

1. a)  $\text{Gain} = 0.9 \times 20 = 18 = \boxed{12.55 \text{ dB}}$  ←
- b)  $\theta = \lambda / \text{dia}$ ,  $A_{\text{eff}} = A_{\text{actual}} = \frac{\pi d^2}{4} = \frac{\pi}{4} \left(\frac{\lambda}{\theta}\right)^2 = D \left(\frac{\lambda^2}{4\pi}\right)$   
 $\therefore D = \frac{\pi}{4} \left(\frac{\lambda}{\theta}\right)^2 \times \frac{4\pi}{\lambda^2} = \left(\frac{\pi}{\theta}\right)^2$  ←
- c) Real input impedance  $\approx 73 \Omega$ , much better efficiency
- d) Device that radiates or receives energy from space

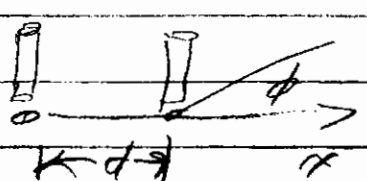
2. Noise Power =  $kTB$  received power must be  $10kTB$   
 $10kTB = P_f G_f G_r \left(\frac{\lambda}{4\pi R}\right)^2$  for no path loss

for 60dB path loss  $P_f$  must be  $10^6$  times the above

$$\therefore P_f = \frac{10 \times 1.38 \times 10^{-23} \times 4 \times 10^2 \times 10 \times 16 \times \pi^2 \times 9 \times 10^8}{10^6 \times 15.8 \times 0.25 \times 2.5 \times 10^{-4}} = 23.36 \times 10^{-4} \text{ W}$$

in the above  $\lambda = \frac{3 \times 10^8}{6 \times 10^9} = 0.5 \times 10^{-1}$  and  $R_{\text{trans}} = 10^{10} = 15.8$

so for no path loss  $P_f = 2.336 \text{ mW}$  } ←  
 and for 60dB path loss  $P_f = 2.336 \text{ kW}$  }

3.   $|A| = \frac{\sin \chi}{\sin \frac{\chi}{2}}$  with  $\chi = \frac{2\pi d}{\lambda} \cos \phi$

want maximum @  $\phi = 0$  so  $\frac{2\pi d}{\lambda} = \psi$

zero @  $\phi = \pi$  or  $\chi = -\frac{2\pi d}{\lambda} - \frac{2\pi d}{\lambda} = -\frac{4\pi d}{\lambda}$

1st zero for  $|A|$  @  $\chi = -\pi$

so  $-\pi = -\frac{4\pi d}{\lambda}$  or  $\boxed{\frac{d}{\lambda} = \frac{1}{4} \text{ and } \psi = \frac{\pi}{2}}$  ←

# ANTENNA ARRAY RADIATION PATTERNS

The radiation pattern of a linear antenna array is given by the following:

$$N := 2; \quad d := \frac{1}{4}; \quad \psi := \frac{\pi}{2}; \quad j := \sqrt{-1}; \quad \phi := 0, \frac{\pi}{100} \dots 2 \cdot \pi \quad n := 0, 1 \dots N - 1; \quad F(\phi) := \left[ \frac{1}{N} \cdot \sum_n e^{-j \cdot n \cdot (2 \cdot \pi \cdot d \cdot \cos(\phi) - \psi)} \right]^2$$

Where "N" is the number of array elements, "ψ" the progressive phase shift (element to element), and "d" the element spacing in wavelengths.

