EE 322 Advanced Electronics, Spring 2012 Homework #1 solution

HH 6.1

We are going to place a voltage divider on both the reference, and on the output. The output problem hints that we should compare a fraction of the output to half of the input, so let us place a voltage divider across the input. I will use two 4.7K resistors for that. We thus have a input of $V_{+} = 7.15/2 = 3.575$ V on the input.

On the output we want to be able to adjust the voltage from +5 V to +10 V. We must have a voltage divider which can take a fraction of this and compare it to the input of the comparator. I will use a 10K potentiometer as the variable element. Let's say that when the potentiometer has zero resistance we want +5 V on the output whereas when the potentiometer has full resistance we want +10 V on the output. We will use two more resistors in this configuration,



and the relevant equations are

$$V_{\text{out,max}} \frac{R_1}{R_{10} + R_2 + R_1} = V_-$$
 and $V_{\text{out,min}} \frac{R_1}{R_2 + R_1} = V_-$

Dividing the two equations and re-arranging we get

$$\frac{V_{\rm out,max}}{V_{\rm out,min}} = \frac{R_{10} + R_2 + R_1}{R_2 + R_1}$$

Which gives us

$$2(R_2 + R_1) = R_{10} + R_2 + R_1$$

or

$$R_2 + R_1 = R_{10} = 10K$$

Next we go back to the equation for the minimum voltage and find that

$$\frac{V_{\rm out,min}}{V_{-}} = \frac{R_2 + R_1}{R_1} = \frac{R_2}{R_1} + 1$$

Inserting $V_{\text{out,min}}/V_{-} = 5/3.575 = 1.4$, we get

$$\frac{R_2}{R_1} = 0.4$$

Inserting $R_2 = R_{10} - R_1$ we get

$$\frac{R_{10} - R_1}{R_1} = 0.4$$

$$R_{10} - R_1 = 0.4R_1$$
 $R_1 = \frac{R_{10}}{1.4} = 7.14K$

Then

$$R_2 = R_{10} - R_1 = 10 - 7.14 = 2.86K$$

To limit the current to $I_{\text{max}} = 50 \text{ mA}$, we insert a current-sensing resistor, R_{CS} such that

$$V_{BE,min} = I_{\max} R_{CS} \Longrightarrow R_{CS} = \frac{V_{BE,min}}{I_{\max}} = \frac{0.5}{50 \times 10^{-3}} = 10\,\Omega$$

HH 6.2

The scenario is illustrated in this figure



The temperature difference can be written as

$$T_{\text{junction}} - T_{\text{ambient}} = (\theta_{2\text{N5320}} + \theta_{\text{TXBF}}) F$$

And we wish to find P_{max} corresponding to $T_{\text{junction,max}} = 200^{\circ}C$.

$$P_{\rm max} = \frac{T_{\rm junction,max} - T_{\rm ambient}}{\theta_{\rm 2N5320} + \theta_{\rm TXBF}}$$

Inserting values we get

$$P_{\rm max} = \frac{200 - 25}{17.5 + 70} = 2 \,\rm W$$

HH 6.3

I will first find the relationship between R_2 and R_1 with the formula

$$\frac{I_{\text{max}}}{I_{\text{SC}}} = 1 + \frac{R_2}{R_1 + R_2} \frac{V_{\text{reg}}}{V_{\text{BE}}}$$

assuming that having R_1 and R_2 above $1K\Omega$ will be sufficient to not draw significant current away from the current sensing resistor. We find

$$\frac{R_2}{R_1 + R_2} = \left(\frac{I_{\text{max}}}{I_{\text{SC}}} - 1\right) \frac{V_{\text{BE}}}{V_{\text{reg}}}$$

Inserting values from the problem we get

$$\frac{R_2}{R_1 + R_2} = \left(\frac{1}{0.4} - 1\right)\frac{0.5}{5} = 0.15$$

If we choose $R_2 = 1K$, we get

$$R_2 = 0.15(R_1 + R_2)R_2 = 0.15R_1 + 0.15R_2 \\ 0.85R_2 = 0.15R_1$$

$$R_1 = \frac{1 - 0.15}{0.15} R_2 = 5.7K$$

Next we want to find the value of the current sensing resistor, R_S . We will use the formula

$$I_{\rm SC} = \frac{1}{R_S} \left(1 + \frac{R_2}{R_1} \right) V_{\rm BE}$$

or

$$R_S = \frac{1}{I_{\rm SC}} \left(1 + \frac{R_2}{R_1} \right) V_{\rm BE}$$

Inserting values we get

$$R_S = \frac{1}{0.4} \left(1 + \frac{1}{5.7K} \right) 0.5 = 1.25 \,\Omega$$

Note that the value of R_S is much smaller than the values we picked for R_1 and R_2 .