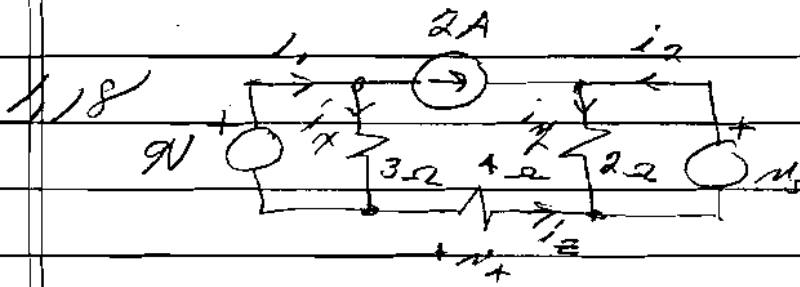


a)  $v_1 = 30V$   $\therefore i_1 = \frac{30}{5} = 6A$  ←

b)  $v_2 = 12V$   $\therefore i_2 = -\frac{12}{4} = -3A$  ←

c)  $v_3 = -9V$   $\therefore i_3 = -\frac{-9}{3} = 3A$  ←

d)  $v_4 = -3V$   $\therefore i_4 = -3A$



a)  $v_5 = 2V$  ;  $i_x = \frac{9}{3} = 3A$  ;  $i_y = \frac{2}{2} = 1A$

∴  $i_R + 2 - i_y = 0$  or  $i_R = i_y - 2 = -1$

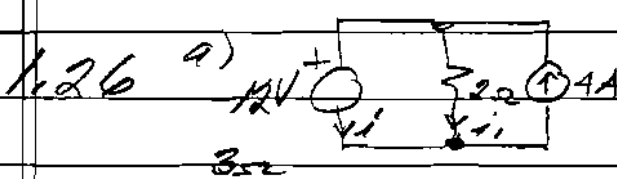
$i_2 + i_y - i_x = 0$  or  $i_2 = i_x - i_y = -2$  ∴  $v_4 = -8$

b)  $v_5 = 4V$  ;  $i_y = 2A$ ,  $i_x = 3A$

again  $i_2 = i_y - 2 = 0$  ;  $i_2 = i_x - i_y = -2A$  ;  $v_4 = i_2 \cdot 4 = -8$

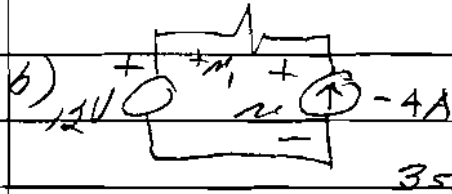
c)  $v_5 = 6V$  ;  $i_x = 3A$ ,  $i_y = 3A$

again  $i_2 = i_y - 2 = 1A$  ;  $i_2 = i_x - i_y = -2A$  ;  $v_4 = 8$



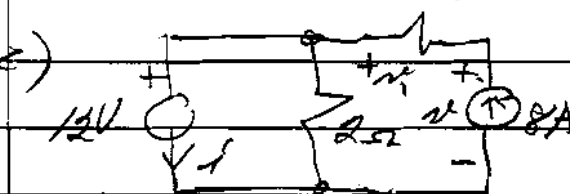
$i = \frac{12}{2} = 6A$

$i + i_1 - 4 = 0$  or  $i_1 = 4 - 6 = -2A$



$v_1 = -(-4) \times 3 = 12V$

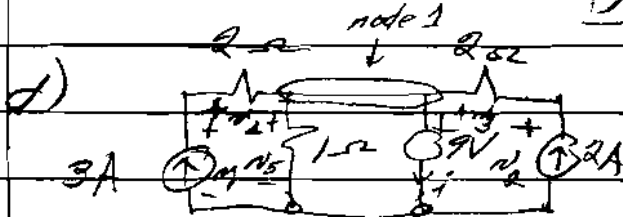
$-12 + 12 + v_1 = 0$  ∴  $v_1 = 0$



$v_1 = -3 \times 8 = -24V$

$-12 + v_1 + v_1 = 0$  ∴  $v_1 = 36V$

$i = 8 - \frac{12}{2} = 2A$



$-9 + v_3 + i_2 = 0$  but  $v_3 = -2 \times 2 = -4$

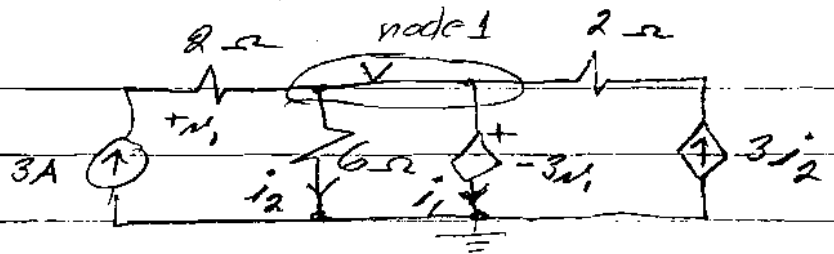
∴  $v_2 = 9 - v_3 = 13V$

KCL @ node 1  $3 - i_1 - i + 2 = 0$

$v_4 = 2 \times 3 = 6V$  ;  $-v_1 + v_4 + v_3 + v_2 = 0$  ∴  $v_1 = 15$

$i = -4A$

143 a)  $K = -3$



$V_1 = 6V$     $i_1 = -3A$     $i_2 = -3A$     $i_1 = \frac{-3V_1}{6} = -3A$

KCL @ node 1

$$\begin{cases} -3 + i_2 + i_1 - 3i_2 = 0 \\ -3 - 3 + i_1 - 3(-3) = 0 \end{cases}$$

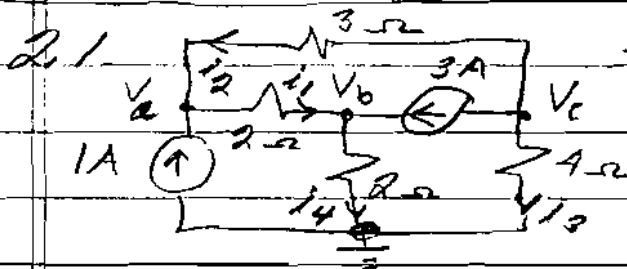
$i_1 = -3A$  ←

Node Voltage Solution

$-3 + \frac{V}{6} + i_1 - 3i_2 = 0 \Rightarrow -3 + \frac{V}{6} + i_1 - 3\frac{V}{6} = 0$

so  $i_1 = 3 + V(\frac{1}{6} - \frac{1}{2}) = 3 + (-3A)\frac{1}{3}$  but  $i_1 = 6$

so  $i_1 = 3 - 6 = -3A$  ←



Node Equations

$-1 + \frac{V_a - V_b}{2} + \frac{V_b - V_c}{3} = 0$

$\frac{V_b - V_a}{2} + \frac{V_b}{3} = 3$

$\frac{V_c - V_a}{3} + \frac{V_c}{4} = -3$

or  $V_a(\frac{5}{6}) - \frac{1}{2}V_b - \frac{1}{3}V_c = 1$

$$\begin{cases} 5V_a - 3V_b - 2V_c = 6 \\ -\frac{1}{2}V_a + V_b = 3 \\ -\frac{V_a}{3} + V_c(\frac{7}{12}) = -3 \end{cases} \Rightarrow \begin{cases} 5V_a - 3V_b - 2V_c = 6 \\ -V_a + 2V_b = 6 \\ -4V_a + 7V_c = -36 \end{cases}$$

$V_c = \frac{1}{33} \begin{vmatrix} 6 & -3 & 2 \\ 6 & 2 & 0 \\ -36 & 0 & 7 \end{vmatrix} = \frac{-36(4) + 7(12 + 18)}{-4(4) + 7(10 - 3)} = \frac{-144 + 210}{-16 + 49} = \frac{66}{33} = 2$

$V_b = \frac{1}{33} \begin{vmatrix} 5 & 6 & -2 \\ -1 & 2 & 0 \\ -4 & 0 & 7 \end{vmatrix} = \frac{-2(36 + 24) + 7(30 + 6)}{33} = \frac{-120 + 252}{33} = 4V$

$V_a = \frac{1}{33} \begin{vmatrix} 5 & -3 & 6 \\ -1 & 2 & 4 \\ -4 & 0 & -36 \end{vmatrix} = \frac{-4(-18 - 12) - 36(10 - 3)}{33} = \frac{120 - 252}{33} = -4V$

