

For Z_1 , $\begin{cases} P = 500W \\ pf = 0.8 \text{ lagging} \end{cases}$

for Z_2 , $\begin{cases} P = 1000W \\ pf = 0.9 \text{ lagging} \end{cases}$

for Z_3 , $\begin{cases} P = 1500W \\ pf = 0.95 \text{ leading} \end{cases}$

$$|I_1| = \frac{500}{115 \times 0.8} = 5.435; \quad \theta = \cos^{-1} 0.8 = 36.87^\circ$$

$$\therefore \underline{\hat{I}_1} = 5.435 \angle -36.87^\circ$$

$$\underline{\hat{I}_2} = \frac{1000}{115 \times 0.9} \angle -\cos^{-1}(0.9) = 9.66 \angle -25.84^\circ$$

$$\underline{\hat{I}_3} = \frac{1500}{830 \times 0.95} \angle +\cos^{-1}(0.95) = 6.865 \angle 18.19^\circ$$

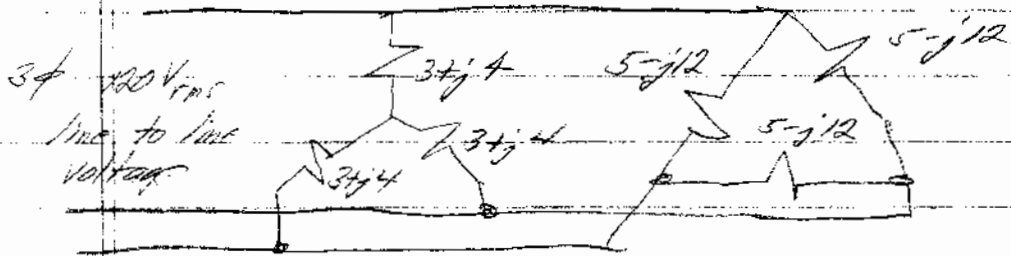
$$\underline{\hat{I}_{s1}} = \underline{\hat{I}_1} + \underline{\hat{I}_3} = 4.348 - j3.241 + 6.522 + j2.143$$

$$\underline{\hat{I}_{s1}} = \boxed{10.87 - j1.118} = 10.92 \angle -5.27^\circ$$

$$\underline{\hat{I}_{s2}} = \underline{\hat{I}_2} + \underline{\hat{I}_3} = 8.694 - j4.21 + 6.522 + j2.143 = 15.22 - j2.07$$

$$\underline{\hat{I}_{s2}} = 15.36 \angle -7.75^\circ$$

9.44

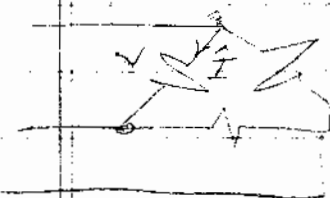


convert Y load to delta $Z_D = 3Z_Y = 9 + j12$

this gives a Δ connected load with each impedance =
$$\frac{(9 + j12)(5 - j12)}{14} = \frac{(45 + 144) + j(-48)}{14}$$

$$Z_{total} = 13.5 - j3.429 = 13.93 \angle -14.25^\circ$$

$$pf = \cos(14.25) = 0.97$$



$$I_{rms} = \frac{120}{13.93 \angle -14.25} = 8.615 \angle 14.25$$

$$P_{/phase} = I_{rms}^2 \times 13.5 = 1001.9 \text{ Watts}$$

$$total P = 3 P_{/phase} = \boxed{3005.8 \text{ W}}$$
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or
$$P_{/phase} = V_{rms} I_{rms} \cos \theta = 120 \times 8.615 \cos(14.25^\circ) = 1001.99$$