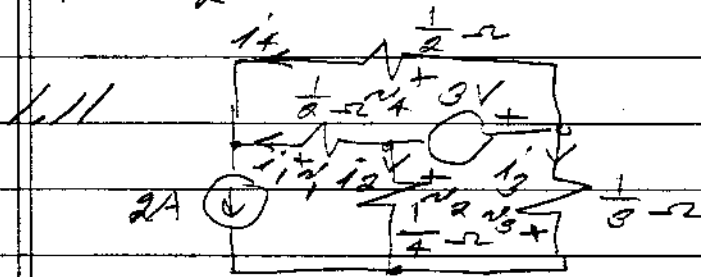


$$14 \quad q = 4e^{-2t} \quad \therefore i = \frac{dq}{dt} = -8e^{-2t} \quad \leftarrow$$



$$a) \quad i_1 = -2A \quad \therefore v_1 = -i_1 \left(\frac{1}{8}\right) = 2V \quad \leftarrow$$

$$b) \quad v_2 = -\frac{11}{7}V \quad \therefore i_2 = \frac{v_2}{\frac{1}{4}} = -\frac{44}{7}A \quad \leftarrow$$

$$c) \quad i_3 = \frac{30}{7}A \quad \therefore v_3 = -i_3 \left(\frac{1}{3}\right) = -\frac{10}{7}V \quad \leftarrow$$

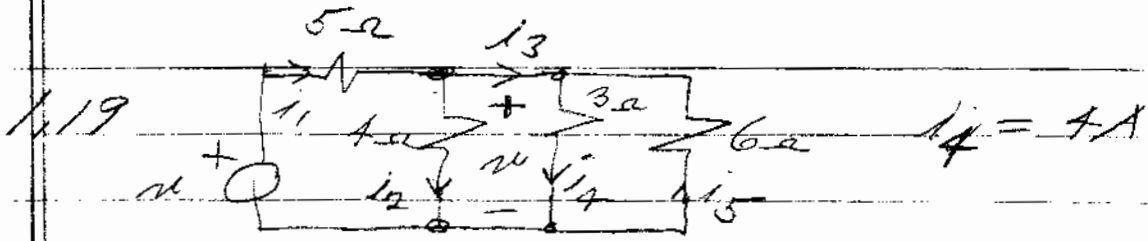
$$d) \quad v_4 = 2V \quad \therefore i_4 = v_4 \times 2 = 4A \quad \leftarrow$$

$$v_1 - 3 + v_4 = 0$$

$$1 - 3 + 2 = 0 \quad \checkmark$$

EE 211

Homework 2

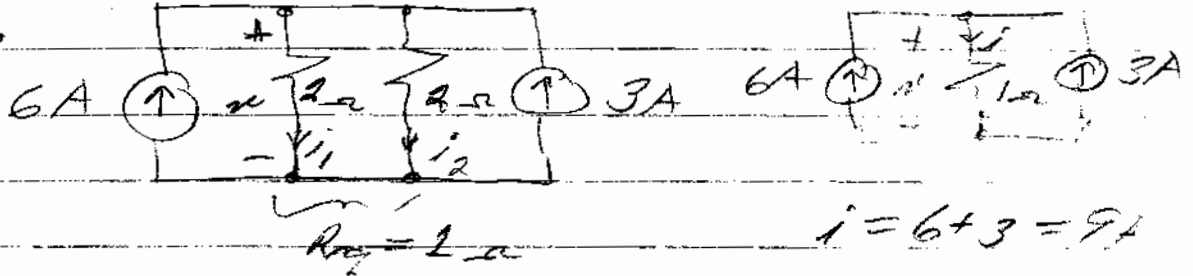


$$v = 3 + i_4 = 12 \text{ V}$$

$$\text{So } i_2 = \frac{12}{4} = 3 \text{ A}, \quad i_5 = -\frac{12}{6} = -2 \text{ A}, \quad i_3 = i_4 - i_5 = 6 \text{ A}$$

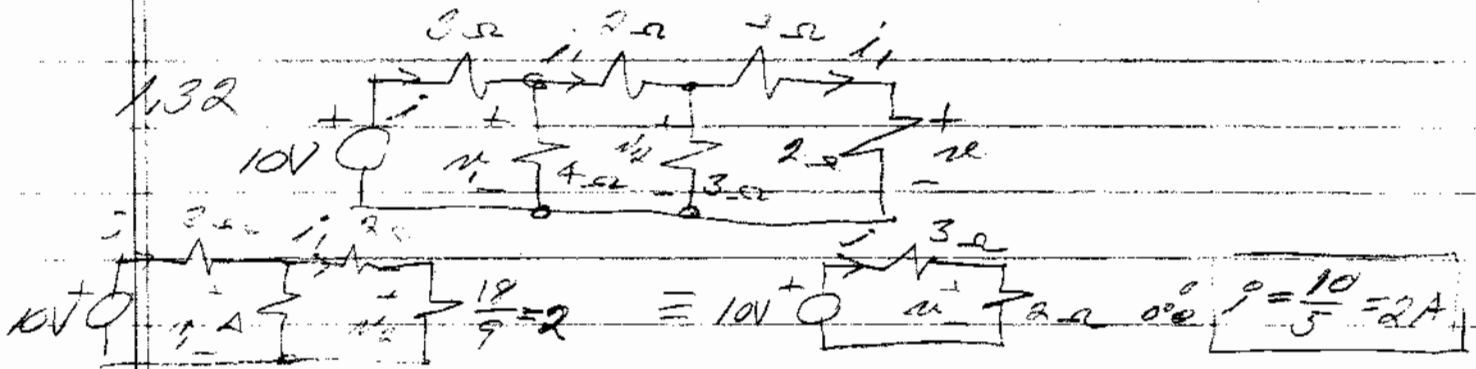
$$i_1 = i_2 + i_3 = 9 \text{ A}$$

1.30a

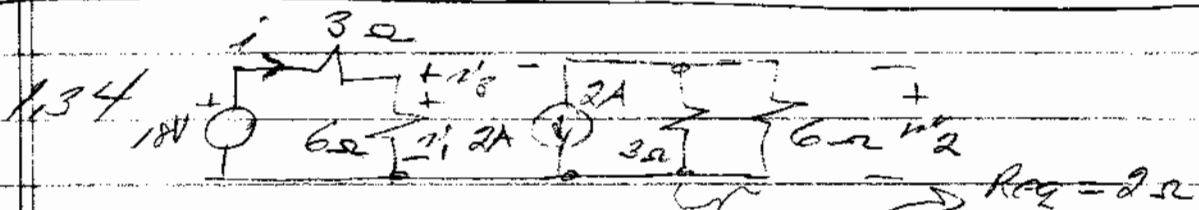


$$\text{So } v = 9 \text{ V}$$

$$\text{and } i_1 = i_2 = \frac{v}{2} = \frac{9}{2} \text{ A}$$



$$v_1 = 10V \times \frac{2}{5} = 4V ; v_2 = 4 + \frac{2}{4} = 2V ; i_1 = \frac{1}{3}A \text{ and } v_3 = \frac{2}{3}V$$



$$a) \quad i = \frac{18}{9} = 2A \quad \therefore \quad v_1 = 18V, \quad v_2 = -2 \times R_{eq} = -4V$$

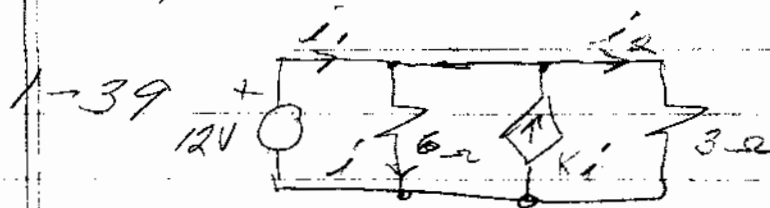
$$v_3 = v_1 - v_2 = 18 + 4 = 16V$$

b) for ab connection removed

i, v_1, v_2 do not change but v_3 can be anything!!

EE, 211

Homework 4

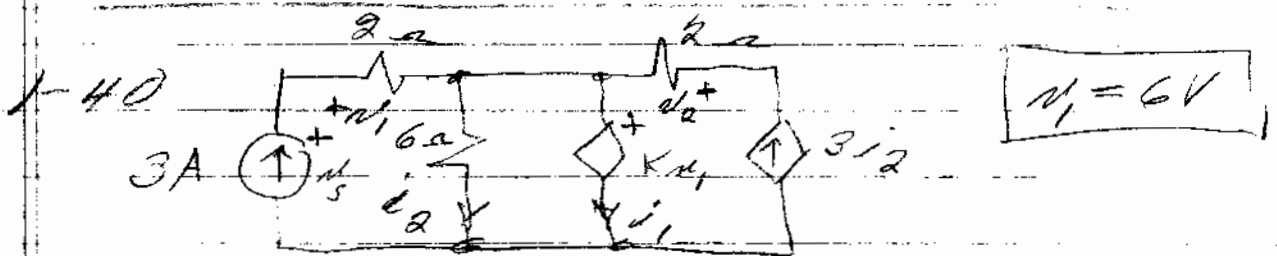


a) $K=2$; $i_1 = 2A$; $i_2 = 4A$; $i_1 = 2 + 4 - K \cdot 2$

$i_1 = 6 - 4 = 2A$

b) $K=3$; $i_1 = 6 - 6 = 0$

c) $K=4$; $i_1 = 6 - 8 = -2A$



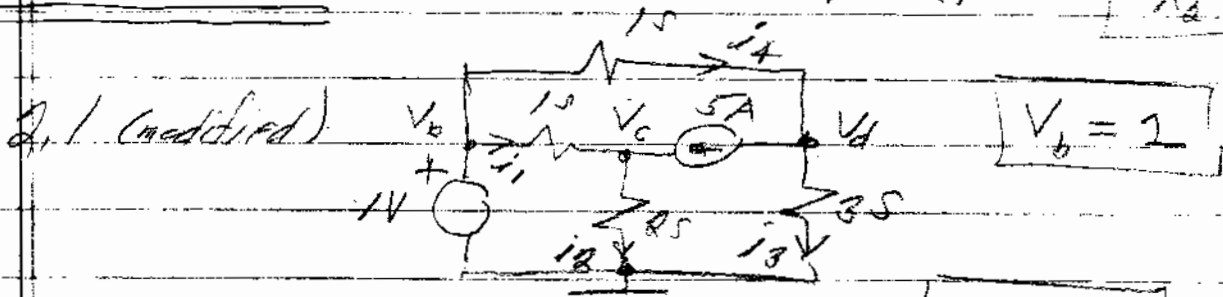
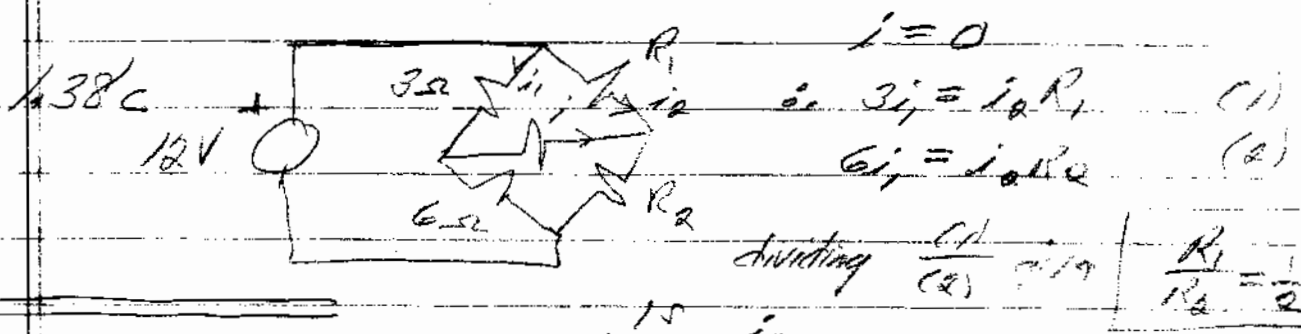
a) $K=2$

$$i_2 = \frac{K i_1}{6} = K ; -3 + \frac{K i_1}{6} + i_1 - 3 i_2 = 0$$

or $i_1 = 3 - K + 3K = 3 + 2K = 7A$

b) $i_1 = 3 + 2(3) = 9A$

c) $i_1 = 3 + 2(4) = 11A$



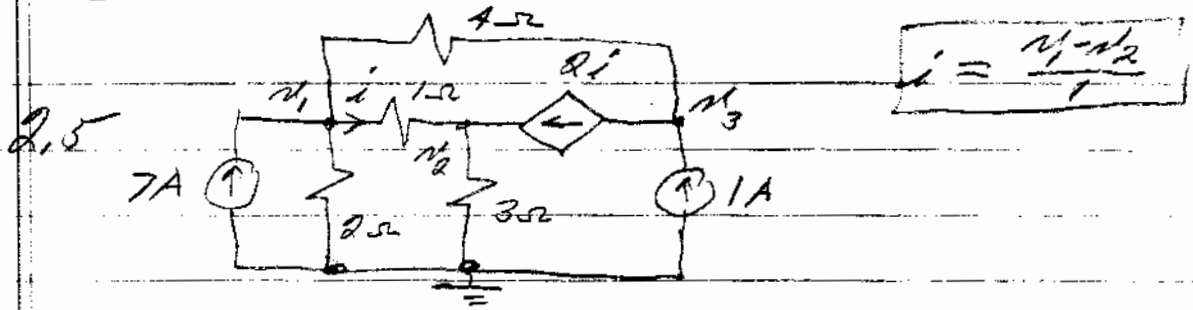
$$\left. \begin{aligned} (V_c - 1) + 2V_c &= 5 \\ (V_d - 1) + 3V_d &= -5 \end{aligned} \right\} \begin{aligned} 3V_c &= 6 \Rightarrow V_c = 2 \\ 4V_d &= -4 \Rightarrow V_d = -1 \end{aligned}$$

$$i_1 = 1 - V_c = -1 \text{ A}; \quad i_2 = 2V_c = 4; \quad i_3 = 3V_d = -3; \quad i_4 = 1 - V_d = +2$$

power balance

$$\begin{aligned} P_{1V} &= -(i_1 + i_4) \times 1 = -2 \text{ Watt} \\ P_{1\Omega} &= i_1^2 \times 1 = 4 \text{ W} \\ P_{1\Omega} &= i_2^2 = 1 \text{ W} \\ P_{2\Omega} &= \frac{i_2^2}{2} = 8 \text{ W} \\ P_{3\Omega} &= \frac{i_3^2}{3} = 3 \text{ W} \\ P_{5A} &= (V_d - V_c) \times 5 = -15 \text{ W} \end{aligned}$$