ES. 332

Homework 3

(continued)

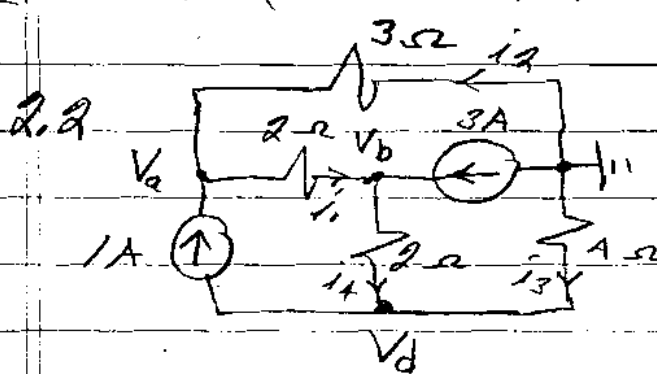
2.1

$$b) i_1 = \frac{V_a - V_b}{2} = \boxed{-1 A}$$

$$i_2 = \frac{V_c - V_a}{3} = \frac{-6}{3} = \boxed{-2 A}$$

$$i_3 = \frac{V_c}{4} = \boxed{-1 A}$$

$$i_4 = \frac{V_b}{2} = \boxed{2 A}$$



$$\frac{V_a}{3} + \frac{V_b - V_d}{2} = 1$$

$$\frac{V_b - V_a}{2} + \frac{V_b - V_d}{2} = 3$$

$$\frac{V_d - V_b}{2} + \frac{V_d}{4} = -1$$

or  $V_a \frac{5}{6} - V_b \frac{1}{2} = 1$

$$\left. \begin{aligned} -V_a \frac{1}{2} + V_b - \frac{V_d}{2} &= 3 \\ -V_b \frac{1}{2} + V_d \frac{3}{4} &= -1 \end{aligned} \right\} \begin{aligned} 5V_a - 3V_b &= 6 \\ -V_a + 2V_b - V_d &= 6 \\ -2V_b + 3V_d &= -4 \end{aligned}$$

$$V_d = \frac{\begin{vmatrix} 6 & -3 & 0 \\ 6 & 2 & -1 \\ -4 & -2 & 3 \end{vmatrix}}{\begin{vmatrix} 5 & -3 & 0 \\ -1 & 2 & -1 \\ 0 & -2 & 3 \end{vmatrix}} = \frac{6(6-2) + 3(18-4)}{5(6-2) + 3(-3)} = \frac{66}{11} = \boxed{6V}$$

$$V_b = \frac{1}{11} \begin{vmatrix} 5 & 6 & 0 \\ -1 & 6 & -1 \\ 0 & -4 & 3 \end{vmatrix} = \frac{1}{11} \{ 5(18-4) - 6(-3) \} = \boxed{8V}$$

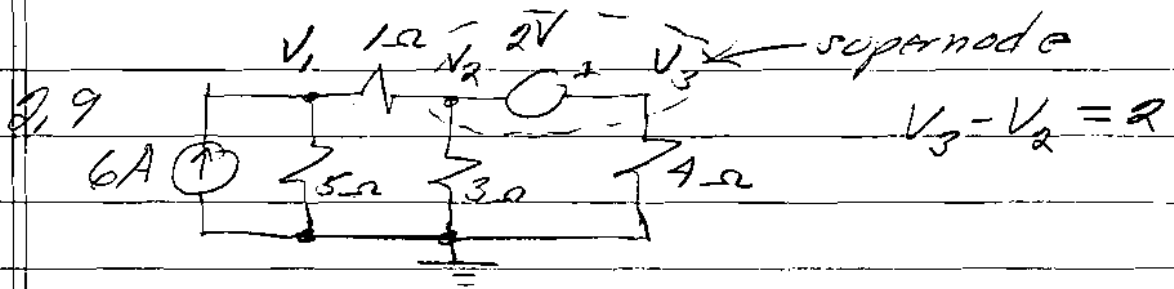
$$V_d = \frac{1}{11} \begin{vmatrix} 5 & -3 & 6 \\ -1 & 2 & 6 \\ 0 & -2 & -4 \end{vmatrix} = \frac{1}{11} \{ 5(-8+12) + 1(18+12) \} = \boxed{1V}$$

so  $i_1 = \frac{V_b - V_d}{2} = \boxed{-1A}$

$$i_2 = -\frac{V_a}{3} = \boxed{-2A}$$

$$i_3 = -\frac{V_d}{4} = \boxed{-1A}$$

$$i_4 = \frac{V_b - V_d}{2} = \boxed{2A}$$



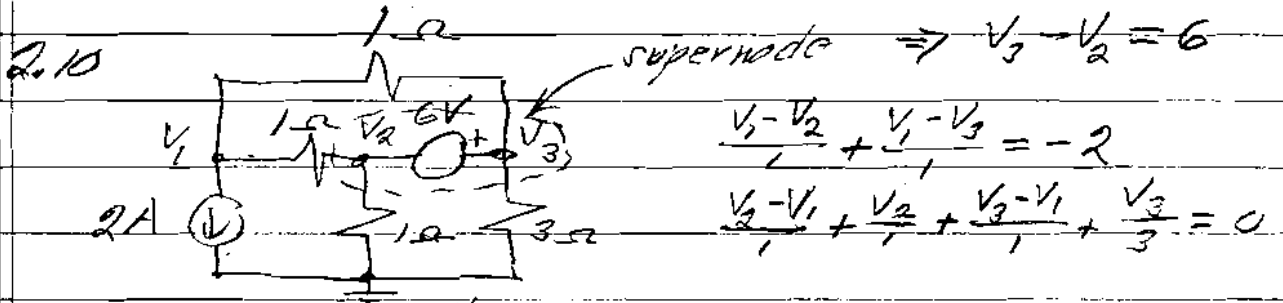
$$\left. \begin{aligned} \frac{V_1}{5} + \frac{V_1 - V_2}{1} &= 6 \\ \frac{V_2 - V_1}{1} + \frac{V_2}{3} + \frac{V_2}{4} &= 0 \end{aligned} \right\} \begin{aligned} \frac{6}{5}V_1 - V_2 &= 6 \\ -V_1 + \left(\frac{4}{3} + \frac{1}{4}\right)V_2 &= -\frac{1}{2} \end{aligned}$$

or 
$$\begin{cases} 6V_1 - 5V_2 = 30 \\ -12V_1 + 19V_2 = -6 \end{cases}$$

$$V_1 = \frac{\begin{vmatrix} 30 & -5 \\ -6 & 19 \end{vmatrix}}{\begin{vmatrix} 6 & -5 \\ -12 & 19 \end{vmatrix}} = \frac{540}{54} = \boxed{10V} \leftarrow$$

$$V_2 = \frac{\begin{vmatrix} 6 & 30 \\ -12 & -6 \end{vmatrix}}{54} = \frac{324}{54} = \boxed{6V} \leftarrow$$

$$V_3 = V_2 + 2 = \boxed{8V} \leftarrow$$



$$\frac{V_1 - V_2}{1} + \frac{V_1 - V_3}{1} = -2$$

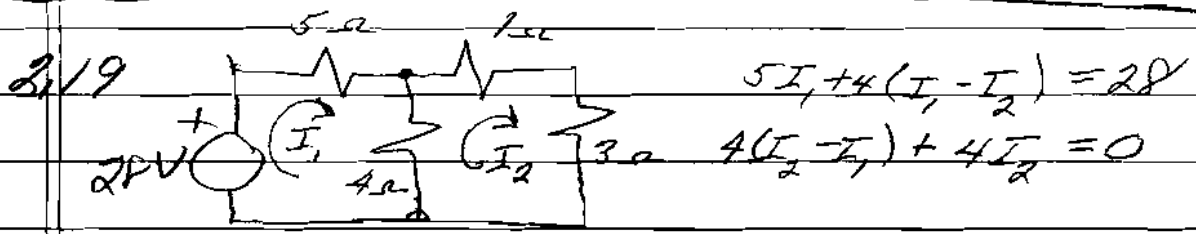
$$\frac{V_2 - V_1}{1} + \frac{V_2}{1} + \frac{V_3 - V_1}{1} + \frac{V_3}{3} = 0$$

