifier and determine its overall voltage gain.

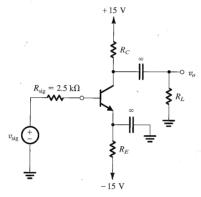
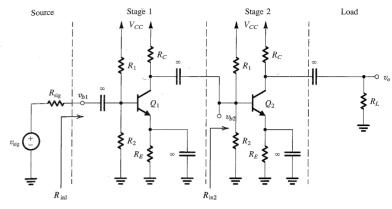


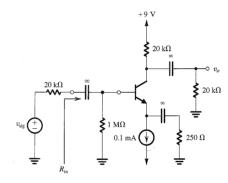
FIGURE P5.134

- \*5.135 The amplifier of Fig. P5.135 consists of two identical common-emitter amplifiers connected in cascade. Observe that the input resistance of the second stage,  $R_{\rm in2}$ , constitutes the load resistance of the first stage.
- (a) For  $V_{CC}$  = 15 V,  $R_1$  = 100 k $\Omega$ ,  $R_2$  = 47 k $\Omega$ ,  $R_E$  = 3.9 k $\Omega$ ,  $R_C$  = 6.8 k $\Omega$ , and  $\beta$  = 100, determine the dc collector current and dc collector voltage of each transistor.
- (b) Draw the small-signal equivalent circuit of the entire amplifier and give the values of all its components. Neglect  $r_{cl}$  and  $r_{c2}$ .
- (c) Find  $R_{\text{inl}}$  and  $v_{b1}/v_{\text{sig}}$  for  $R_{\text{sig}} = 5 \text{ k}\Omega$ .
- (d) Find  $R_{in2}$  and  $v_{b2}/v_{b1}$ .
- (e) For  $R_L = 2 k\Omega$ , find  $v_o / v_{h2}$ .
- (f) Find the overall voltage gain  $v_a/v_{\rm sig}$ .



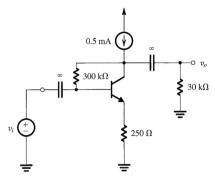
## FIGURE P5.135

**5.136** In the circuit of Fig. P5.136,  $v_{\rm sig}$  is a small sine-wave signal. Find  $R_{\rm in}$  and the gain  $v_o/v_{\rm sig}$ . Assume  $\beta=100$ . If the amplitude of the signal  $v_{be}$  is to be limited to 5 mV, what is the largest signal at the input? What is the corresponding signal at the output?



## FIGURE P5.136

- \*5.137 The BJT in the circuit of Fig. P5.137 has  $\beta = 100$ .
- (a) Find the dc collector current and the dc voltage at the collector.
- (b) Replacing the transistor by its T model, draw the small-signal equivalent circuit of the amplifier. Analyze the resulting circuit to determine the voltage gain  $v_0/v_l$ .



## FIGURE P5.137

- \*5.138 Refer to the voltage-gain expression (in terms of transistor  $\beta$ ) given in Eq. (5.135) for the CE amplifier with a resistance  $R_e$  in the emitter. Let the BJT be biased at an emitter current of 0.5 mA. The source resistance  $R_{\rm sig}$  is 10 k $\Omega$ . The BJT  $\beta$  is specified to lie in the range of 50 to 150 with a nominal value of 100.
- (a) What is the ratio of maximum to minimum voltage gain obtained without R.?
- (b) What value of  $R_e$  should be used to limit the ratio of maximum to minimum gain to 1.2?
- (c) If the  $R_e$  found in (b) is used, by what factor is the gain reduced (compared to the case without  $R_e$ ) for a BJT with a nominal  $\beta$ ?