$$\Sigma = 0$$



$$\left. \begin{aligned} \frac{n_1}{2} + \frac{n_1 - n_3}{4} + \frac{n_1 - n_2}{1} &= 7 \\ \frac{n_2 - n_1}{1} + \frac{n_2}{3} - 2i &= 0 \\ \frac{n_3 - n_1}{4} + 2i &= 1 \end{aligned} \right\} \begin{aligned} \frac{7}{4}n_1 - n_2 - \frac{1}{4}n_3 &= 7 \\ -3n_1 + \frac{10}{3}n_2 &= 0 \\ \frac{7}{4}n_1 - 2n_2 + \frac{1}{4}n_3 &= 1 \end{aligned}$$

$$n_1 = \begin{vmatrix} 7 & -1 & -1/4 \\ 0 & 10/3 & 0 \\ 1 & -2 & 1/4 \end{vmatrix} = \frac{10/3 \left(\frac{7}{4} + \frac{1}{4} \right)}{-\frac{1}{4} \left(6 - \frac{70}{12} \right) + \frac{1}{4} \left(\frac{70}{12} - 3 \right)} = \frac{90}{3} = 30$$

$$n_1 = \frac{90}{3} \times \frac{1}{9} = 10 \text{ V}$$

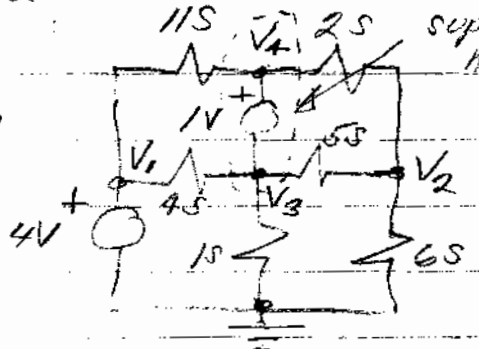
$$n_2 = \begin{vmatrix} \frac{7}{4} & 7 & -\frac{1}{4} \\ -3 & 0 & 0 \\ \frac{7}{4} & 1 & \frac{1}{4} \end{vmatrix} = \frac{3 \left(\frac{7}{4} + \frac{1}{4} \right)}{2/3} = \frac{6 \times 3}{2} = 9 \text{ V}$$

$$n_3 = \begin{vmatrix} \frac{7}{4} & -1 & 7 \\ -3 & \frac{10}{3} & 0 \\ \frac{7}{4} & -2 & 1 \end{vmatrix} = \frac{\frac{2}{12} \cdot \frac{34}{12}}{2/3} = \frac{24}{12} \times \frac{3}{4} = 6 \text{ V}$$

EE 211

Homework 7

2.10



$V_A - V_B = 1$; $V_1 = 4V$

$(V_A - 4)11 + (V_1 - V_2)2 + (V_3 - 4)1 + V_3 + (V_3 - V_2)5 = 0$
 $(V_2 - V_A)2 + (V_2 - V_3)5 + V_2 6 = 0$

or

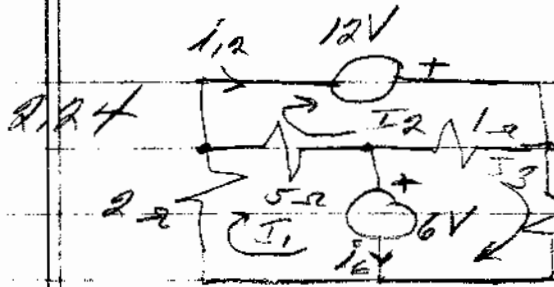
$-V_3 + V_4 = 1$
 $-7V_2 + 10V_3 + 13V_4 = 60$
 $13V_2 - 5V_3 - 2V_4 = 0$

$V_2 = \frac{\begin{vmatrix} 1 & -1 & 1 \\ 60 & 10 & 13 \\ 0 & -5 & -2 \end{vmatrix}}{\begin{vmatrix} 1 & -1 & 1 \\ -7 & 10 & 13 \\ 13 & -5 & -2 \end{vmatrix}} = \frac{45 - 420}{1(-20+65) - 60(2+6)} = \frac{15}{-375} = -0.04V$

$V_3 = \frac{\begin{vmatrix} 0 & -1 & 1 \\ -7 & 10 & 13 \\ 13 & -5 & -2 \end{vmatrix}}{\begin{vmatrix} 1 & -1 & 1 \\ -7 & 10 & 13 \\ 13 & -5 & -2 \end{vmatrix}} = \frac{1(14-169) + 1(35-130)}{-155 - 95} = \frac{-250}{-250} = 1V$

$V_4 = \frac{\begin{vmatrix} 0 & 1 & 1 \\ -7 & 60 & 13 \\ 13 & 0 & -2 \end{vmatrix}}{\begin{vmatrix} 1 & -1 & 1 \\ -7 & 10 & 13 \\ 13 & -5 & -2 \end{vmatrix}} = \frac{+155 - 790}{-250} = \frac{-635}{-250} = 2.54V$

$V_A = \frac{\begin{vmatrix} 0 & -1 & 1 \\ -7 & 10 & 60 \\ 13 & -5 & 0 \end{vmatrix}}{\begin{vmatrix} 1 & -1 & 1 \\ -7 & 10 & 13 \\ 13 & -5 & -2 \end{vmatrix}} = \frac{1(-780) + 1(35-130)}{-250} = \frac{-845}{-250} = 3.38V$



$$I_1 \cdot 2 + (I_1 - I_2) \cdot 5 = -6$$

$$(I_2 - I_1) \cdot 5 + (I_2 - I_3) \cdot 1 = 12$$

$$4I_3 + (I_3 - I_2) \cdot 1 = 6$$

or

$$7I_1 - 5I_2 = -6$$

$$-5I_1 + 6I_2 - I_3 = 12$$

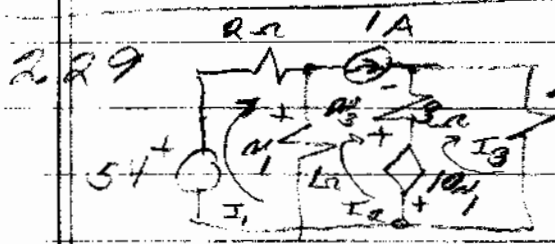
$$-I_2 + 5I_3 = 6$$

$$I_1 = \begin{vmatrix} -6 & -5 & 0 \\ 12 & 6 & -1 \\ 6 & -1 & 5 \end{vmatrix} = \frac{-6(29) + 5(66)}{78} = \frac{156}{78} = 2A$$

$$I_2 = \begin{vmatrix} 7 & -6 & 0 \\ -5 & 12 & -1 \\ 0 & 6 & 5 \end{vmatrix} = \frac{7(66) + 6(-25)}{78} = \frac{312}{78} = 4A$$

$$I_3 = \begin{vmatrix} 7 & -5 & -6 \\ -5 & 6 & 12 \\ 0 & -1 & 6 \end{vmatrix} = \frac{7(48) + 5(-36)}{78} = \frac{156}{78} = 2A$$

a) $I_1 = I_2 = 4A$ b) $I_6 = I_1 - I_3 = 0$



$$2I_1 + (I_1 - I_2) = 5 \Rightarrow I_2 = 1A$$

$$10I_1 + (I_3 - I_2) \cdot 3 + 4I_3 = 0$$

$$u_1 = (I_1 - I_2)$$

$$3I_1 = 6 \Rightarrow I_1 = 2A$$

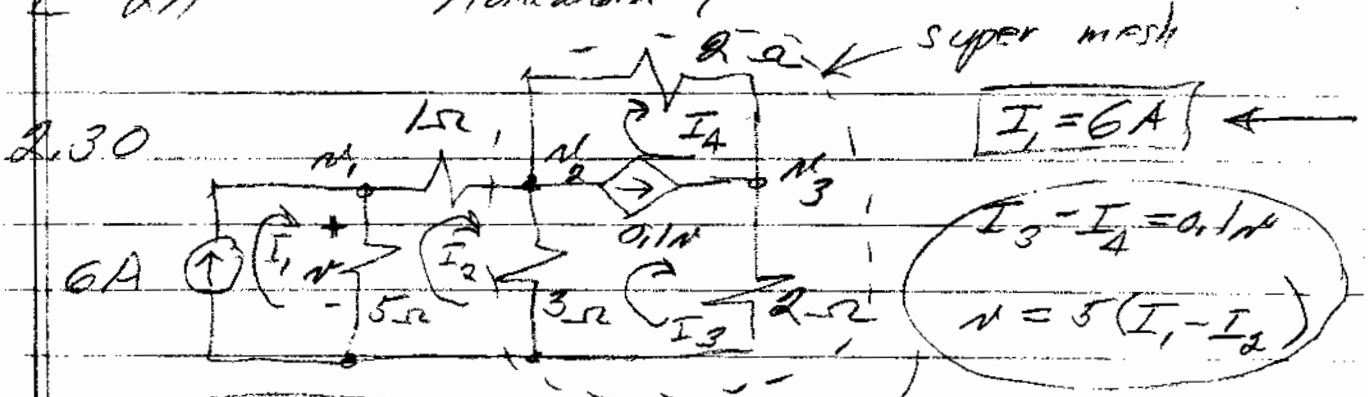
or

$$10(1) + (I_3 - 1) \cdot 3 + 4I_3 = 0 \Rightarrow 7I_3 = -7 \Rightarrow I_3 = -1A$$

$$u_1 = (I_1 - I_2) \cdot 1 = 1V$$

$$u_2 = 4I_3 = -4V$$

$$u_3 = (I_3 - I_2) \cdot 3 = -6V$$



I_2 mesh: $(I_2 - I_1)5 + I_2 + (I_2 - \frac{I_3}{3})3 = 0$ $-5I_1 + 9I_2 - 3I_3 = 0$
 Super mesh: $(I_3 - I_4)3 + 2I_4 + 2I_3 = 0$ $-3I_2 + 5I_3 + 2I_4 = 0$
 $I_1 - I_2 - 2I_3 + 2I_4 = 0$

$I_3 - I_4 = \frac{1}{2}(I_1 - I_2)$

$$\left. \begin{aligned} 9I_2 - 3I_3 &= 30 \\ -3I_2 + 5I_3 + 2I_4 &= 0 \\ -I_2 - 2I_3 + 2I_4 &= -6 \end{aligned} \right\}$$

$$I_2 = \frac{\begin{vmatrix} 30 & -3 & 0 \\ 0 & 5 & 2 \\ -6 & -2 & 2 \end{vmatrix}}{\begin{vmatrix} 9 & -3 & 0 \\ -3 & 5 & 2 \\ -1 & -2 & 2 \end{vmatrix}} = \frac{30(14) + 3(12)}{9(14) + 3(-4)} = \frac{456}{114} = 4A$$

$$I_3 = \frac{\begin{vmatrix} 9 & 30 & 0 \\ -3 & 0 & 2 \\ -1 & -6 & 2 \end{vmatrix}}{114} = \frac{9(12) - 30(-4)}{114} = \frac{228}{114} = 2A$$

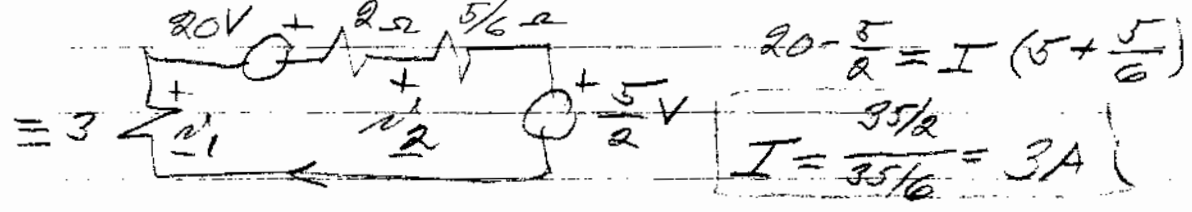
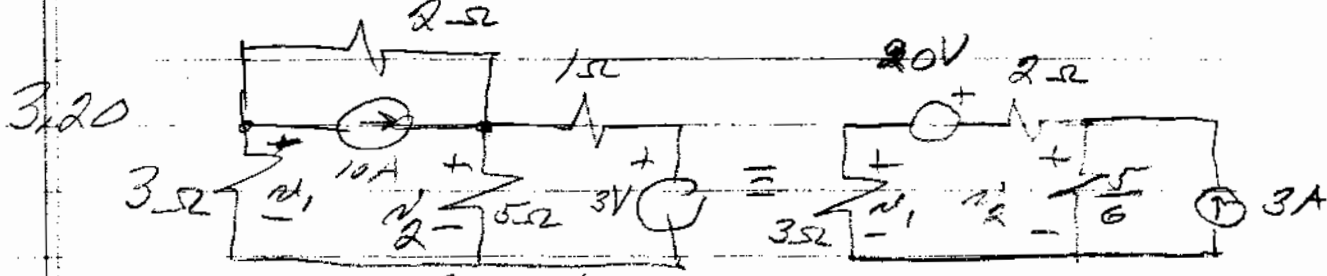
$$I_4 = \frac{\begin{vmatrix} 9 & -3 & 30 \\ -3 & 5 & 0 \\ -1 & -2 & -6 \end{vmatrix}}{114} = \frac{3(78) + 5(-24)}{114} = \frac{144}{114} = 1A$$

$$V_1 = (I_1 - I_2)5 = 10V$$

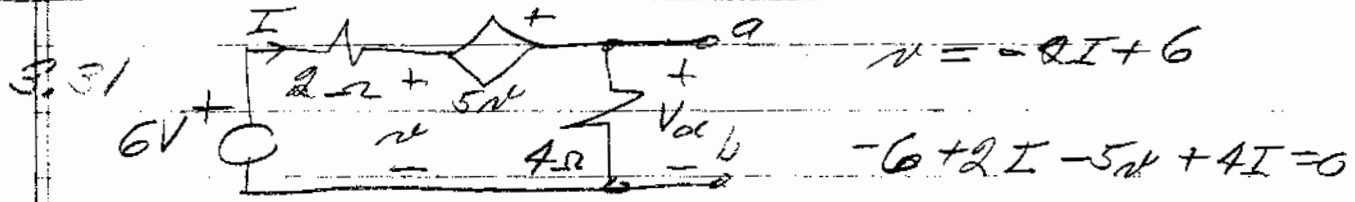
$$V_2 = (I_2 - I_3)3 = 6V$$

$$V_3 = 2I_3 = 4V$$

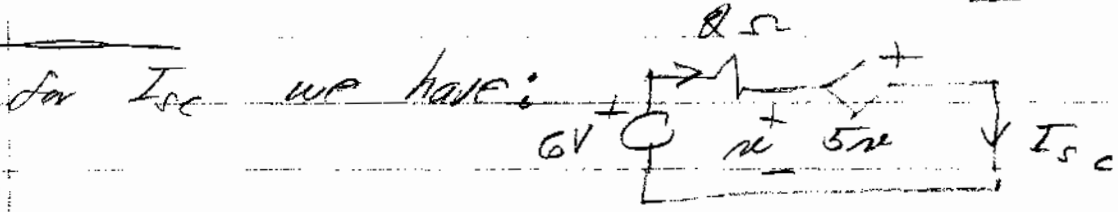
EE 211 Homework 10



$v_1 = -3 \times 3 = -9V$; $v_2 = \frac{5}{6}I + \frac{5}{2} = 5V$



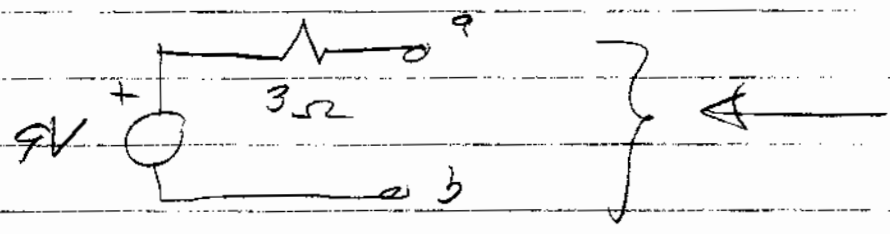
or $16I = 36$; $I = \frac{36}{16} = \frac{9}{4}$ and $V_{oc} = V_{th} = 9V$