or  $2V_1 - V_2 - V_3 = -2$   $\left. \begin{array}{l} 2V_1 - 2V_2 = 4 \\ -2V_1 + 2V_2 + \frac{4}{3}V_3 = 0 \\ -V_2 + V_3 = 6 \end{array} \right\} \begin{array}{l} 2V_1 - 2V_2 = 4 \\ -2V_1 + \frac{10}{3}V_2 = -8 \end{array}$

$$V_1 = \frac{\begin{vmatrix} 4 & -2 \\ -8 & \frac{10}{3} \end{vmatrix}}{\begin{vmatrix} 2 & -2 \\ -2 & \frac{10}{3} \end{vmatrix}} = \frac{\frac{40}{3} - 16}{\frac{20}{3} - 4} = \frac{40 - 48}{20 - 12} = \frac{-8}{8} = \boxed{-1V}$$

$$V_2 = \frac{\begin{vmatrix} 2 & 4 \\ -2 & -8 \end{vmatrix}}{\frac{8}{3}} = \frac{-16 + 8}{\frac{8}{3}} = \boxed{-3V}$$

$$V_3 = V_2 + 6 = \boxed{3V}$$



$$5I_1 + 4(I_1 - I_2) = 28$$

$$4(I_2 - I_1) + 4I_2 = 0$$

or  $\begin{cases} 9I_1 - 4I_2 = 28 \\ -4I_1 + 8I_2 = 0 \end{cases}$

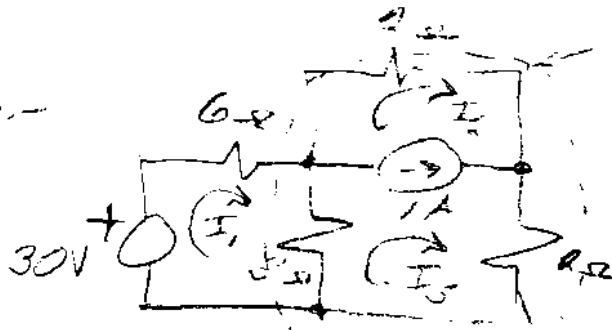
$$I_1 = \frac{\begin{vmatrix} 28 & -4 \\ 0 & 8 \end{vmatrix}}{\begin{vmatrix} 9 & -4 \\ -4 & 8 \end{vmatrix}} = \frac{224}{72 - 16} = \frac{224}{56} = \boxed{4A}$$

$$I_2 = \frac{\begin{vmatrix} 9 & 28 \\ -4 & 0 \end{vmatrix}}{56} = \frac{4 \times 28}{56} = \boxed{2A}$$

FS 33K

Homework 6

2.2-



supermesh  $\Rightarrow I_3 - I_2 = 1$

$$6I_1 + 3(I_1 - I_2) = 30$$

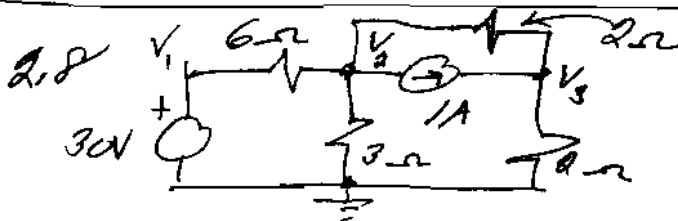
$$3(I_3 - I_1) + 2I_2 + 5I_3 = 0$$

$$\begin{aligned} \text{or } 9I_1 - 3I_2 &= 30 \\ -3I_1 + 2I_2 + 5I_3 &= 0 \\ -I_2 + I_3 &= 1 \end{aligned} \quad \left. \begin{aligned} 9I_1 - 3I_2 &= 33 \\ -3I_1 + 7I_2 &= -5 \end{aligned} \right\}$$

$$I_1 = \frac{\begin{vmatrix} 33 & -3 \\ -5 & 7 \end{vmatrix}}{\begin{vmatrix} 9 & -3 \\ -3 & 7 \end{vmatrix}} = \frac{231 - 15}{63 - 9} = \frac{216}{54} = \boxed{4A}$$

$$I_2 = \frac{\begin{vmatrix} 9 & 33 \\ -3 & -5 \end{vmatrix}}{54} = \frac{-45 + 99}{54} = \boxed{1A}$$

$$I_3 = 1 + I_2 = \boxed{2A}$$



$$V_1 = 30 \leftarrow$$

$$\frac{V_2 - 30}{6} + \frac{V_2}{3} + \frac{V_2 - V_3}{2} + 1 = 0$$

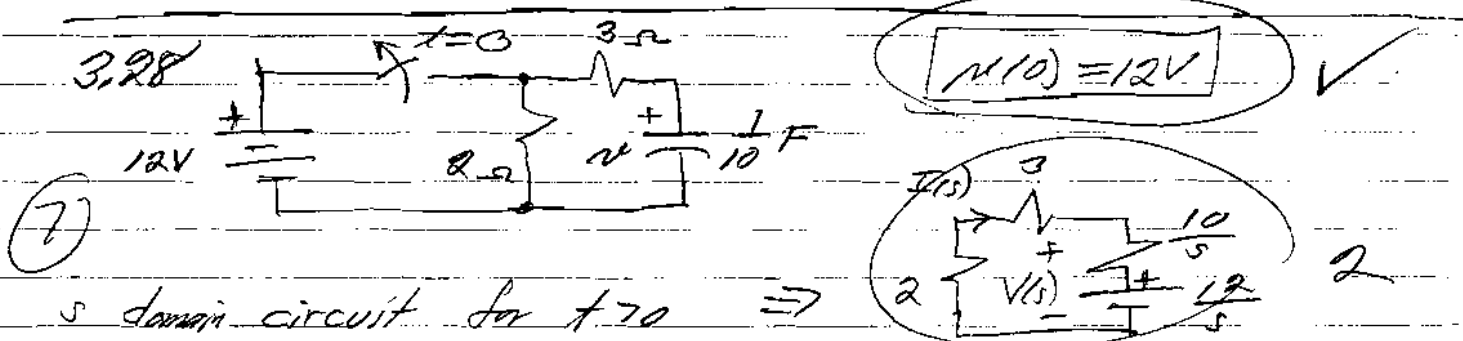
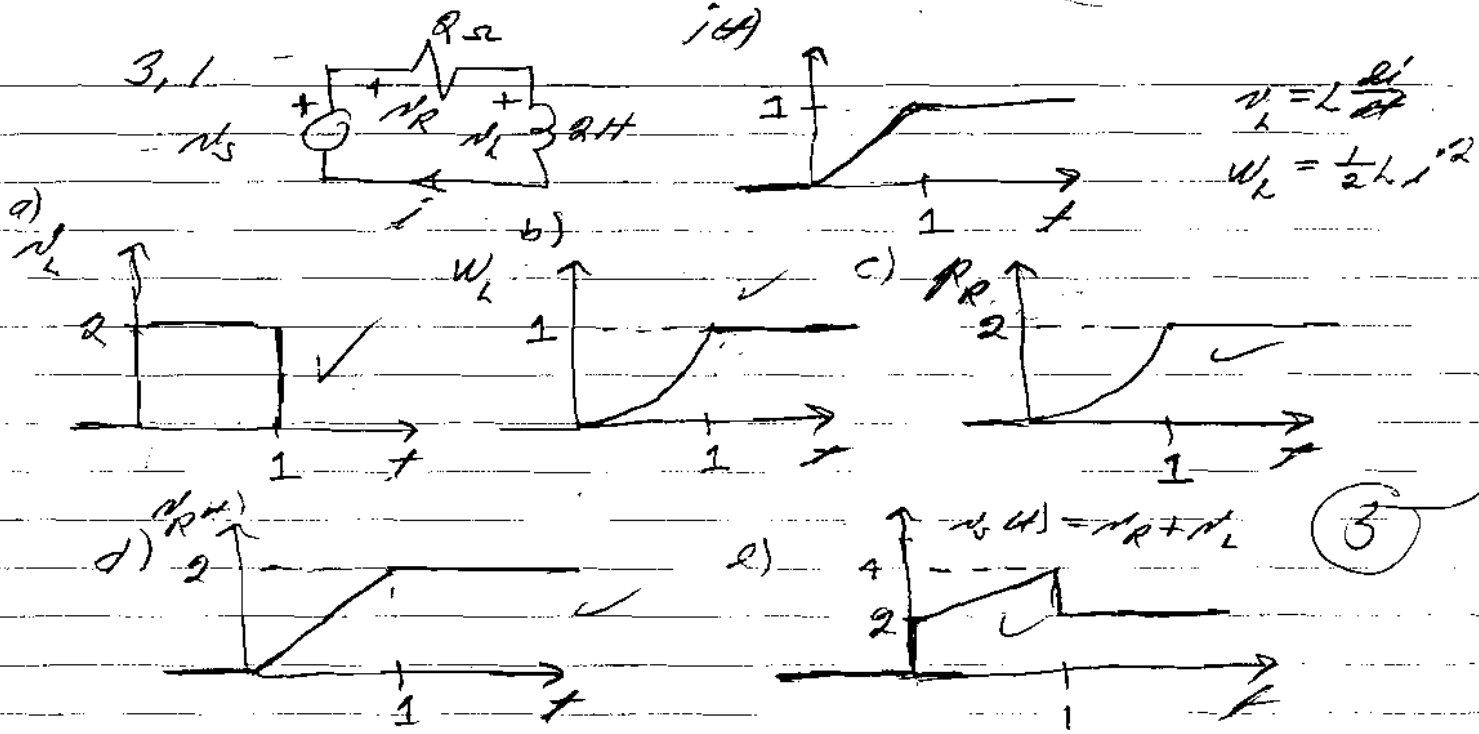
$$\frac{V_3 - V_2}{2} + \frac{V_3}{2} = 1$$

