

EE 341 – Homework Chapter 5

5.3 Three functions $x_1(t)$, $x_2(t)$, and $x_3(t)$ have an identical magnitude spectrum $|X(\omega)|$ but different phase spectra denoted, respectively, by $\angle X_1(\omega)$, $\angle X_2(\omega)$, and $\angle X_3(\omega)$; magnitude and phase plots are shown in Figs. P5.3 (a) – (d). By representing the CTFTs as $X_p(\omega) = |X(\omega)|\exp(j\angle X_n(\omega))$, for $p=1,2$, and 3 , and calculating the inverse CTFT, determine the functions $x_1(t)$, and $x_2(t)$, and $x_3(t)$.

5.9 Using table 5.2 and the properties of the CTFT, calculate the CTFT of the following functions:

(a) $x_1(t) = 5 + 3 \cos(10t) - 7e^{-2t} \sin(3t) u(t)$

(b) $x_2(t) = 1/\pi t$

(c) $x_3(t) = t^2 e^{-4|t-5|}$

5.17 For each of the following functions, (i) draw a rough sketch of the function, and (ii) determine if the CTFT exists by evaluating Eq. (5.59):

(a) $x_1(t) = e^{-a|t|}$, with $a \in R^+$

(b) $x_2(t) = e^{-at} \cos(\omega_0 t) u(t)$, with $a, \omega_0 \in R^+$

(c) $x_3(t) = t^4 e^{-at} u(t)$, with $a \in R^+$

5.22 Determine the T.F. of the system shown in Fig. P5.22 (a). Calculate the output of the system for the input signal shown in Fig. P5.22(b).

5.28 Using the results derived in Section 5.9.2 and the linearity property of the CTFT, calculate the output of the system shown in Fig. P5.23 for the following input signals. Assume $R=1 \text{ M}\Omega$ and $C=0.1 \text{ }\mu\text{F}$. Hint: can use the results of Example 5.30 in this problem.

(i) $x_1(t) = \sin(3t)$

(ii) $x_2(t) = \cos(3t) - 5\sin(6t + 30^\circ)$

(iii) $x_3(t) = \cos(2t) + \sin(2000t)$

5.35 (MATLAB exercise) Compute the output response $y(t)$ from Problem 5.29 by computing the CTFT for $x(t)$ and $h(t)$, multiplying the CTFTs and then taking the inverse CTFT of the result.