$v = -I_{sc} \cdot 2 + 6$; $-6 + 2 \frac{v}{5} - 5(-2I_{sc} + 6) = 0$

or $18I_{sc} = 36$; $I_{sc} = 3A$

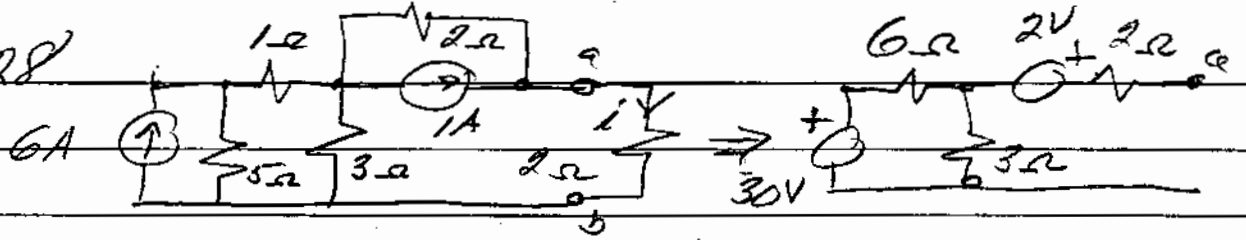
$R_{th} = \frac{V_{oc}}{I_{sc}} = \frac{9}{3} = 3\Omega$



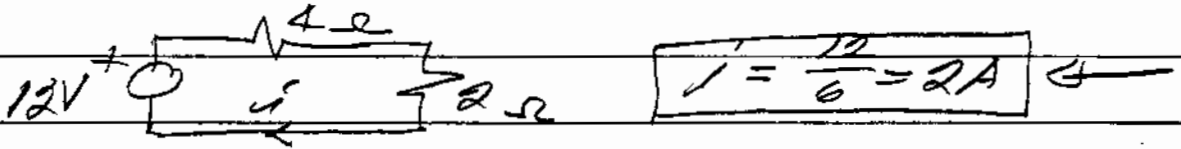
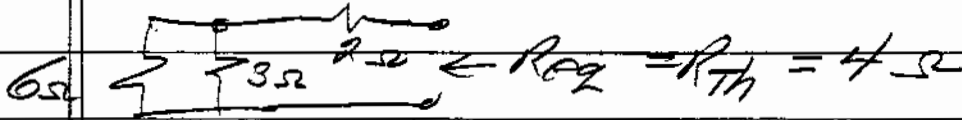
EE 211

Homework 11

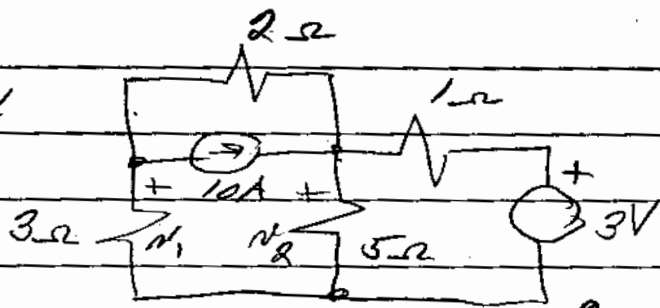
3.28



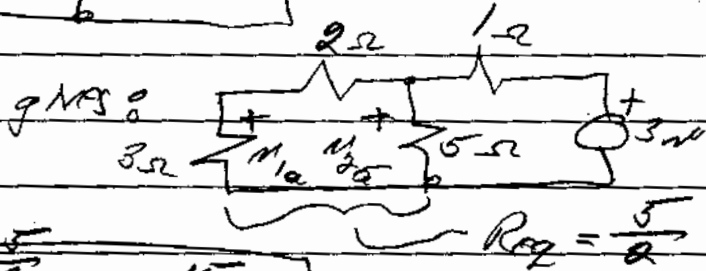
$$V_{TH} = V_{OC} = \frac{3}{9} \times 30 + 2 = 12V$$



3.64



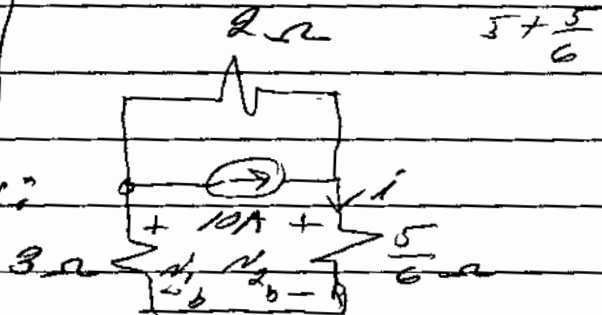
current source = 0



$$V_{n2} = 3 \times \frac{2}{\frac{2}{1} + 5} = \frac{15}{7} \text{ V}$$

$$V_{n1} = 10 \times \frac{3}{5} = \frac{9}{7} \text{ V}$$

voltage source = 0



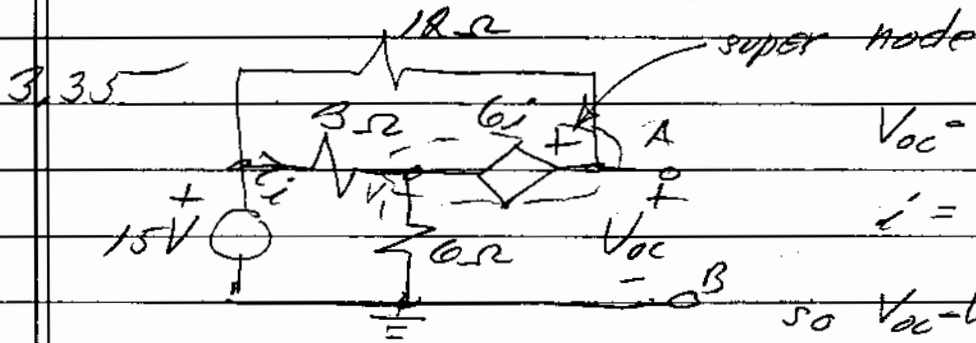
using current division $i = 10 \times \frac{2}{3 + \frac{5 \times 2}{5+2}} = \frac{20 \times 6}{35} = \frac{24}{7}$

$$V_{n2} = i \times \frac{5}{6} = \frac{24}{7} \times \frac{5}{6} = \frac{20}{7}$$

$$V_{n1} = -i \times 3 = -\frac{72}{7}$$

$$V_{n2 \text{ total}} = \frac{15}{7} + \frac{20}{7} = \frac{35}{7} = 5 \text{ V}$$

$$V_{n1 \text{ total}} = \frac{9}{7} - \frac{72}{7} = -\frac{63}{7} = -9 \text{ V}$$



$$V_{oc} = V_1 = 6i_1$$

$$i_1 = \frac{15 - V_1}{3} = 5 - \frac{V_1}{3}$$

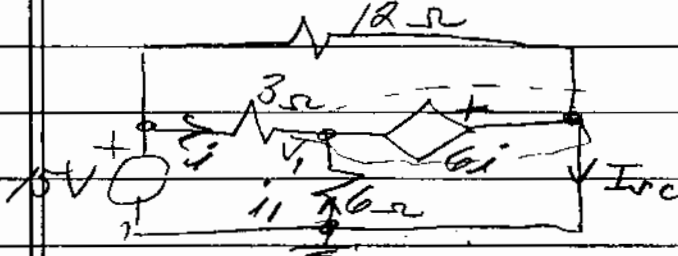
$$\text{so } V_{oc} - V_1 = 30 - 2V_1$$

$$\text{or } \boxed{V_{oc} + V_1 = 30}$$

$$\frac{V_1 - 15}{3} + \frac{V_1}{6} + \frac{V_{oc} - 15}{12} = 0 \Rightarrow \boxed{\frac{1}{12}V_{oc} + \frac{1}{2}V_1 = \frac{25}{4}}$$

$$V_{oc} = \frac{\begin{vmatrix} 30 & 1 \\ 25 & \frac{1}{2} \end{vmatrix}}{\begin{vmatrix} \frac{1}{12} & \frac{1}{2} \\ \frac{1}{2} & \frac{1}{12} \end{vmatrix}} = \frac{15 - \frac{25}{4}}{\frac{1}{2} - \frac{1}{12}} = \frac{\frac{35}{4}}{\frac{5}{12}} = \frac{35 \times 12}{4 \times 5} = \boxed{21V}$$

Finding I_{sc}



$$i_1 = \frac{15 - V_1}{3}$$

$$\therefore 6i_1 = 30 - 2V_1$$

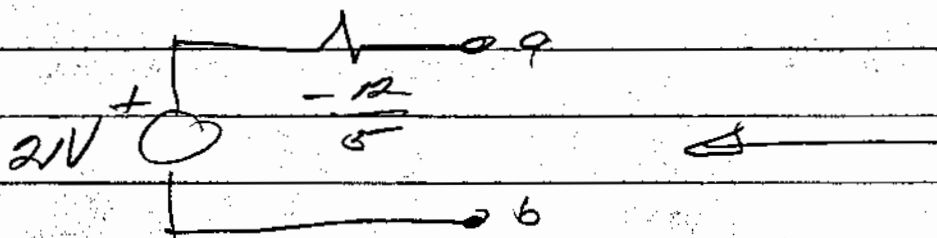
$$i_1 = \frac{6i_1}{6} = 5 - \frac{1}{3}V_1 = -\frac{V_1}{6}$$

$$5 = \frac{1}{6}V_1 \text{ or } \boxed{V_1 = 30V}$$

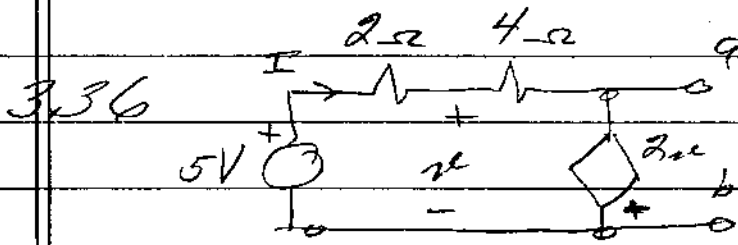
$$\frac{V_1 - 15}{3} + \frac{V_1}{6} + \frac{0 - 15}{12} + I_{sc} = 0$$

$$\text{or } \frac{15 + 5 - 5}{3} = -I_{sc} \Rightarrow \boxed{I_{sc} = -\frac{35}{12} A}$$

