

- **Decimal, Hexadecimal and Binary Numbers**

- Binary numbers are a code, and represent what the programmer intends for the code
- Convert binary and hex numbers to unsigned decimal
- Convert unsigned decimal to hex
- Unsigned number line and wheel
- Signed number line and wheel
- Binary, Hex, Signed and Unsigned Decimal
- Signed number representation --- 2's Complement form
- Using the 1's complement table to find 2's complements of hex numbers
- Overflow and Carry
- Addition and subtraction of binary and hexadecimal numbers
- The Condition Code Register (CCR): N, Z, V and C bits

| Binary | Hex | Decimal |
|--------|-----|---------|
| 0000   | 0   | 0       |
| 0001   | 1   | 1       |
| 0010   | 2   | 2       |
| 0011   | 3   | 3       |
| 0100   | 4   | 4       |
| 0101   | 5   | 5       |
| 0110   | 6   | 6       |
| 0111   | 7   | 7       |
| 1000   | 8   | 8       |
| 1001   | 9   | 9       |
| 1010   | A   | 10      |
| 1011   | B   | 11      |
| 1100   | C   | 12      |
| 1101   | D   | 13      |
| 1110   | E   | 14      |
| 1111   | F   | 15      |

**What does a number represent?**

Binary numbers are a code, and represent what the programmer intends for the code.

**0x72** Some possible meanings:

'r' (ASCII)

INC MEM (hh ll) (HC12 instruction)

2.26V (Input from A/D converter)

114<sub>10</sub> (Unsigned number)

114<sub>10</sub> (Signed number)

Set temperature in room to 69 °F

Set cruise control speed to 120 mph

**Binary to Unsigned Decimal:**

Convert Binary to Unsigned Decimal

$1111011_2$

$$1 \times 2^6 + 1 \times 2^5 + 1 \times 2^4 + 1 \times 2^3 + 0 \times 2^2 + 1 \times 2^1 + 1 \times 2^0$$

$$1 \times 64 + 1 \times 32 + 1 \times 16 + 1 \times 8 + 0 \times 4 + 1 \times 2 + 1 \times 1$$

$123_{10}$

**Hex to Unsigned Decimal**

Convert Hex to Unsigned Decimal

$82D6_{16}$

$$8 \times 16^3 + 2 \times 16^2 + 13 \times 16^1 + 6 \times 16^0$$

$$8 \times 4096 + 2 \times 256 + 13 \times 16 + 6 \times 1$$

$33494_{10}$

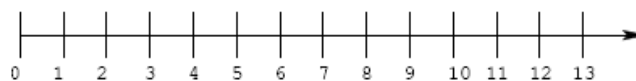
**Unsigned Decimal to Hex**

Convert Unsigned Decimal to Hex

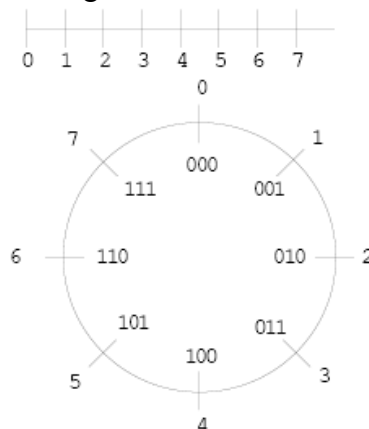
| Division | Q  | R       |     |
|----------|----|---------|-----|
|          |    | Decimal | Hex |
| 721/16   | 45 | 1       | 1   |
| 45/16    | 2  | 13      | D   |
| 2/16     | 0  | 2       | 2   |

$$721_{10} = 2D1_{16}$$

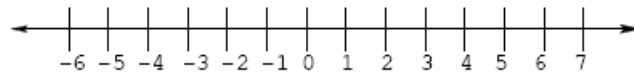
Unsigned Number Line: Numbers go from 0 to  $\infty$



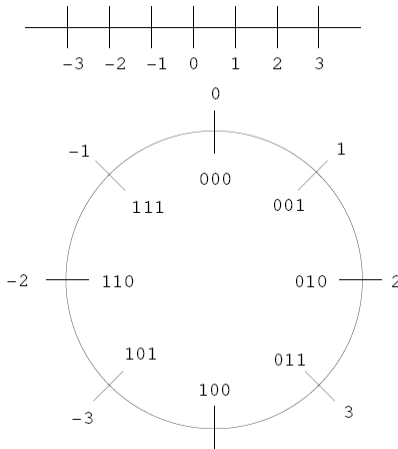
Unsigned Number Wheel: Numbers go from 0 to  $2N - 1$



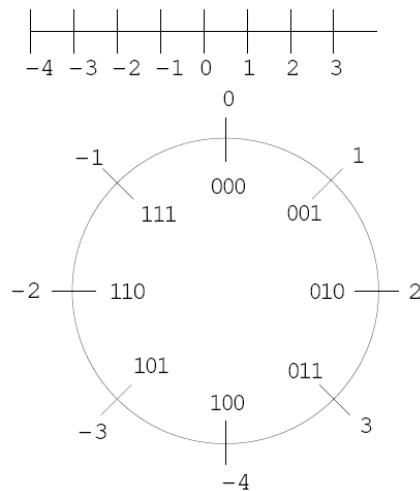
Signed Number Line: Numbers go from  $-\infty$  to  $\infty$