$$\text{or } 2V_2 - V_3 = 8 ; -V_2 + 2V_3 = 2$$

$$V_2 = \frac{\begin{vmatrix} 8 & -1 \\ 2 & 2 \end{vmatrix}}{\begin{vmatrix} 2 & -1 \\ -1 & 2 \end{vmatrix}} = \frac{16 + 2}{4 - 1} = \frac{18}{3} = \boxed{6V} \rightarrow$$

$$V_3 = \frac{\begin{vmatrix} 2 & 8 \\ -1 & 2 \end{vmatrix}}{3} = \frac{4 + 8}{3} = \frac{12}{3} = \boxed{4V} \rightarrow$$

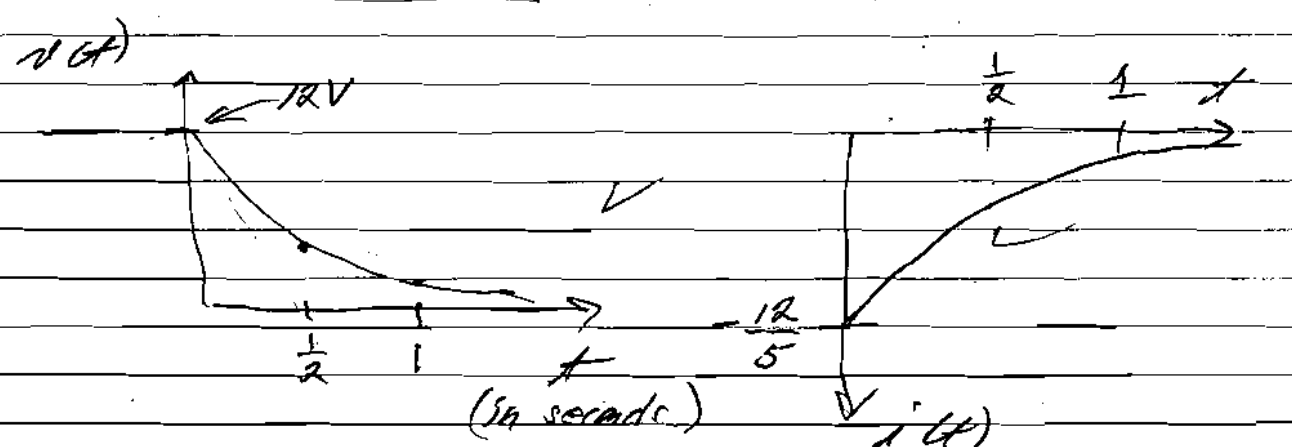




$I(s) \left[ 5 + \frac{10}{s} \right] = -\frac{12}{s}$  ;  $I(s) = -\frac{12/s}{5s+10} = -\frac{12}{5} \cdot \frac{1}{s+2}$

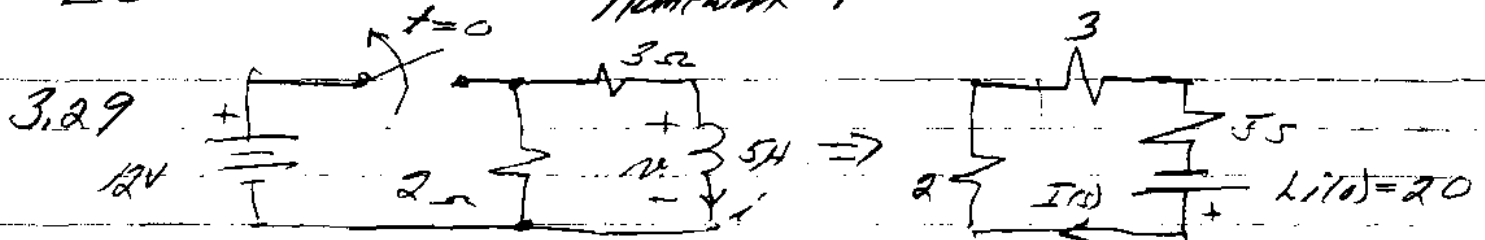
$\therefore i(t) = -\frac{12}{5} e^{-2t} \text{ A}$

$v(t) = -5i(t) = 12 e^{-2t} \text{ V}$



ES 332

Homework 7

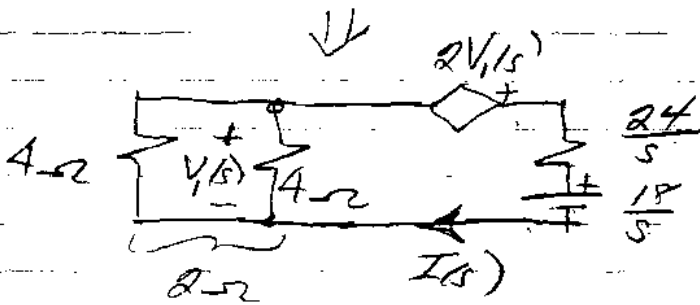
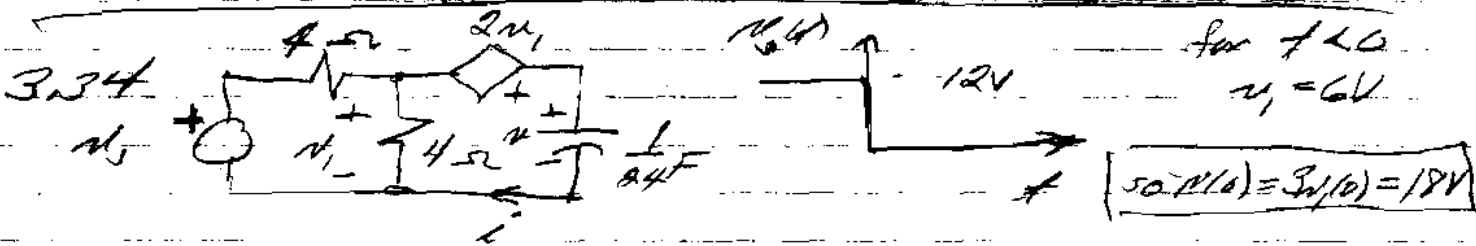


$$i(t) = \frac{12}{3} = 4A$$

$$\therefore I(t) [5 + 5s] = 20$$

$$\text{or } I(s) = \frac{4}{s+1}; i(t) = 4e^{-t} \mu A$$

$$V(t) = I(t) \times 5S - 20 = \frac{20s}{s+1} - 20 = -\frac{20}{s+1}; v(t) = -20e^{-t} \mu A$$