$$\therefore R_{Th} = \frac{-21 \times 4}{-35} = \frac{12}{5} \Omega$$



EE 211 Homework 14



$$6I - 2v = 5$$

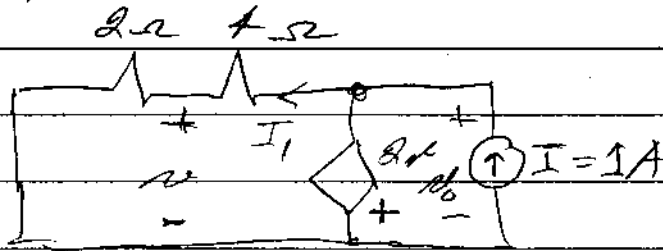
$$\text{but } v = -2I + 5$$

$$\therefore 6I + 4I - 10 = 5$$

$$10I = 15$$

→ so $I = \frac{3}{2}$; $v = -3 + 5$; $V_{oc} = V_{Th} = -2v = -4$

Using hint our circuit is



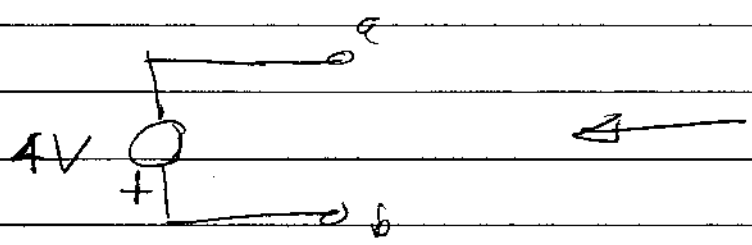
$$I_1 = -\frac{2v}{6}$$

$$\text{but } v = 2I_1$$

$$\therefore I_1 = -\frac{2}{3}I_1$$

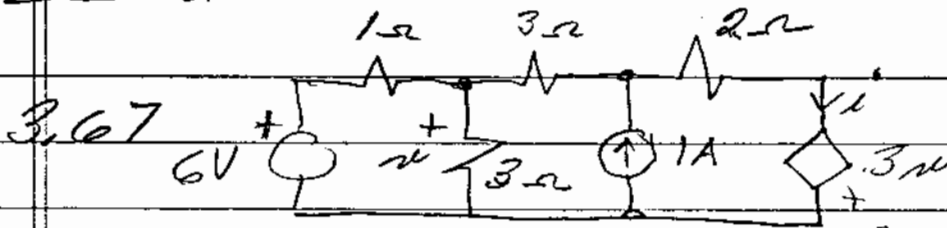
→ so $I_1 = 0$; $v = 0$

∴ $N_0 = 0$ and $R_{Th} = \frac{N_0}{I} = 0$

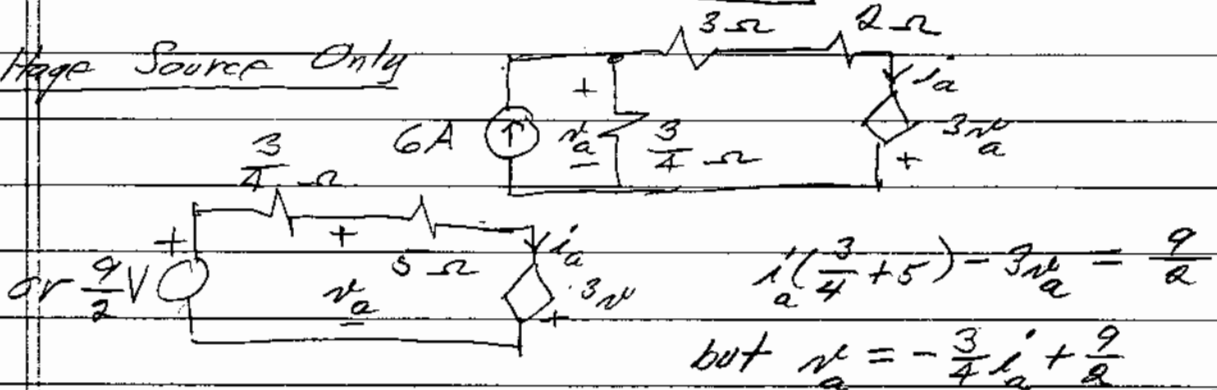


EE 211

Homework 15



Voltage Source Only

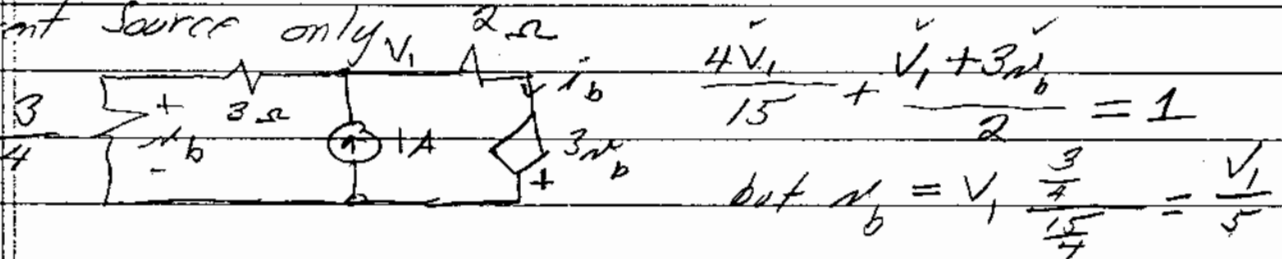


$$\text{or } \frac{9}{2} \text{ V} \quad \text{but } n_a = -\frac{3}{4}i_a + \frac{9}{2}$$

$$\text{so } i_a \left(\frac{3}{4} + 5 \right) + \frac{9}{4} = \frac{27}{2} + \frac{9}{2}; \quad 8i_a = 18; \quad \boxed{i_a = \frac{9}{4}}$$

$$\text{and } n_a = -\frac{3}{4} \left(\frac{9}{4} \right) + \frac{9}{2} = \frac{72 - 27}{16} = \frac{45}{16}$$

Current Source only



$$\frac{4V_1}{15} + \frac{V_1 + 3n_b}{2} = 1$$

$$\text{but } n_b = V_1 \frac{3}{15} = \frac{V_1}{5}$$

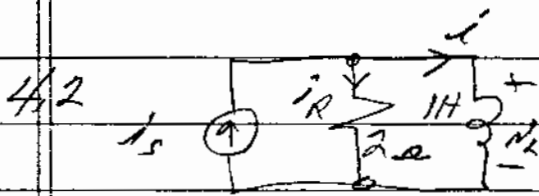
$$\text{so } V_1 \left(\frac{4}{15} + \frac{1}{2} + \frac{3}{10} \right) = 1 = V_1 \left(\frac{8+15+9}{30} \right) = 1 = \frac{16}{15} V_1$$

$$\text{so } \boxed{V_1 = \frac{15}{16}}; \quad \boxed{n_b = \frac{V_1}{5} = \frac{3}{16}}$$

$$i_b = \frac{V_1 + 3n_b}{2} = \frac{V_1 + \frac{3}{5}V_1}{2} = \frac{4V_1}{5} = \frac{4 \cdot \frac{15}{16}}{5} = \frac{3}{4} \text{ A}$$

$$\text{so } i = i_a + i_b = \frac{9}{4} + \frac{3}{4} = 3 \text{ A}$$

$$n = n_a + n_b = \frac{45}{16} + \frac{3}{16} = 3 \text{ V}$$



$i(t) = 0$ for $t < 0$

$i(t) = 1 - e^{-2t}$ for $t \geq 0$

$v_L(t) = L \frac{di}{dt}$

a) $v_L(t) = 0$ for $t < 0$

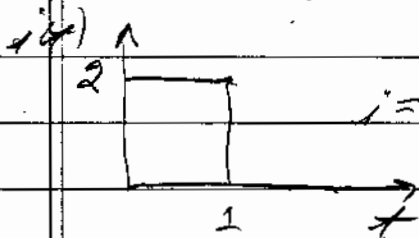
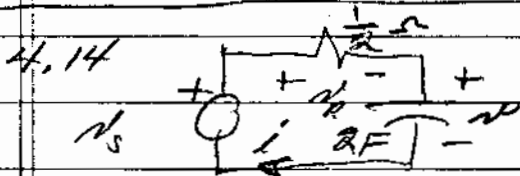
$v_L(t) = 2e^{-2t}$ for $t \geq 0$

b) $i_R(t) = 0$ for $t < 0$

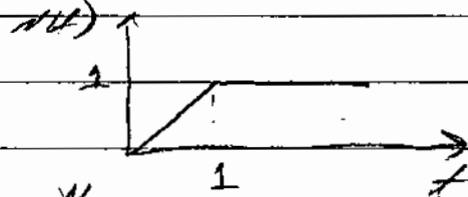
$i_R(t) = \frac{v_L(t)}{R} = e^{-2t}$ for $t \geq 0$

c) $i(t) = 0$ for $t < 0$

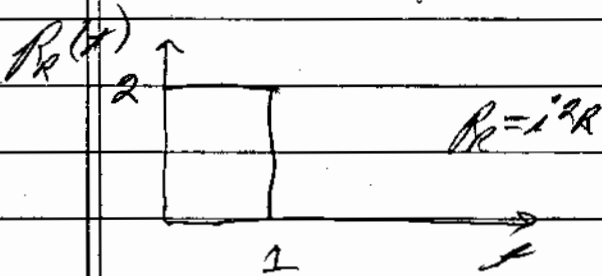
$i(t) = i + i_R = 1 - e^{-2t} + e^{-2t} = 1A$ for $t \geq 0$



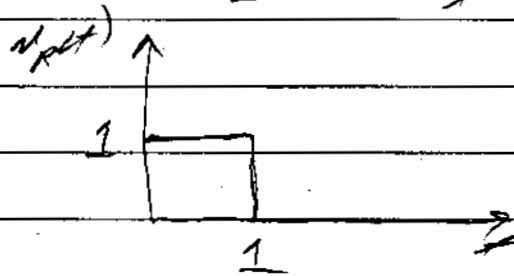
$i = C \frac{dv_C}{dt}$



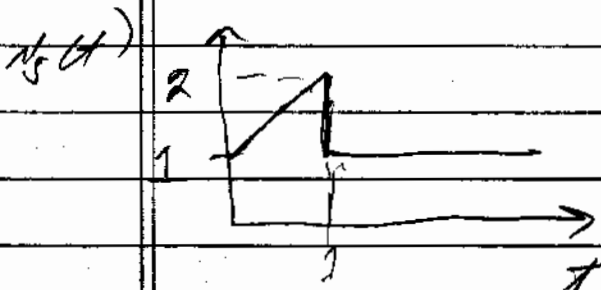
$v_C = \frac{1}{C} \int i dt$



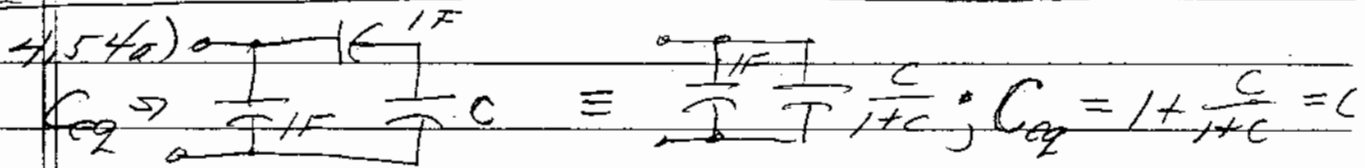
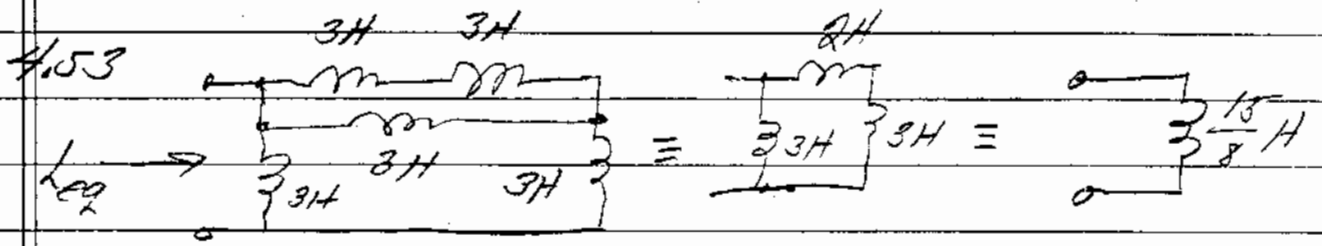
$P_R = i^2 R$



$P_C(t) = i v_C$

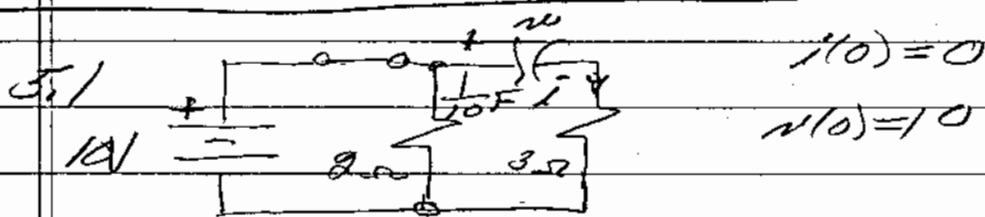


$P_S(t) = P_R(t) + P_C(t)$



so $1+C+C = C(C+1)$; $C^2 - C - 1 = 0$

$$C = \frac{1 \pm \sqrt{1+4}}{2} = \frac{1 \pm \sqrt{5}}{2} = 1.618 F$$



for $t > 0$ $5i + 10 \int_0^t i dt + 10 = 0$

so $5 \frac{di}{dt} + 10i = 0$; $i = A e^{st}$

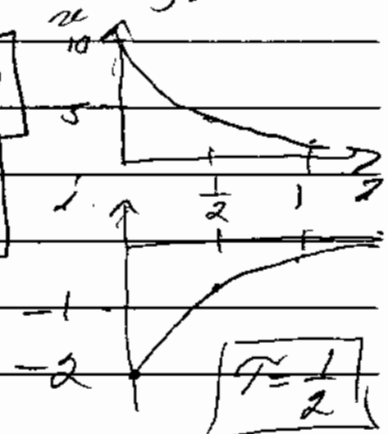
$5sA e^{st} + 10A e^{st} = 0$; $5s = -10$ or $s = -2$

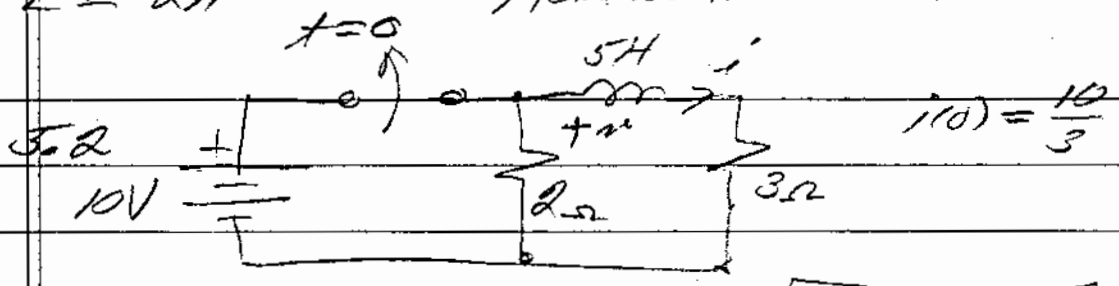
and $i = A e^{-2t}$

from (1) evaluated @ $t=0$; $5i(0) + 10 = 0$; $i(0) = -2$

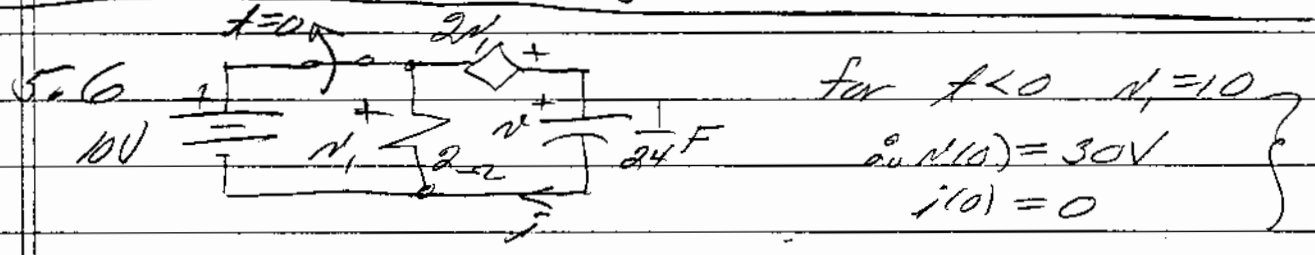
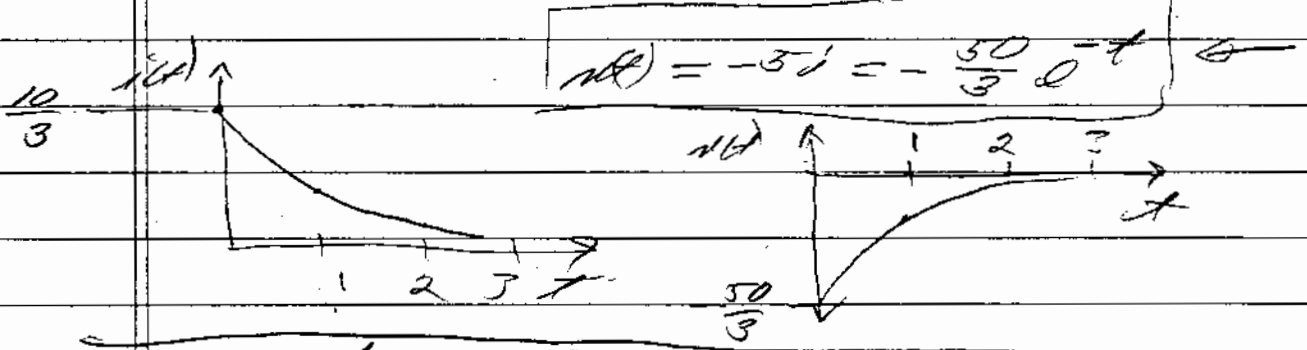
so $i = -2 e^{-2t}$ for $t > 0$