Number Wheel: What to do about  $100_2$

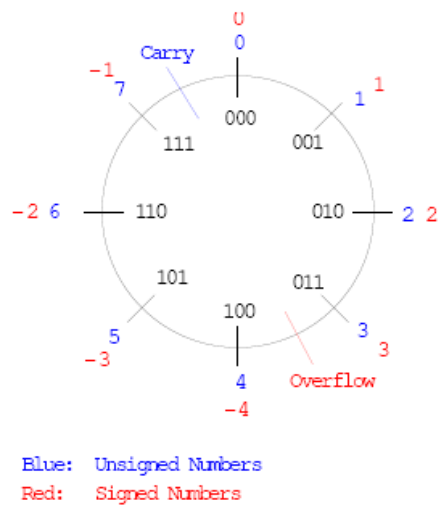


Number Wheel: Numbers go from  $-2^{(N-1)}$  to  $2^{(N-1)} - 1$



### Number Wheel: Carry and Overflow

- Carry applies to **unsigned numbers** — when adding or subtracting, result is incorrect.
- Overflow applies to **signed numbers** — when adding or subtracting, result is incorrect.



Binary, Hex and Decimal (Signed & Unsigned) Numbers (4-bit representation)

| Binary | Hex | Decimal  |        |
|--------|-----|----------|--------|
|        |     | Unsigned | Signed |
| 0000   | 0   | 0        | 0      |
| 0001   | 1   | 1        | 1      |
| 0010   | 2   | 2        | 2      |
| 0011   | 3   | 3        | 3      |
| 0100   | 4   | 4        | 4      |
| 0101   | 5   | 5        | 5      |
| 0110   | 6   | 6        | 6      |
| 0111   | 7   | 7        | 7      |
| 1000   | 8   | 8        | -8     |
| 1001   | 9   | 9        | -7     |
| 1010   | A   | 10       | -6     |
| 1011   | B   | 11       | -5     |
| 1100   | C   | 12       | -4     |
| 1101   | D   | 13       | -3     |
| 1110   | E   | 14       | -2     |
| 1111   | F   | 15       | -1     |

## Signed Number Representation in 2's Complement Form:

If the most significant bit (MSB) is 0 (most significant hex digit 0–7), then the number is positive.

Get decimal equivalent by converting number to decimal, and use the + sign.

**Example for 8-bit number:**

$$\begin{aligned} 3A_{16} &\rightarrow + (3 \times 16^1 + 10 \times 16^0)_{10} \\ &+ (3 \times 16 + 10 \times 1)_{10} \\ &+ 58_{10} \end{aligned}$$

If the most significant bit is 1 (most significant hex digit 8–F), then the number is negative.

Get decimal equivalent by taking 2's complement of number, converting to decimal, and using – sign.

Example for 8-bit number:

$$\begin{aligned} A3_{16} &\rightarrow - (5D)_{16} \\ &- (5 \times 16^1 + 13 \times 16^0)_{10} \\ &- (5 \times 16 + 13 \times 1)_{10} \\ &- 93_{10} \end{aligned}$$

## One's complement table makes it simple to finding 2's complements

|   |   |
|---|---|
| 0 | F |
| 1 | E |
| 2 | D |
| 3 | C |
| 4 | B |
| 5 | A |
| 6 | 9 |
| 7 | 8 |

To take two's complement, add one to one's complement.

Take two's complement of **D0C3**:

$$2F3C + 1 = 2F3D$$

- Overflow and Carry assume you have a fixed word size
- A carry is generated when you add **two unsigned numbers** together, and the result is too large to fit in the fixed word size.
- A carry is generated when you subtract **two unsigned numbers**, and the result should be negative.
- An overflow is generated when you add or subtract **two signed numbers**, and the fixed-length answer has the wrong sign.

### Addition and Subtraction of Binary and Hexadecimal Numbers

1) Limit number of digits to specified word size.

4-bit word:

$$\begin{array}{r} 1101 \\ + 1011 \\ \hline 1\ 1000 \end{array}$$

Keep only 4 bits in answer, carry is set

2) It does not matter if numbers are signed or unsigned – the mechanics are the same  
Do the operation, then determine if carry and/or overflow bits are set.

4-bit word:

$$\begin{array}{r} 1101\ \text{Neg} \\ + 1001\ \text{Neg} \\ \hline 1\ 0110\ \text{Pos} \end{array}$$

Keep only 4 bits in answer, overflow is clear

**Condition Code Register (CCR) gives information on the result of last operation**

|   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|
| S | X | H | I | N | Z | V | C |
|---|---|---|---|---|---|---|---|

### Condition Code Register – 8 FFs

- C** – Carry : 1 -> last operation generated a carry
- V** – Overflow : 1 -> last operation generated an overflow
- Z** – Zero : 1 -> result zero, 0 -> result not zero
- N** – Negative : most significant bit of result
- I** – Interrupt mask
- H** – Half carry
- X** – Interrupt mask
- S** – Stop disable

**Note:** Not all HC12 instructions change CCR bits.

A bit in the CCR is the result of the last executed instruction which affects that bit. For example, consider the following instruction sequence:

```
aba           ; Add B to A  
staa $0900   ; Store A in address $0900
```

The ABA instruction will change the **H, N, Z, V and C bits** of the CCR. The STAA instruction will change the **N and Z bit, and clear the V bit**. After the two instructions, the H and C bits will reflect the result of the ABA instruction; the N and Z bits will reflect the result of the STAA instruction (was the number stored negative or zero?), and the V bit will be 0.

**Overflow occurs only under certain addition and subtraction operations**

- If you add a positive and a negative number, an overflow never occurs.
- If you subtract two positive numbers, an overflow never occurs.
- If you subtract two negative numbers, an overflow never occurs.