$$2I(s) - 2V_1 + \frac{24}{5} I + \frac{18}{5} = 0$$

$$I(s) \left\{ 2 + \frac{24}{5} \right\} = 2V_1 - \frac{18}{5}$$

$$\text{but } V_1 = -2I(s)$$

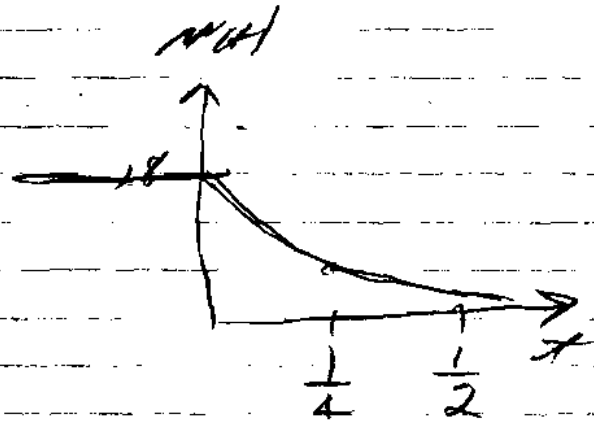
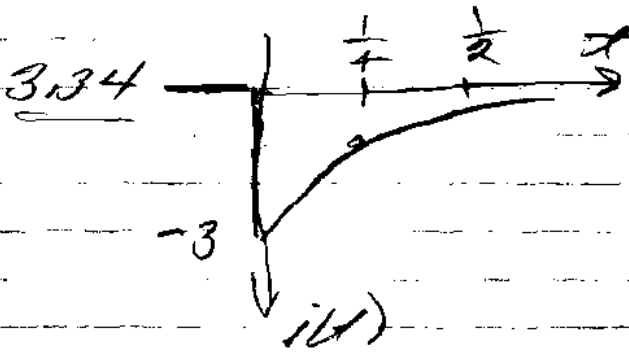
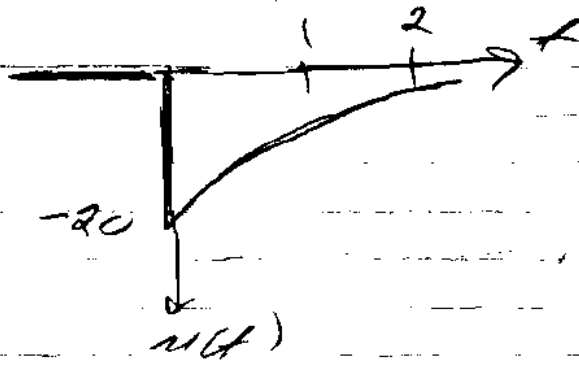
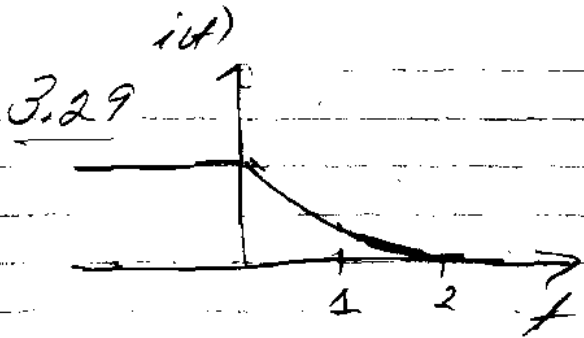
$$\therefore I(s) \left\{ 2 + \frac{24}{5} + 4 \right\} = -\frac{18}{5}; I(s) = \frac{-\frac{18}{5}}{6 + \frac{24}{5}} = \frac{-18}{6s + 24} = \frac{-3}{s+4}$$

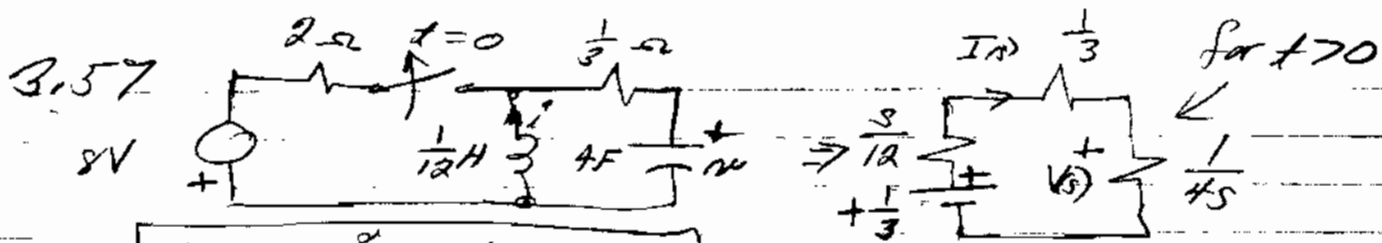
$$\text{so } i(t) = -3e^{-4t} \mu A$$

$$V(t) = I(s) \times \frac{24}{5} + \frac{18}{5} = \frac{-72}{5(s+4)} + \frac{18}{5} = \frac{-18}{5} + \frac{18}{s+4} + \frac{18}{5}$$

$$v(t) = 18e^{-4t} \mu A$$

{ sketches on next page! }



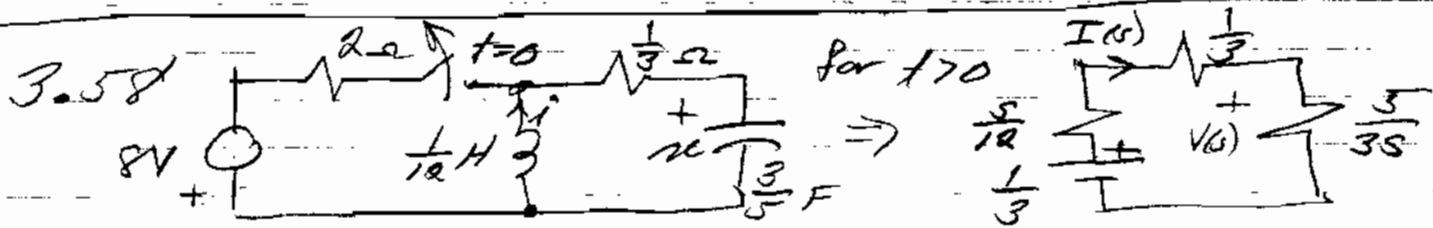


$$i(0) = +\frac{8}{2} = +4A ; v(0) = 0$$

$$I(s) \left[ \frac{5}{12} + \frac{1}{3} + \frac{1}{45} \right] - \frac{1}{3} = 0 ; I(s) = \frac{45}{5s^2 + 45s + 3} = \frac{45}{(s+1)(s+3)}$$

$$I(s) = \frac{-2}{s+1} + \frac{+6}{s+3} ; i(t) = \left[ -2e^{-t} + 6e^{-3t} \right] u(t)$$

$$V(s) = I(s) \frac{1}{45} = \frac{1}{(s+1)(s+3)} = \frac{1/2}{s+1} + \frac{-1/2}{s+3} ; v(t) = \frac{1}{2} \left[ e^{-t} - e^{-3t} \right] u(t)$$



$$i(0) = 4A ; v(0) = 0$$

$$I(s) = \frac{1/3}{\frac{5}{12} + \frac{1}{3} + \frac{5}{35}} = \frac{45}{5s^2 + 45s + 20} = \frac{4(s+2) - 8}{(s+2)^2 + 16}$$

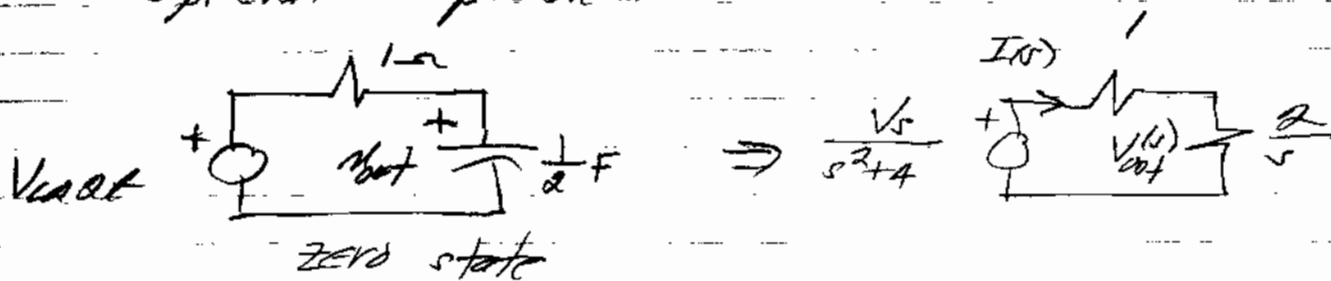
$$\text{and } i(t) = \left[ 4e^{-2t} \cos 4t - 2e^{-2t} \sin 4t \right] u(t)$$

$$V(s) = I(s) \times \frac{5}{35} = \frac{20}{3} \cdot \frac{1}{5s^2 + 45s + 20} = \frac{20}{3} \cdot \frac{1}{(s+2)^2 + 16}$$