$v = -5i = 10 e^{-2t}$ for $t > 0$





for $t > 0$ $5i + 5 \frac{di}{dt} = 0$; $i = \frac{10}{3} e^{-t}$



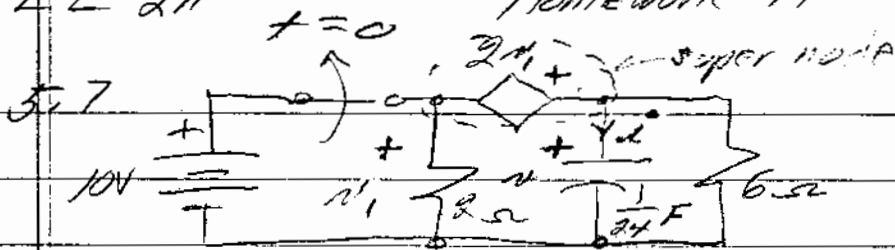
for $t > 0$ $2i - 2v_1 + 24 \int_0^t i dt + 30 = 0$; but $v_1 = -2i$

so $6i + 24 \int_0^t i dt + 30 = 0$ or $6 \frac{di}{dt} + 24i = 0$

$i = A e^{-4t}$

but from above $6i(0) = -30$ or $i(0) = -5$

so $i = -5 e^{-4t}$ for $t > 0$
 $v = 3v_1 = -6i = 30 e^{-4t}$



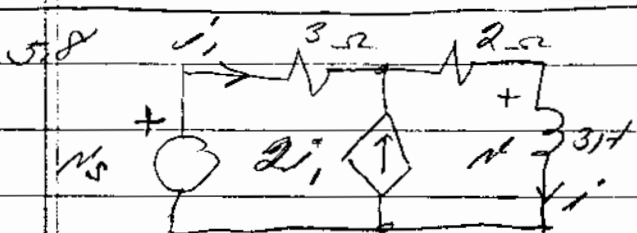
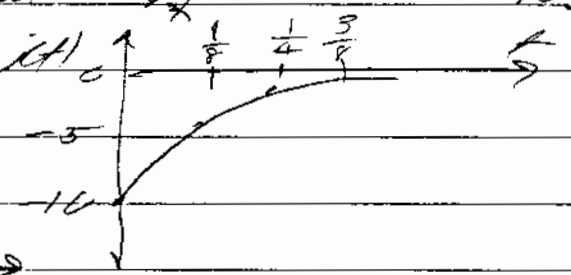
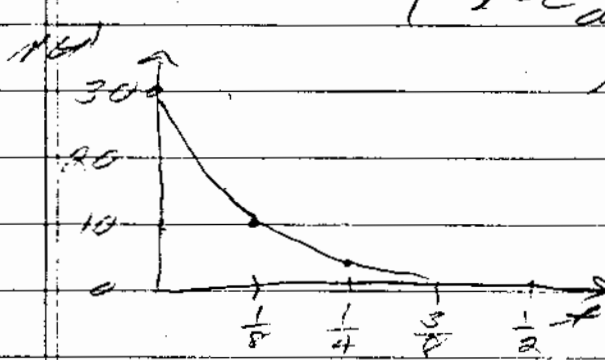
$v(0) = 30V$
 $i = 3i_1$
 $50 \mu A(0) = 10V$

$\frac{v_1}{2} + \frac{3i_1}{6} + \frac{1}{24} \frac{d(3v_1)}{dt} = 0$; $v_1 + \frac{1}{8} \frac{dv_1}{dt} = 0$

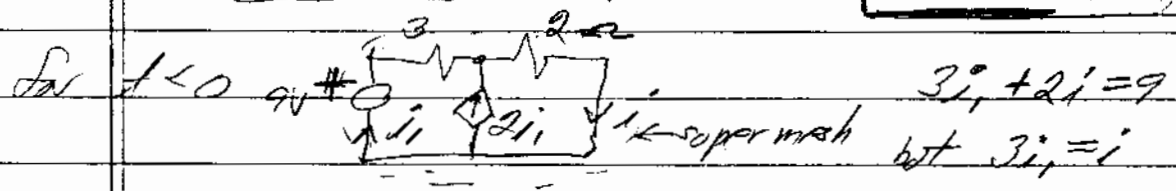
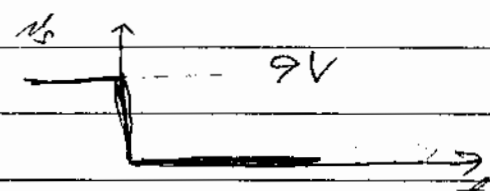
$v_1 = A e^{-8t}$ or $v_1 = 10 e^{-8t}$

∴ for $t > 0$ } $v = 3v_1 = 30 e^{-8t}$

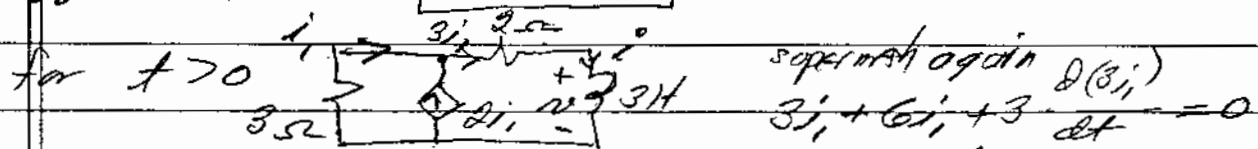
$i = C \frac{dv}{dt} = \frac{1}{24} \times 30 \times (-8) e^{-8t} = -10 e^{-8t}$



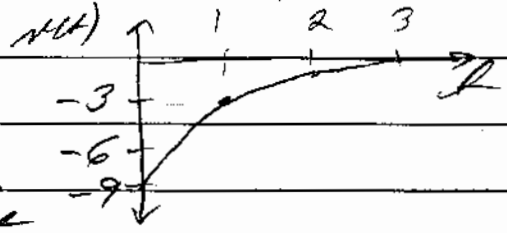
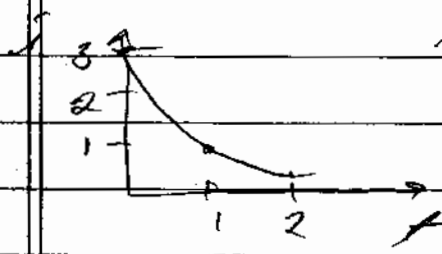
$v_s(t) = 9 [1 - u(t)]$

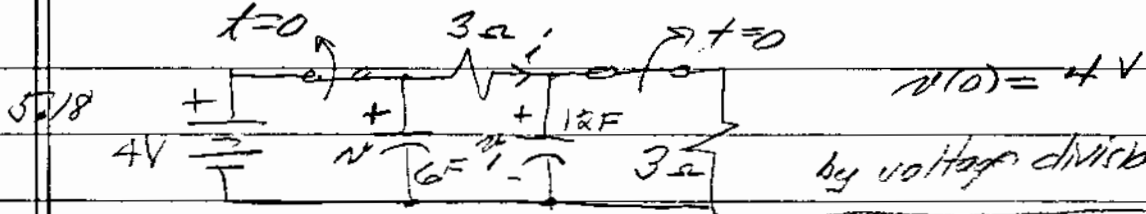


∴ $3i_1 = 9$ or $i_1(0) = 3$



$i_1 = A e^{-t}$ but $i = 3i_1$, so $i = 3 e^{-t}$; $v = 3 \frac{di}{dt} = -9 e^{-t}$





by voltage division $v_1(t) = 2$

for $t > 0$

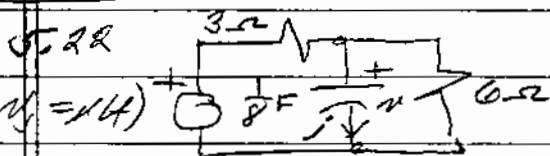
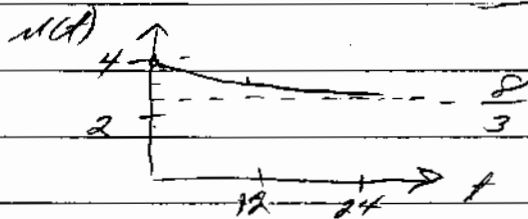
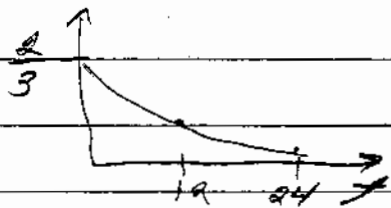
$$3i + \frac{1}{6} \int_0^t i dt - 4 + \frac{1}{12} \int_0^t i dt + 2 = 0$$

$$\Rightarrow \left[3 \frac{di}{dt} + \left(\frac{1}{6} + \frac{1}{12} \right) i = 0 \right] \Rightarrow \left[\frac{di}{dt} + \frac{1}{12} i = 0 \right]$$

so $i = A e^{-\frac{t}{12}}$ and from integral equation $i(0) = \frac{2}{3}$

$$\rightarrow i = \frac{2}{3} e^{-\frac{t}{12}} \quad \text{and} \quad v = -\frac{1}{6} \int_0^t \frac{2}{3} e^{-\frac{t}{12}} dt + 4$$

$$v = -\frac{2}{3 \times 6} \times (-12) e^{-\frac{t}{12}} + 4 = \frac{4}{3} e^{-\frac{t}{12}} - \frac{4}{3} + 4 = \frac{4}{3} e^{-\frac{t}{12}} + \frac{8}{3}$$



zero state (i.e. $v(0) = 0$)

for $t > 0$

$$\frac{v-1}{3} + \frac{v}{6} + \frac{1}{8} \frac{dv}{dt} = 0 \Rightarrow \frac{1}{8} \frac{dv}{dt} + \frac{1}{2} v = \frac{1}{3}$$

so $v_h = A e^{-4t}$; $v_p = K = \frac{2}{3}$

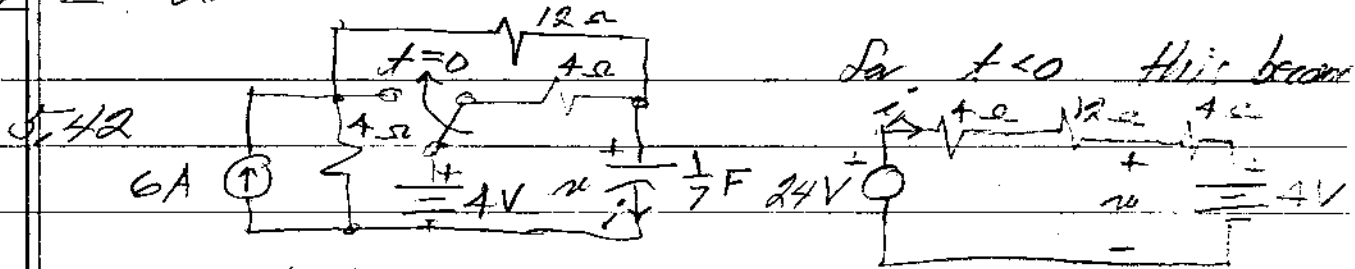
$v = v_h + v_p = A e^{-4t} + \frac{2}{3}$ but $v(0) = 0$

$$\therefore v(t) = \frac{2}{3} (1 - e^{-4t})$$

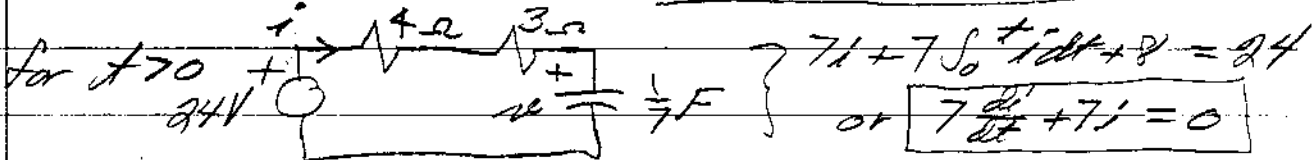
$$i(t) = \frac{1}{8} \frac{dv}{dt} = \frac{1}{8} (4) e^{-4t} \left(\frac{2}{3} \right) = \frac{1}{3} e^{-4t}$$

FE 211

Homework 21



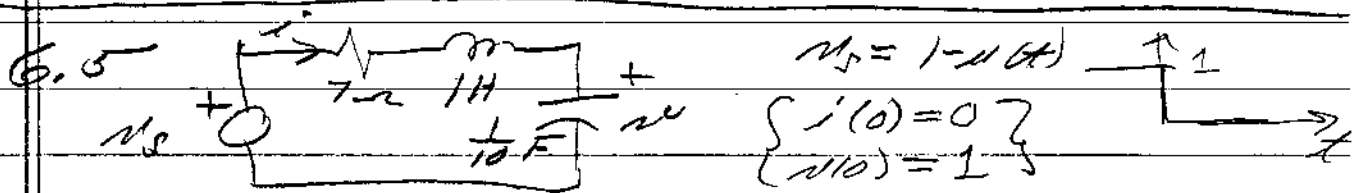
so $i_1 = \frac{24}{40} = 1 \text{ A}$ and $v(0) = 4i_1 + 4 = 8 \text{ V}$ ←



$7i + 7 \int_0^t i dt + 8 = 24$
or $7 \frac{di}{dt} + 7i = 0$

$i = A e^{-t}$ from initial equation $i(0) = \frac{16}{7}$

∴ $i(t) = \frac{16}{7} e^{-t}$ for $t > 0$ ←
 $v(t) = 24 - 7i = 24 - 16e^{-t}$



for $t > 0$ $7i + \frac{di}{dt} + 10 \int_0^t i dt + 1 = 0$ or $\frac{di}{dt} + 7 \frac{dv}{dt} + 10i = 0$

$s_{1,2} = \frac{-7 \pm \sqrt{49 - 40}}{2} = -\frac{7}{2} \pm \frac{3}{2} = -2, -5$

