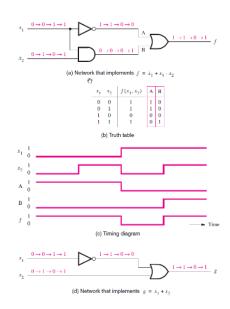
Verify that the logic circuits in (a) and (d) are equivalent. (Find the expression for f in both cases and show they are equivalent from truth tables).



2.- Determine whether or not the following expressions are valid, i.e., whether the left- and right-hand sides represent the same function.

(a) 
$$\bar{x}_1 x_3 + x_1 x_2 \bar{x}_3 + \bar{x}_1 x_2 + x_1 \bar{x}_2 = \bar{x}_2 x_3 + x_1 \bar{x}_3 + x_2 \bar{x}_3 + \bar{x}_1 x_2 x_3$$

(b) 
$$x_1\overline{x}_3 + x_2x_3 + \overline{x}_2\overline{x}_3 = (x_1 + \overline{x}_2 + x_3)(x_1 + x_2 + \overline{x}_3)(\overline{x}_1 + x_2 + \overline{x}_3)$$

(c) 
$$(x_1 + x_3)(\overline{x}_1 + \overline{x}_2 + \overline{x}_3)(\overline{x}_1 + x_2) = (x_1 + x_2)(x_2 + x_3)(\overline{x}_1 + \overline{x}_3)$$

3.- Use algebraic manipulation to prove that

$$xy + yz + \overline{x}z = xy + \overline{x}z.$$

4.- Use the Venn diagram to prove that

$$(x_1 + x_2 + x_3) \cdot (x_1 + x_2 + \overline{x}_3) = x_1 + x_2$$