$$v(t) = \left[ \frac{20}{3 \times 4} e^{-2t} \sin 4t \right] u(t)$$

$$v(t) = \left[ \frac{5}{3} e^{-2t} \sin 4t \right] u(t)$$

## Special problem



$$\frac{V_s}{s^2+4} = I(s) \left[ 1 + \frac{2}{s} \right] \quad \therefore I(s) = \frac{V_s}{s^2+4} \cdot \frac{s}{s+2} = \frac{V_s s}{(s+2)(s^2+4)}$$

$$I(s) = \frac{K_1}{s+2} + \frac{K_2 s + K_3}{s^2+4} \quad ; \quad K_1 = \frac{4V}{8} = \frac{V}{2}$$

$$\text{so } V_s s = \frac{V}{2}(s^2+4) + (K_2 s + K_3)(s+2)$$

$$s^2 \text{ terms} \quad V = \frac{V}{2} + K_2 \quad \text{or } K_2 = \frac{V}{2}$$

$$s \text{ terms} \quad 0 = 2K_2 + K_3 \quad \text{or } K_3 = -2K_2 = -V$$

$$I(s) = \frac{V/2}{s+2} + \frac{V/2 s - V}{s^2+4}$$

$$i(t) = \left[ \frac{V}{2} e^{-2t} + \frac{V}{2} \cos 2t - \frac{V}{2} \sin 2t \right] u(t)$$

$$V_{out}(s) = I(s) \cdot \frac{2}{s} = \frac{2sV}{(s+2)(s^2+4)} = \frac{A}{s+2} + \frac{Bs+C}{s^2+4}$$

$$A = \frac{-4V}{8} = -\frac{V}{2}$$

$$2sV = -\frac{V}{2}(s^2+4) + (Bs+C)(s+2)$$

$$s^2 \text{ terms} \quad 0 = -\frac{V}{2} + B \quad \therefore B = \frac{V}{2}$$

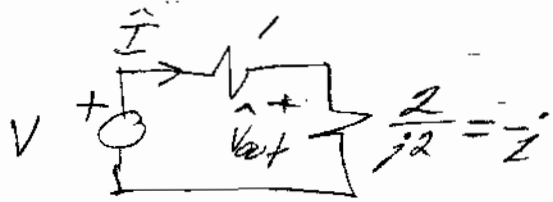
$$s \text{ terms} \quad 2V = C + 2B = C + V \quad \therefore C = V$$

$$\text{and } V_{out}(s) = \frac{-V/2}{s+2} + \frac{V/2 s + V}{s^2+4}$$

$$v_{out}(t) = \left[ -\frac{V}{2} e^{-2t} + \frac{V}{2} \cos 2t + \frac{V}{2} \sin 2t \right] u(t)$$

# Homework 9

Sinusoidal steady state solution to spectral prob.



$$\hat{I} = \frac{V}{1-j} = \frac{V}{\sqrt{2}} e^{j45^\circ}$$

$$i(t) = \text{Re}\{\hat{I} e^{j2t}\} = \frac{V}{\sqrt{2}} \cos(2t + 45^\circ)$$

$$\hat{V}_{out} = -j \hat{I} = e^{-j90^\circ} \frac{V}{\sqrt{2}} e^{j45^\circ}$$

$$\text{so } v_{out}(t) = \frac{V}{\sqrt{2}} \cos(2t - 45^\circ)$$

$$5.110 \quad H(s) = \frac{s}{s+2}$$

$$a) x(t) = u(t) \quad \therefore X(s) = \frac{1}{s} \quad \text{and} \quad Y(s) = \frac{1}{s+2}$$

$$\text{so } y(t) = \boxed{e^{-2t} u(t)}$$

$$b) x(t) = e^{-t} u(t); \quad X(s) = \frac{1}{s+1} \quad \text{and} \quad Y(s) = \frac{s}{(s+1)(s+2)}$$

$$\text{so } Y(s) = \frac{-1}{s+1} + \frac{2}{s+2} \quad \text{and} \quad y(t) = \boxed{[-e^{-t} + 2e^{-2t}] u(t)}$$

$$c) x(t) = (1 - e^{-t}) u(t); \quad X(s) = \frac{1}{s} - \frac{1}{s+1}$$

$$Y(s) = \frac{s}{s+2} \left[ \frac{1}{s} - \frac{1}{s+1} \right] = \frac{1}{s+2} + \frac{1}{s+1} - \frac{2}{s+2}$$

$$\text{or } Y(s) = \frac{-1}{s+2} + \frac{1}{s+1}$$

$$\text{and } y(t) = \boxed{[e^{-t} - e^{-2t}] u(t)}$$

$$d) x(t) = e^{-2t} u(t); \quad X(s) = \frac{1}{s+2}$$

$$\text{so } Y(s) = \frac{s}{(s+2)^2} = \frac{K_1}{s+2} + \frac{K_2}{(s+2)^2}$$

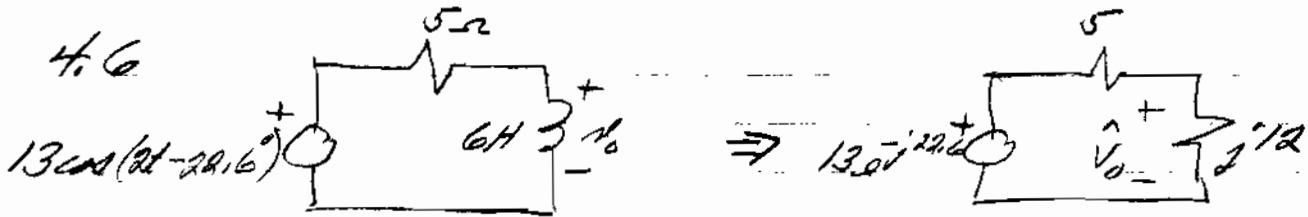
$$K_2 = -2$$

$$\text{so } s = K_1(s+2) - 2; \quad 1 = K_1$$

$$Y(s) = \frac{1}{s+2} - \frac{2}{(s+2)^2}$$

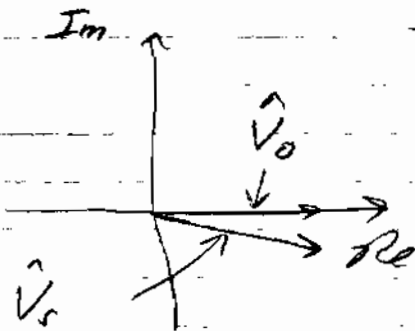
$$y(t) = \boxed{[e^{-2t} - 2te^{-2t}] u(t)}$$

# Homework 11

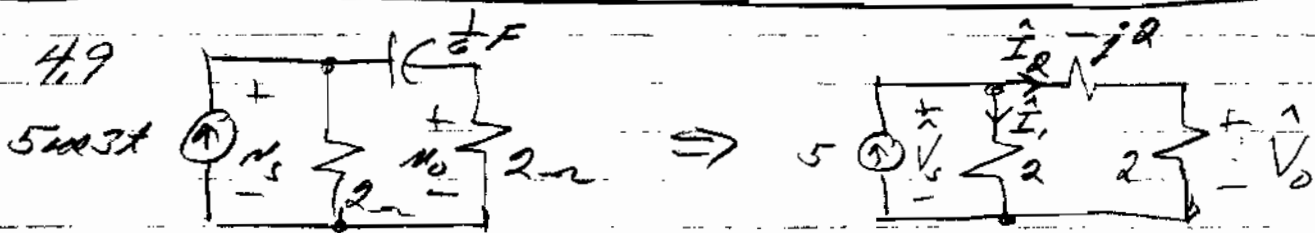


$$\hat{V}_o = \frac{13e^{j28.6^\circ} \times j12}{5 + j12} = \frac{12 \times 13 e^{j67.4^\circ}}{13 e^{j67.4^\circ}} = 12$$

so  $v_o(t) = 12 \cos(2t)$



$\hat{V}_o$  leads  $\hat{V}_s$



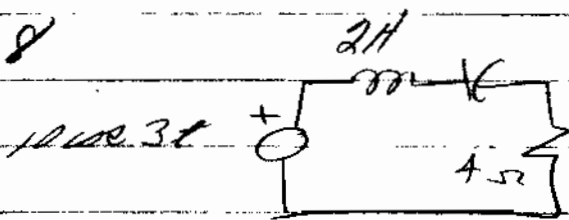
$$\hat{V}_s = \hat{I}_1 \times 2 = 2 \times 5 \times \frac{2 - j2}{4 - j2} = 10 \times \frac{2.828 e^{j45^\circ}}{4.472 e^{j26.56^\circ}} = 6.32 e^{j18.44^\circ}$$

$$\hat{V}_o = \hat{I}_2 \times 2 = 2 \times 5 \times \frac{2}{4 - j2} = \frac{20}{4.472 e^{j26.56^\circ}} = 4.47 e^{j26.56^\circ}$$