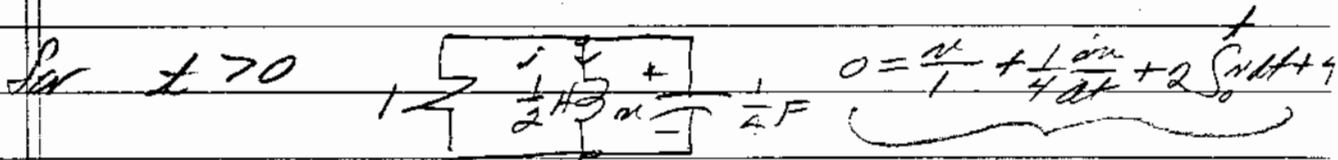
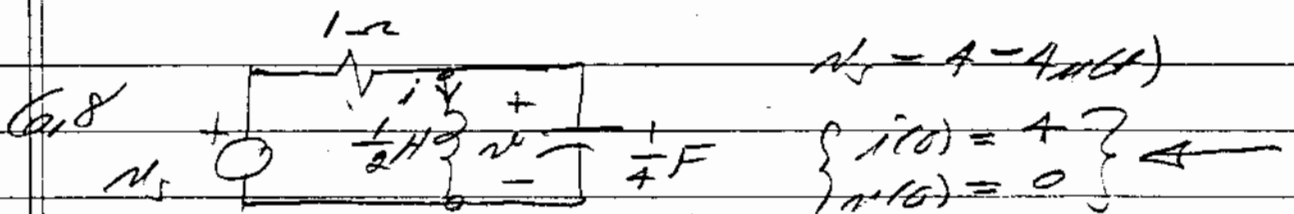
so $i(t) = A_1 e^{-2t} + A_2 e^{-5t}$ but $i(0) = 0$ so $A_2 = -A_1$

$\left. \frac{di}{dt} \right|_{t=0} = -1 = -2A_1 - 5A_2 = -2A_1 + 5A_1$; $A_1 = -\frac{1}{3}$

and $i(t) = \frac{1}{3} e^{-5t} - \frac{1}{3} e^{-2t}$ ←

$v(t) = -7i - \frac{di}{dt} = -\frac{7}{3} e^{-5t} + \frac{7}{3} e^{-2t} + \frac{5}{3} e^{-5t} - \frac{2}{3} e^{-2t}$

$v(t) = \frac{5}{3} e^{-5t} - \frac{2}{3} e^{-2t}$ ←



$$\text{or } \frac{d^2 v}{dt^2} + 4 \frac{dv}{dt} + 8v = 0 \quad ; \quad s^2 + 4s + 8 = 0$$

$$s_{1,2} = \frac{-4 \pm \sqrt{16 - 32}}{2} = \boxed{-2 \pm j2}$$

$$v = A_1 e^{-2t} \cos 2t + A_2 e^{-2t} \sin 2t$$

but $v(0) = 0$ so $A_1 = 0$

$$\rightarrow \left. \frac{dv}{dt} \right|_{t=0} = -16 = A_2 \left[2e^{-2t} \cos 2t - 2e^{-2t} \sin 2t \right]_{t=0}$$

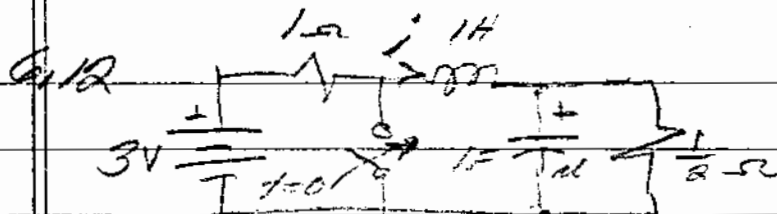
$$\therefore A_2 = -8$$

and $v = \boxed{-8 e^{-2t} \sin 2t}$ for $t > 0$

$$i = -\frac{v}{R} - C \frac{dv}{dt} = 8 e^{-2t} \sin 2t - \frac{1}{4} \left[16 e^{-2t} \sin 2t - 8 \times 2 e^{-2t} \cos 2t \right]$$

$$i(t) = \boxed{4 e^{-2t} \sin 2t + 4 e^{-2t} \cos 2t}$$

9



$$v(0) = 1V$$

$$i(0) = \frac{3}{2} = 1.5A$$

For $t < 0$

$$2v + \frac{di}{dt} + \int_0^t v dt - 2 = 0$$

$$or \frac{dv}{dt} + 2\frac{di}{dt} + v = 0$$

$$v = A_1 e^{st}; s^2 + 2s + 1 = 0 \quad \therefore s_{1,2} = \frac{-2 \pm \sqrt{4-4}}{2} = -1$$

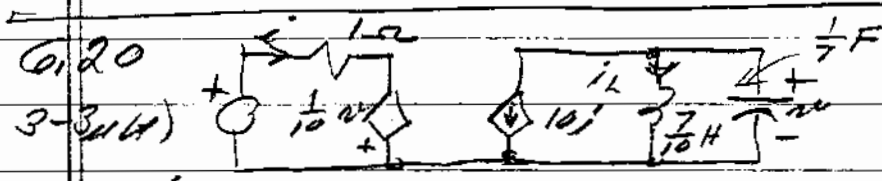
$$v = A_1 e^{-t} + A_2 t e^{-t} \quad \text{but } v(0) = 1 \quad \text{so } A_1 = 1$$

from (1) above $\frac{dv}{dt} = 0 \bigg|_{t=0} = -e^{-t} + A_2 e^{-t} - A_2 t e^{-t} \bigg|_{t=0}$

$$0 = -1 + A_2; A_2 = 1 \quad \text{and } v = e^{-t} + t e^{-t}$$

$$i = 2v + \frac{dv}{dt} = 2e^{-t} + 2t e^{-t} - e^{-t} - t e^{-t} + e^{-t} = 2e^{-t} + t e^{-t}$$

10



For $t < 0$ $v = 0$

$$i_L = -10i \quad \text{but } i = 3$$

For $t > 0$

$$v + \frac{1}{10} \frac{dv}{dt} + \frac{10}{7} \int_0^t v dt - 30 = 0$$

$$\left. \begin{matrix} i = \frac{1}{10} v \\ \therefore 10i = v \end{matrix} \right\} \text{ so } i_L(0) = -30$$

$$KCL: v + \frac{1}{10} \frac{dv}{dt} + \frac{10}{7} \int_0^t v dt - 30 = 0 \quad \therefore \frac{dv}{dt} = 210V$$

$$\frac{dv}{dt^2} + 7 \frac{dv}{dt} + 10v = 0 \quad \therefore s_{1,2} = \frac{-7 \pm \sqrt{49-40}}{2} = -\frac{7}{2} \pm \frac{3}{2} = -2, -5$$

$$v(t) = A_1 e^{-2t} + A_2 e^{-5t} \quad \text{but } v(0) = 0 \quad \text{so } A_2 = -A_1$$

$$\frac{dv}{dt} \bigg|_{t=0} = -2A_1 - 5A_2 = 210 \quad \text{so } -2A_1 + 5A_1 = 210; A_1 = 70$$

$$v(t) = 70 e^{-2t} - 70 e^{-5t}$$

EE 211

Homework 24

$$2.17 \quad a) \frac{-j6}{1+j} = \frac{6 e^{-j90^\circ}}{\sqrt{2} e^{j45^\circ}} = 3\sqrt{2} e^{-j135^\circ}$$

$$b) \frac{-8}{2+j3} = \frac{8 e^{j180^\circ}}{3.606 e^{j56.31^\circ}} = 2.22 e^{j123.7^\circ}$$

$$c) \frac{j^3}{-2+j} = \frac{3 e^{j90^\circ}}{2.236 e^{j153.43^\circ}} = 1.34 e^{-j63.43^\circ}$$

$$d) \frac{85}{-1-j4} = \frac{85}{4.123 e^{j55.9^\circ}} = 20.62 e^{-j205.9^\circ}$$

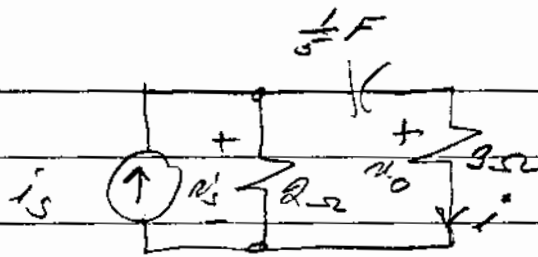
$$e) \frac{200(1-j)}{4+j3} = \frac{200\sqrt{2} e^{-j45^\circ}}{5 e^{j36.87^\circ}} = 40\sqrt{2} e^{-j81.87^\circ}$$

$$f) \frac{80(1+j) e^{j30^\circ}}{4+j3} = \frac{20\sqrt{2} e^{j45^\circ} e^{j30^\circ}}{5 e^{j36.87^\circ}} = 4\sqrt{2} e^{-j21.87^\circ}$$

$$g) 37.1 e^{j14^\circ} + 20.6 e^{j166^\circ} \\ = 35.998 + j8.975 = 19.988 - j4.984 = 16.01 + j3.99 \\ = 16.5 e^{j13.99^\circ}$$

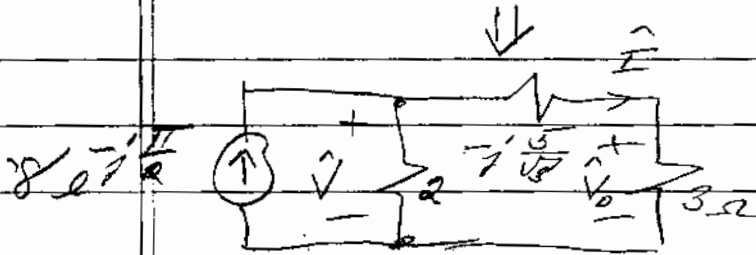
$$h) 16.5 e^{j14^\circ} + 4.12 e^{-j76^\circ} \\ = 16 + j3.99 + 0.997 - j3.998 = 17.01 e^{j0^\circ}$$

8.21



$$i_s(t) = 8 \sin \sqrt{3}t$$

$$= 8 \cos(\sqrt{3}t - \frac{\pi}{2})$$



$$\hat{I} = 8 e^{-j\frac{\pi}{2}} \frac{2}{5 - j\sqrt{3}}$$

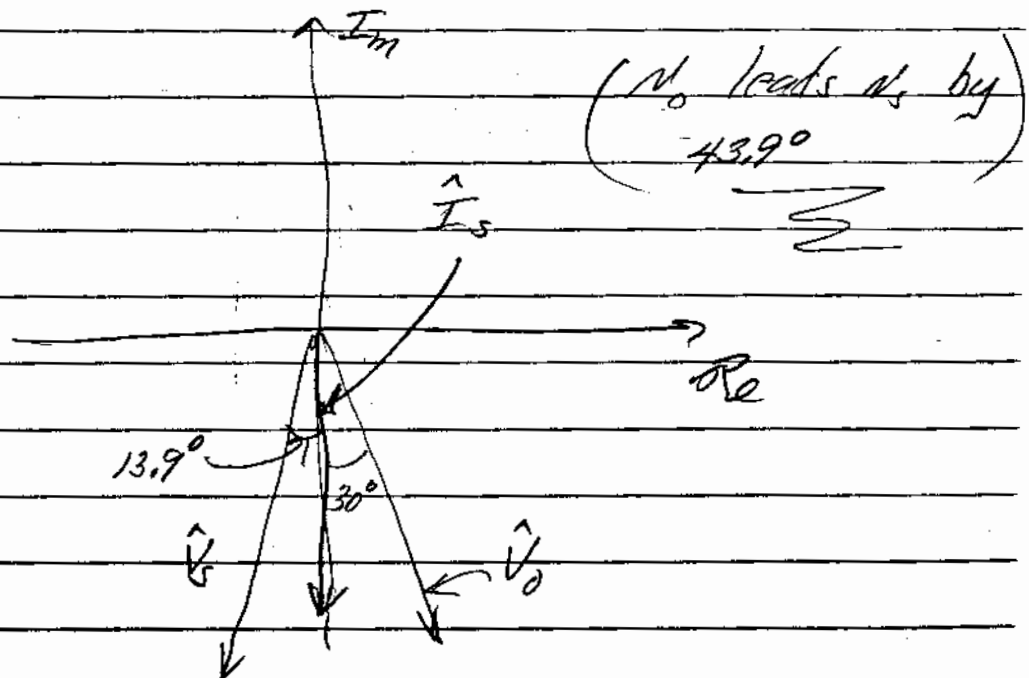
$$\hat{V}_0 - 3\hat{I} = \frac{48 e^{-j\frac{\pi}{2}}}{5 - j\sqrt{3}}$$

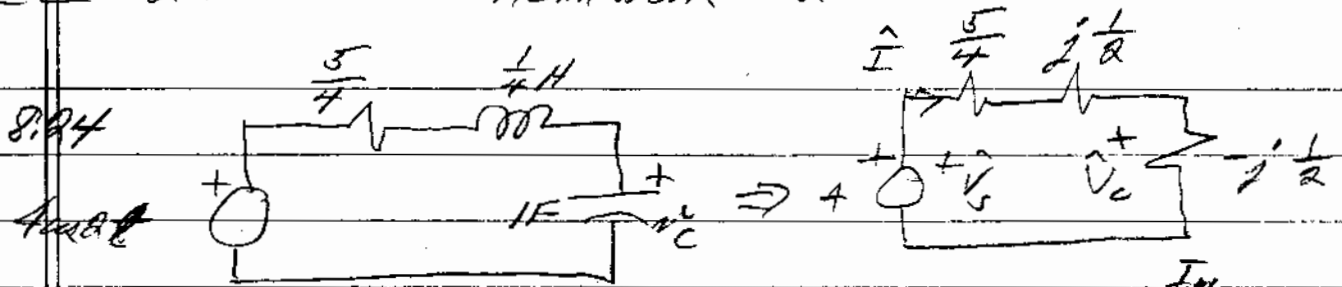
$$\text{so } \hat{V}_0 = \frac{48 e^{-j90^\circ}}{5.77 e^{-j30^\circ}} = 8.32 e^{-j60^\circ}$$

$$v_0(t) = \text{Re}\{\hat{V}_0 e^{j\sqrt{3}t}\} = 8.32 \cos(\sqrt{3}t - 60^\circ)$$

$$\hat{V}_0 = \hat{I} (3 - j\frac{5}{\sqrt{3}}) = \frac{16 e^{-j90^\circ} \cdot 4.16 e^{-j43.9^\circ}}{5.77 e^{-j30^\circ}} = 11.53 e^{-j103.9^\circ}$$

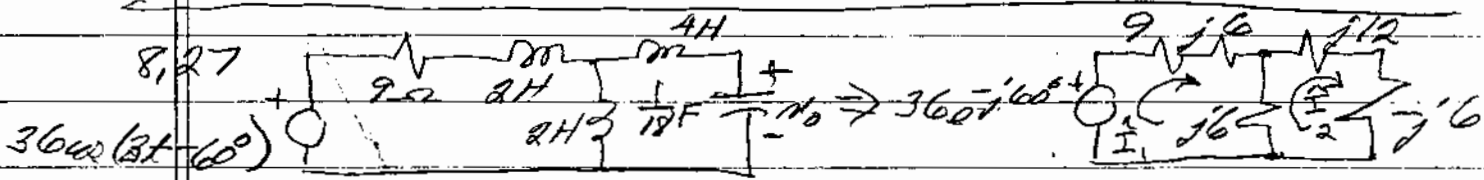
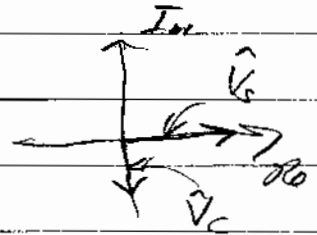
$$\text{or } v_0(t) = 11.53 \cos(\sqrt{3}t - 103.9^\circ)$$





$$\hat{I} = \frac{4}{5/4} = \frac{16}{5} \quad ; \quad \hat{V}_c = (-j1/2) \hat{I} = -j8/5$$

$$\therefore v_c(t) = \frac{8}{5} \cos(2t - 90^\circ) \leftarrow$$



$$360 e^{j60^\circ} = \hat{I}_1 (9 + j6) + (\hat{I}_1 - \hat{I}_2) j6 \quad (1)$$

$$0 = (\hat{I}_2 - \hat{I}_1) j6 + \hat{I}_2 j6 \Rightarrow \hat{I}_2 j12 = \hat{I}_1 j6 \quad \text{or} \quad \boxed{\hat{I}_1 = 2\hat{I}_2} \quad (2)$$

substituting (2) into (1) gives:

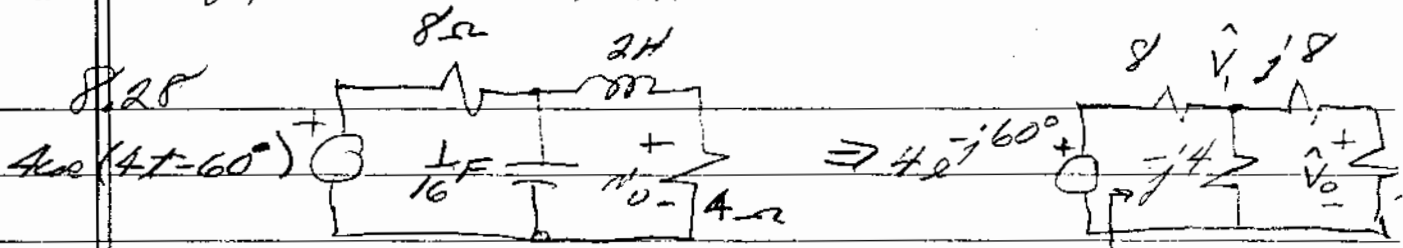
$$360 e^{j60^\circ} = 2\hat{I}_2 (9 + j6) + \hat{I}_2 j6 = \hat{I}_2 (18 + j18)$$

$$\text{so } \hat{I}_2 = \frac{360 e^{j60^\circ}}{\sqrt{2} 18 e^{j45^\circ}} = \sqrt{2} e^{-j15^\circ}$$

$$\text{and } \hat{V}_0 = -j6 \hat{I}_2 = 6\sqrt{2} e^{-j195^\circ}$$

$$\boxed{\text{or } v_0(t) = 6\sqrt{2} \cos(3t - 195^\circ)} \leftarrow$$

$$Z_{eq} \text{ seen by source} = 9 + j6 + \frac{j6(j6)}{j12} = \boxed{9 + j9} \leftarrow$$



$$\frac{\hat{V}_1 - 4e^{-j60^\circ}}{8} + \frac{\hat{V}_1}{-j4} + \frac{\hat{V}_1 - \hat{V}_0}{j8} = 0 \quad (1)$$

$$\frac{\hat{V}_0 - \hat{V}_1}{j8} + \frac{\hat{V}_0}{4} = 0 \Rightarrow \hat{V}_0 \left(\frac{1}{4} + \frac{1}{j8} \right) = \frac{\hat{V}_1}{j8}$$

→ or $\hat{V}_1 = \hat{V}_0 (1 + j2)$

substituting into (1) $\frac{\hat{V}_0 (1 + j2) - 4e^{-j60^\circ}}{8} + \frac{\hat{V}_0 (1 + j2)}{-j4} + \frac{\hat{V}_0 (1 + j2) - \hat{V}_0}{j8} = 0$

$$\hat{V}_0 \left[\frac{1}{8} + j\frac{1}{4} + j\frac{1}{4} - \frac{1}{8} + \frac{1}{8} - \frac{1}{4} + \frac{1}{4} \right] = \frac{1}{2} e^{-j60^\circ} \quad \left[\frac{j\hat{V}_0}{8} = 0 \right]$$

or $\hat{V}_0 \left[-\frac{1}{8} + j\frac{1}{2} \right] = \frac{1}{2} e^{-j60^\circ}$; $\hat{V}_0 = \frac{4e^{-j60^\circ}}{-1 + j4}$

$$\hat{V}_0 = \frac{4e^{-j60^\circ}}{\sqrt{17} e^{-j104.04^\circ}} = 0.97 e^{-j164.04^\circ}$$

$v_0(t) = 0.97 \cos(4t - 164.04^\circ)$ ←

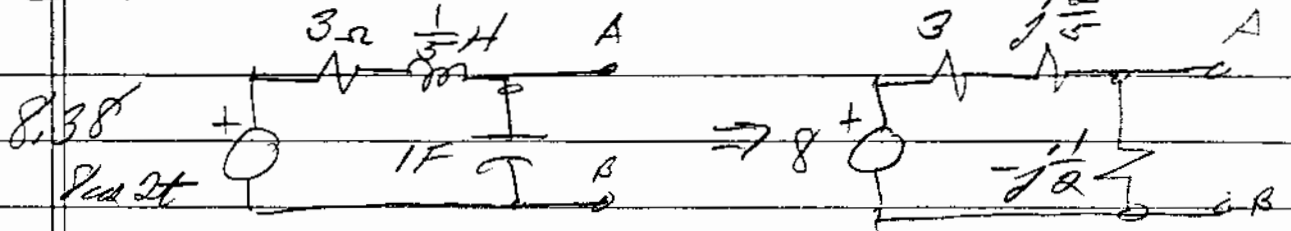
b) $Z_{eq} = 8 + \frac{-j4(4 + j8)}{4 + j4} = \frac{32 + j32 - j16 + 32}{4 + j4}$

$$Z_{eq} = \frac{64 + j16}{4 + j4} = \frac{16 + j4}{1 + j} \cdot \frac{16 + j9.8}{\sqrt{2} e^{j45^\circ}} = 11.65 e^{-j31^\circ}$$

$Z_{eq} = 11.65 e^{-j31^\circ}$ ←

EE 211

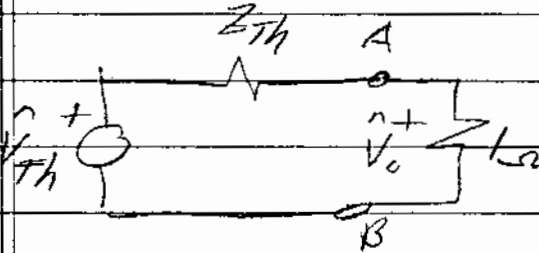
Homework 28



$$\hat{V}_{oc} = \hat{V}_{Th} = 8 \frac{-j \frac{1}{5}}{3 - j \frac{1}{5}} = \boxed{\frac{-j40}{30 - j}}$$

$$\hat{I}_{sc} = \frac{8}{3 + j \frac{2}{5}} = \frac{40}{15 + j2}$$

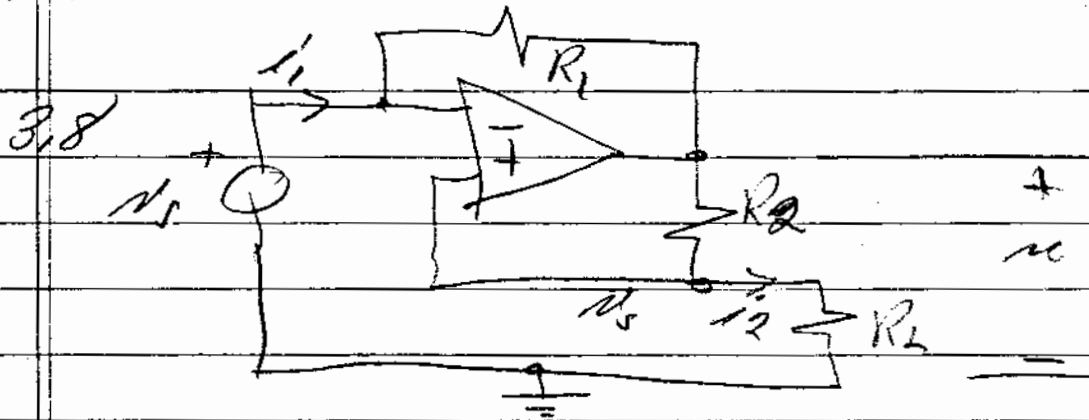
$$\hat{Z}_{Th} = \frac{-j40}{30 - j} \times \frac{15 + j2}{40} = \frac{2 - j15}{30 - j}$$



$$\hat{V}_o = \hat{V}_{Th} \frac{1}{1 + \hat{Z}_{Th}} = \frac{-j40}{30 - j} \times \frac{1}{1 + \frac{2 - j15}{30 - j}} = \frac{-j40}{32 - j16}$$

$$\hat{V}_o = \frac{-j15}{4 - j2} = \frac{30 \angle -90^\circ}{4.472 \angle 26.57^\circ} = \boxed{1.12 \angle -63.43^\circ}$$

$$\boxed{v_o(t) = 1.12 \cos(2t - 63.43^\circ)} \quad \ominus$$



$$v \frac{R_1}{R_1 + R_2} = v_s \quad \text{or} \quad v = v_s \left\{ \frac{R_1 + R_2}{R_1} \right\}$$

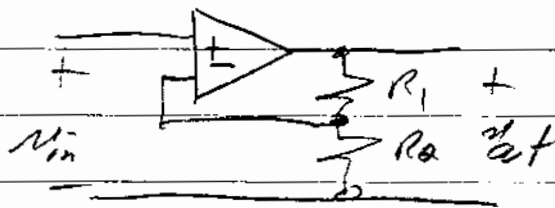
$$i_2 = \frac{v_s}{R_2} \quad ; \quad i_1 = \frac{v_s - v}{R_1}$$

$$\text{so } \frac{i_2}{i_1} = \frac{\frac{v_s}{R_2}}{\frac{v_s - v}{R_1}} = \frac{R_1}{R_2} \frac{v_s}{v_s - v_s \left[\frac{R_1 + R_2}{R_1} \right]}$$

$$\frac{i_2}{i_1} = R_1 \frac{1}{R_1 - R_2 - R_2} = - \frac{R_1}{R_2}$$

Inverting Op-Amp has input resistance equal to R_{in} . We are limited to using resistors $\leq 200k\Omega$ so to obtain $R_{in} > 250k\Omega$ I will use a non inverting first stage. This will give me the necessary R_{in} .

Make 1st stage gain = 20

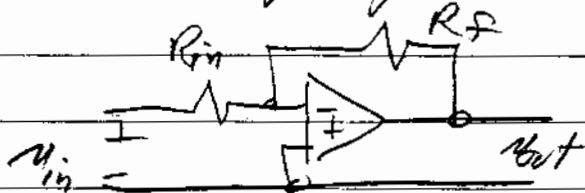


$$\text{Gain} = \frac{R_2 + R_1}{R_2} = 20$$

$$\text{let } R_2 = 10k\Omega$$

$$\text{Then } 1 + \frac{R_1}{10^4} = 20 \quad ; \quad R_1 = (20 - 1) \times 10^4 = 190k\Omega$$

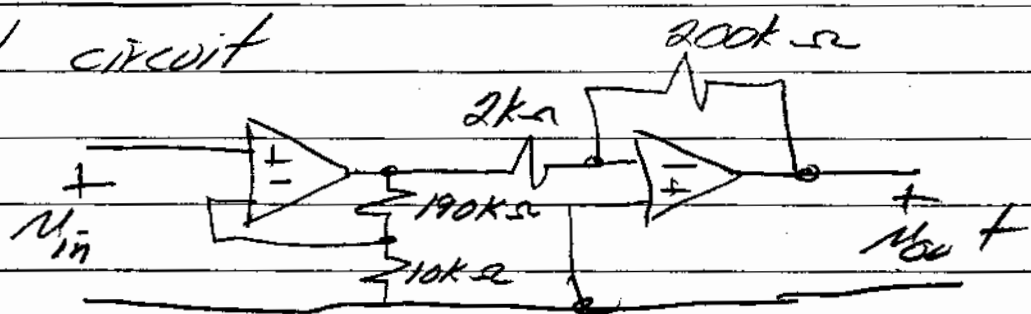
2nd stage gain = -100

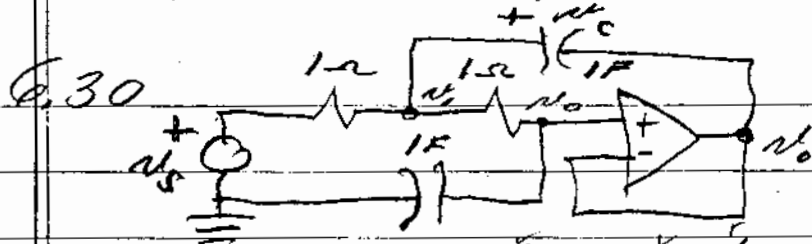


$$\text{Gain} = -\frac{R_f}{R_{in}}$$

pick $R_f = 200k\Omega$
then $R_{in} = 2k\Omega$

total circuit





$$v_o(t) = v(t)$$

"zero state" $\therefore v_o(0) = 0$

Nodal voltage eq.

$$\frac{v_1 - 1}{1} + \frac{v_1 - v_o}{1} + \frac{d}{dt}(v_1 - v_o) = 0 \quad (1)$$

$$\frac{v_o - v_1}{1} + \frac{dv_o}{dt} = 0 \quad (2)$$

from (2) $v_1 = v_o + \frac{dv_o}{dt}$

substituting into (1) 9NBS: $2(v_o + \frac{dv_o}{dt}) - v_o + \frac{d}{dt}(v_o + \frac{dv_o}{dt}) - \frac{dv_o}{dt} = 1$

or $\frac{d^2 v_o}{dt^2} + 2 \frac{dv_o}{dt} + v_o = 1$; $v_{oH} = A e^{st}$

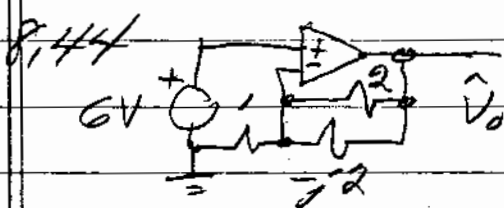
$$s^2 + 2s + 1 = 0 \quad s_{1,2} = \frac{-2 \pm \sqrt{4 - 4}}{2} = -1$$