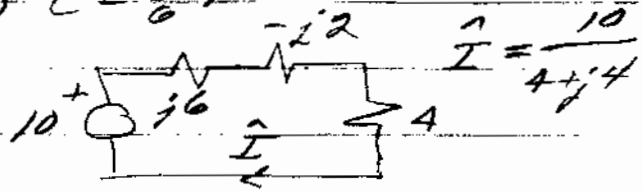
so  $v_s(t) = 6.32 \cos(3t - 18.44^\circ)$   
 $v_o(t) = 4.47 \cos(3t + 26.56^\circ)$



4.28

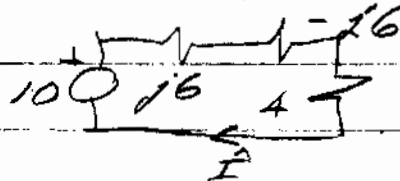


a)  $C = \frac{1}{6} F$



$$P_{avg} = \frac{1}{2} Re \left\{ \frac{40}{4+j4} \times \frac{10}{4-j4} \right\} = \frac{200}{32} = \boxed{6.25 \text{ Watts}}$$

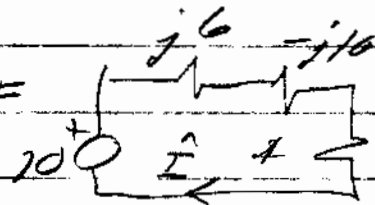
b)  $C = \frac{1}{8}$



$$I = \frac{10}{4} = \frac{5}{2}$$

$$P_{avg} = \frac{1}{2} \left( \frac{5}{2} \right)^2 \times 4 = \frac{25}{2} W$$

c)  $C = \frac{1}{30} F$



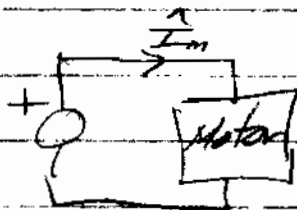
$$I = \frac{10}{4+j4}$$

$$\therefore P_{avg} = 6.25 W$$

4.44

60 Hz

220 rms



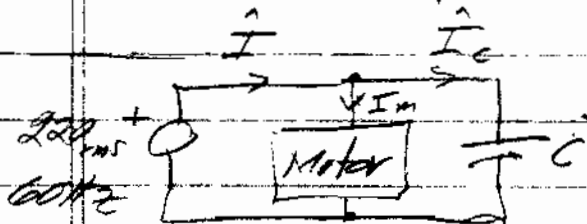
$$|I| = 20_{rms}$$

pf = 0.75 lagging

$$I = 20 e^{j41.41^\circ}$$

$$P_{avg} = V_{rms} I_{rms} \times 0.75 = \boxed{3300 \text{ Watts}}$$

From above  $\hat{I}_m = 20 e^{j41.41^\circ} = 15 - j13.2298$

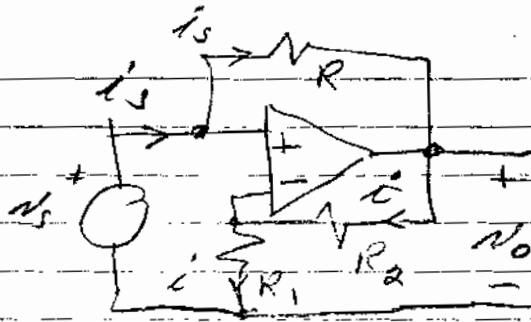


$\therefore$  for pf = 1

$$\hat{I}_c = +j13.2298 = j220 \times 2\pi \times 60 C$$

$$\text{or } C = \frac{13.2298}{2\pi \times 60 \times 220} = \boxed{1.59 \times 10^{-4} F}$$

2.30



$$i = \frac{v_s}{R_1} \quad ; \quad v_o = i(R_1 + R_2) = v_s \left(1 + \frac{R_2}{R_1}\right) \quad \left. \vphantom{i} \right\} 2$$

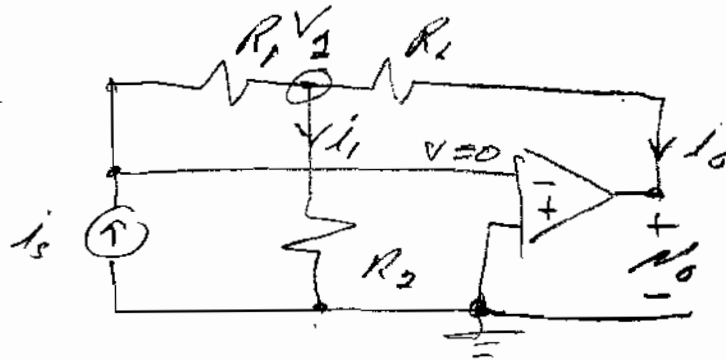
$$i_s = \frac{v_s - v_o}{R} = \frac{v_s}{R} - \frac{v_s}{R} \left(1 + \frac{R_2}{R_1}\right) = v_s \left(\frac{1}{R} - \frac{1}{R} - \frac{R_2}{RR_1}\right)$$

$$\text{or } \frac{v_s}{i_s} = -R \left(\frac{R_1}{R_2}\right) \quad \left. \vphantom{\frac{v_s}{i_s}} \right\} 2$$

ES 332

Homework 14

2.28



$$V_1 = -i_s R_1 \quad (1)$$

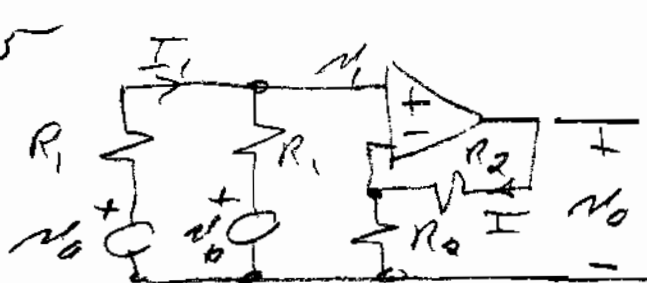
@ node 1  $\frac{V_1}{R_2} + \frac{V_1 - v_o}{R_L} + \frac{V_1}{R_1} = 0 \quad (2)$

combining (1) and (2)  $-i_s R_1 \left[ \frac{1}{R_2} + \frac{1}{R_L} + \frac{1}{R_1} \right] = \frac{v_o}{R_L}$

$$\therefore v_o = -i_s \left[ \frac{R_2 R_1}{R_2} + R_1 + R_L \right] \leftarrow$$

$$i_o = \frac{v_1 - v_o}{R_L} = \frac{-i_s R_1}{R_L} + i_s \left[ \frac{R_1}{R_2} + \frac{R_1}{R_L} + 1 \right] = i_s \left[ 1 + \frac{R_1}{R_2} \right] \leftarrow$$

2.35



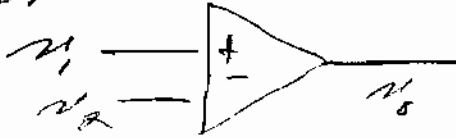
$$\left. \begin{aligned} I &= \frac{v_o}{2R_2} \\ v_1 &= IR_2 = \frac{v_o}{2} \end{aligned} \right\}$$

$$-v_a + I_1 R_1 + I_1 R_1 + v_b = 0 \quad \text{so } I_1 = \frac{v_a - v_b}{2R_1}$$

$$v_1 = I_1 R_1 + v_b = \frac{v_a - v_b}{2} + v_b = \frac{v_a + v_b}{2}$$

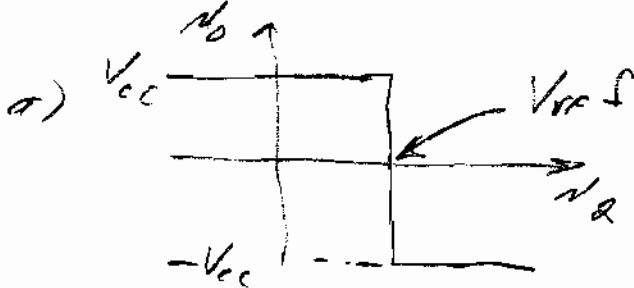
$$\text{so } v_o = 2v_1 = v_a + v_b \leftarrow$$