$v_{o \text{ particular}} = K = 1$ $\therefore v_o = A_1 e^{-t} + A_2 t e^{-t} + 1$

but $v_o(0) = 0 \therefore A_1 = -1$

also $v_1(0) = 0$ so from (2) $\frac{dv_o}{dt} = 0$

$$\left. \frac{dv_o}{dt} \right|_{t=0} = 1 + A_2 \quad \left[v_o(t) = -e^{-t} - t e^{-t} + 1 \right]$$



$$\frac{6 - \hat{V}_o}{2} + \frac{6 - \hat{V}_o}{-j2} + \frac{\hat{V}_o}{1} = 0$$

$$\hat{V}_o \left(+\frac{1}{2} + j\frac{1}{2} \right) = 6 \left(+1 + j\frac{1}{2} + \frac{1}{2} \right)$$

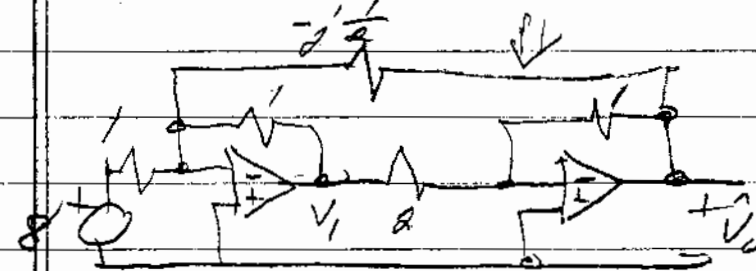
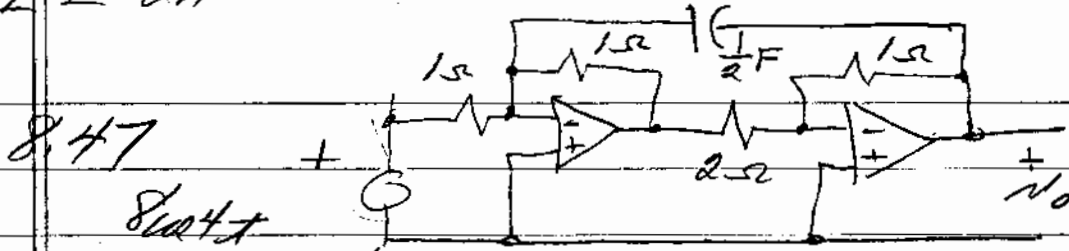
$$\text{or } \hat{V}_o = \frac{9 + j3}{\frac{1}{2} + j\frac{1}{2}} = \frac{18 + j6}{1 + j} = \frac{18.97 \angle 18.43^\circ}{\sqrt{2} \angle 45^\circ} = 13.41 \angle -26.57^\circ$$

$$v_o(t) = \text{Im} \{ \hat{V}_o e^{j2t} \} = 13.41 \sin(2t - 26.57^\circ)$$

$$\text{or } v_o(t) = 13.41 \cos(2t - 116.57^\circ)$$

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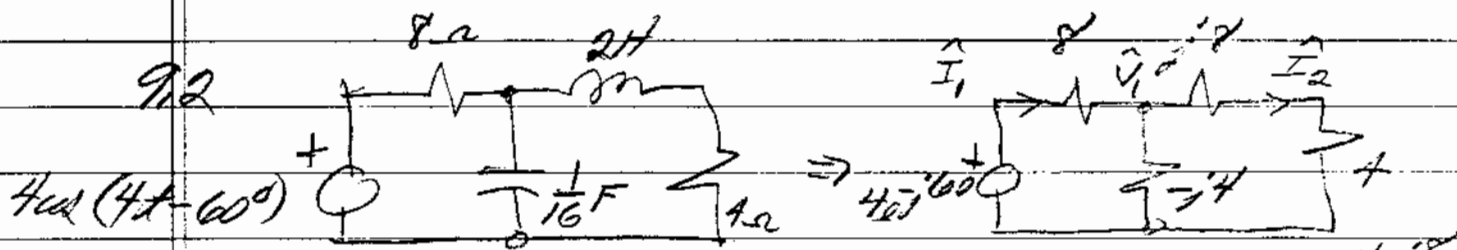
Homework 32



$$\begin{aligned}
 \text{KCL @ 1st inverting node} & \quad -\frac{8}{1} - \frac{V_1}{1} - \frac{\hat{V}_o}{-j/2} = 0 \\
 \text{KCL @ 2nd inverting node} & \quad -\frac{V_1}{2} - \frac{V_o}{1} = 0
 \end{aligned}
 \quad \left. \begin{array}{l} \\ \\ \end{array} \right\} \begin{array}{l} \hat{V}_o(-2j) - \hat{V}_1 = 8 \\ \hat{V}_1 = -2\hat{V}_o \end{array}$$

$$\therefore \hat{V}_o(-2j + 2) = 8 \quad ; \quad \hat{V}_o = \frac{8}{2-2j} = \frac{4}{1-j} = \frac{4}{\sqrt{2}} \angle^{45^\circ}$$

$$\text{or } V_o(t) = 2\sqrt{2} \cos(4t + 45^\circ)$$



$$\frac{\hat{V}_1 - 40e^{-j60^\circ}}{8} + \frac{\hat{V}_1}{-j4} + \frac{\hat{V}_1}{4+j8} = 0 \quad ; \quad \hat{V}_1 \left(\frac{1}{8} + \frac{1}{-j4} + \frac{1}{4+j8} \right) = \frac{1}{2} 40e^{-j60^\circ}$$

multiplying by 80 gives $\hat{V}_1 (14 + j12) = 400e^{-j60^\circ}$

$$\text{so } \hat{V}_1 = \frac{400e^{-j60^\circ}}{18.439 \angle 40.60^\circ} = 21.69 \angle -100.6^\circ$$

$$\hat{I}_1 = \frac{40e^{-j60^\circ} - 21.69 \angle -100.6^\circ}{8} = \frac{2 \angle -3.46^\circ + 0.399 \angle 9.132^\circ}{8}$$

$$\hat{I}_1 = 0.2999 - j0.1065 = 0.343 \angle -29^\circ$$

$$\hat{I}_2 = \frac{\hat{V}_1}{4+j8} = \frac{21.69 \angle -100.6^\circ}{9.944 \angle 63.43^\circ} = 0.242 \angle -164^\circ$$

$$\text{so } P_{ave} = \frac{1}{2} |\hat{I}_1|^2 8 = \boxed{470.6 \text{ mW}}$$

$$P_{ave} = \frac{1}{2} |\hat{I}_2|^2 4 = \boxed{117 \text{ mW}}$$

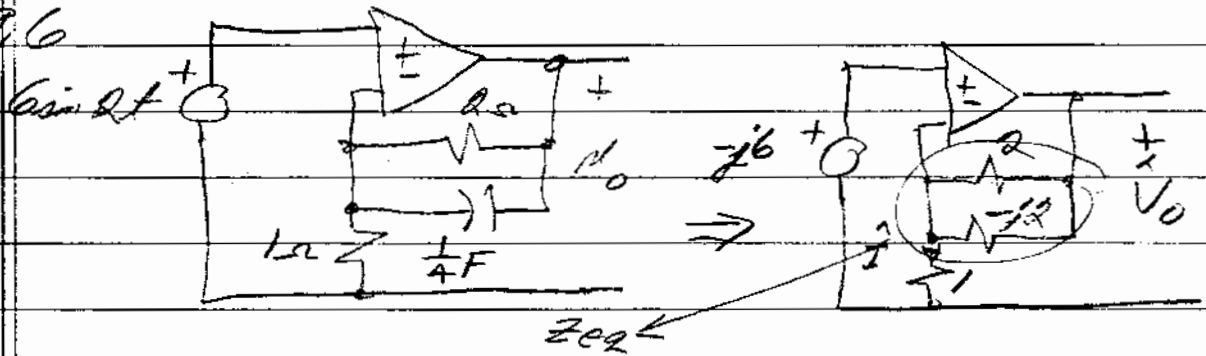
$$P_{ave} = -\frac{1}{2} \text{Re} \left\{ 40 \angle -60^\circ \times 0.343 \angle -29^\circ \right\} = \boxed{-588 \text{ mW}}$$

source

$$P_{ave} \text{ for capacitor and inductor} = 0$$

$$\Sigma P_{ave} = -0.4 \text{ mW} \neq 0$$

9.6



$$\hat{I} = -j6 ; \hat{V}_o = \hat{I} \left[\frac{-j4}{2-j2} + 1 \right] = -j6 \left[\frac{2-j6}{2-j2} \right]$$

$$\hat{V}_o = \frac{-36 - j12}{2-j2} = \frac{-18 - j6}{1-j} = \frac{18.974 \angle 218.4^\circ}{\sqrt{2} \angle 45^\circ} = 13.42 \angle 243.7^\circ$$

$$\text{or } 13.42 \angle 116.6^\circ$$

$$P_{ave_{1\Omega}} = \frac{1}{2} \operatorname{Re} \{ \hat{I} \hat{I}^* \} = \boxed{18 \text{ Watts}} \quad \leftarrow$$

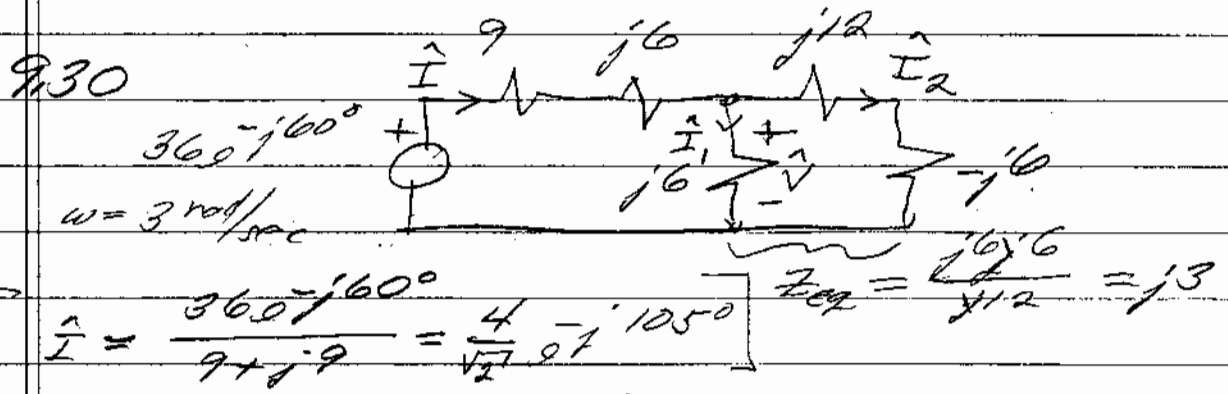
$$P_{ave_{2\Omega}} = \frac{1}{2} \left| \hat{V}_o + j6 \right|^2 \times \frac{1}{2} = \frac{1}{4} \left| \frac{-18 - j6 + j6 + 6}{1-j} \right|^2$$

$$P_{ave_{2\Omega}} = \frac{1}{4} \left| \frac{12}{\sqrt{2}} \right|^2 = \frac{1}{4} \times \frac{144}{2} = \boxed{18 \text{ Watts}} \quad \leftarrow$$

$$\boxed{P_{ave_{\text{capacitor}}} = 0}$$

$$P_{ave_{\text{out of amplifier}}} = \frac{1}{2} \operatorname{Re} \{ \hat{V}_o \hat{I}^* \} = \frac{1}{2} \operatorname{Re} \{ 13.42 \angle -116.6^\circ \cdot 6 \angle 190^\circ \}$$

$$= 36 \text{ Watts}$$



$$\hat{I} = \frac{36\angle -160^\circ}{9 + j3} = \frac{4}{\sqrt{2}} \angle -105^\circ$$

$$\hat{V} = \hat{I} Z_{eq} = \frac{12}{\sqrt{2}} \angle -15^\circ$$

$$\hat{I}_1 = \frac{\hat{V}}{j6} = \frac{2}{\sqrt{2}} \angle -105^\circ ; \hat{I}_2 = \frac{\hat{V}}{j6} = \frac{2}{\sqrt{2}} \angle -105^\circ$$

$$S_{\text{left inductor}} = \frac{1}{2} \cdot \frac{24}{\sqrt{2}} \angle -15^\circ \cdot \frac{4}{\sqrt{2}} \angle +105^\circ = 24j \text{ VA}$$

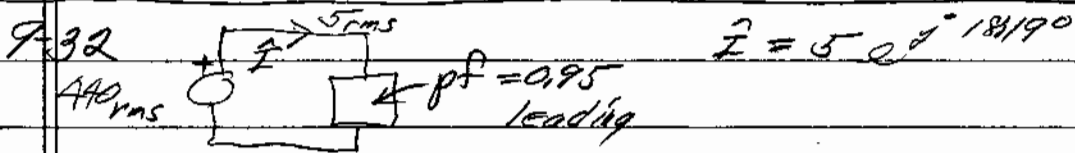
$$S_{\text{middle inductor}} = \frac{1}{2} \cdot \frac{12}{\sqrt{2}} \angle -15^\circ \cdot \frac{2}{\sqrt{2}} \angle +105^\circ = 6j \text{ VA}$$

$$S_{\text{right inductor}} = \frac{1}{2} \cdot \frac{2}{\sqrt{2}} \angle -105^\circ \cdot \frac{12}{\sqrt{2}} \angle +90^\circ = 12j \text{ VA}$$

$$S_{\text{capacitor}} = \frac{1}{2} \cdot \frac{2}{\sqrt{2}} \angle -105^\circ \cdot \frac{6}{\sqrt{2}} \angle +90^\circ = -6j \text{ VA}$$

$$S_{\text{resistor}} = \frac{1}{2} \cdot 9 \cdot \frac{4}{\sqrt{2}} \angle -105^\circ \cdot \frac{4}{\sqrt{2}} \angle +105^\circ = 36 \text{ W}$$

$$S_{\text{source}} = \frac{-36\angle -160^\circ}{2} \cdot \frac{4}{\sqrt{2}} \angle +105^\circ = \frac{-72}{\sqrt{2}} \angle -55^\circ = -36 - j36 \text{ VA}$$



$$a) \hat{S} = 440 \times 5 \angle -18.19^\circ = 2200 - j686.8 \text{ VA}$$

$$b) |\hat{S}| = 5 \times 440 = 2200 \text{ VA}$$

$$c) Z = \frac{\hat{V}}{\hat{I}} = \frac{440}{5 \angle -18.19^\circ} = 88 \angle 18.19^\circ = 83.6 - j27.47 \text{ } \Omega$$