10.67

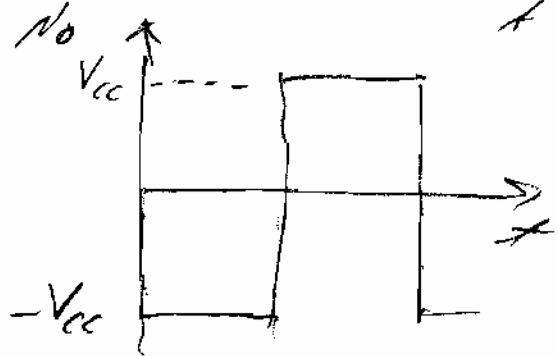
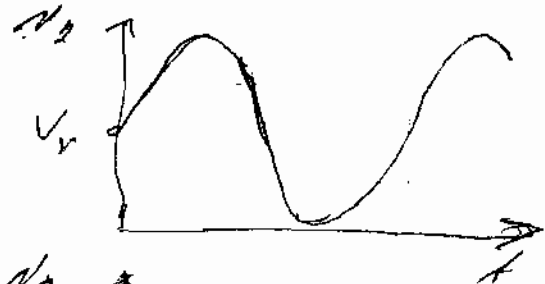


$$N_1 = V_{ref} > 0$$

$$N_2 = \text{input}$$

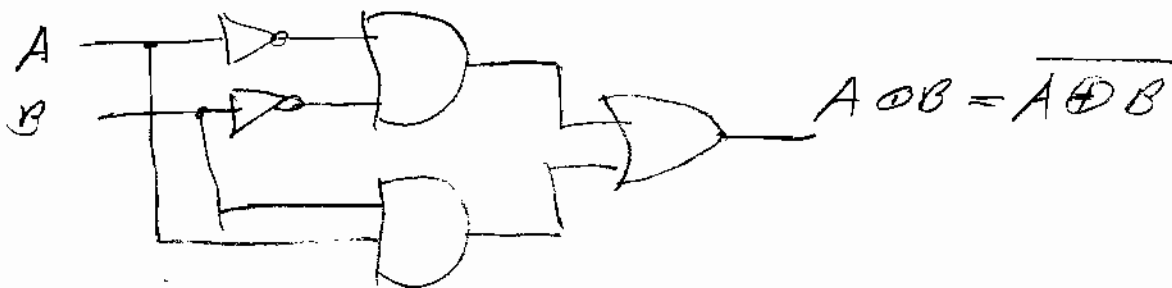


b)  $N_0 = V_r + V_r \sin \omega t$



11.26

A	B	$A \odot B = \bar{A} \cdot \bar{B} + AB$
0	0	1
0	1	0
1	0	0
1	1	1



ES-332

Homework 16

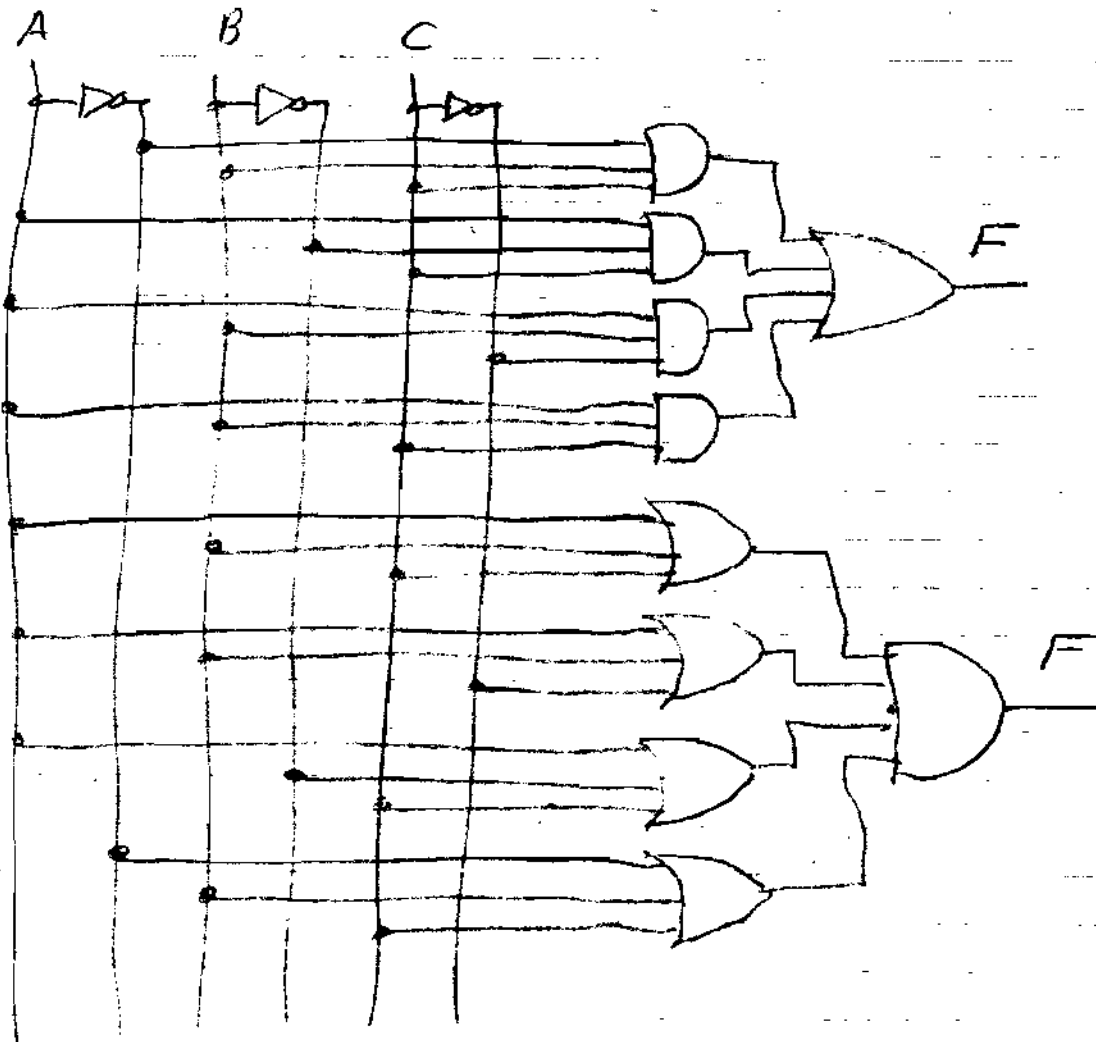
11.44

A	B	C	F	
0	0	0	0	m <sub>0</sub>
0	0	1	0	m <sub>1</sub>
0	1	0	0	m <sub>2</sub>
0	1	1	1	m <sub>3</sub>
1	0	0	0	m <sub>4</sub>
1	0	1	1	m <sub>5</sub>
1	1	0	1	m <sub>6</sub>
1	1	1	1	m <sub>7</sub>

(Majority Logic)

$$F = m_3 + m_5 + m_6 + m_7 = \bar{A}BC + A\bar{B}C + ABC\bar{C} + ABC$$

$$F = M_6 \cdot M_1 \cdot M_2 \cdot M_4 = (A+B+C) \cdot (A+B+\bar{C}) \cdot (A+\bar{B}+C) \cdot (\bar{A}+B+C)$$



11.53 a)

A	BC			
	00	01	11	10
0	0	1	1	1
1	1	1	0	0

$$F = A\bar{B} + \bar{B}C + \bar{A}B$$

b)

A	BC			
	00	01	11	10
0	0	0	0	1
1	1	0	1	1

$$F = A\bar{C} + AB + BC$$

c)

A	BC			
	00	01	11	10
0	1	1	1	1
1	0	1	0	1

$$F = \bar{A} + \bar{B}C + BC$$

11.57 a) AB

		CD			
		00	01	11	10
00		0	0	0	0
01		1	1	1	1
11		0	1	1	1
10		0	0	0	1

$$F = \bar{A}B + B\bar{D} + AC\bar{D}$$

b)

		CD			
	AB	00	01	11	10
00		0	1	1	1
01		0	0	0	1
11		0	1	0	1
10		0	0	1	1

$$F = \bar{B}D + C\bar{D} + A\bar{C}D$$

c)

		CD			
	AB	00	01	11	10
00		1	0	1	0
01		0	0	1	1
11		0	1	0	1
10		1	0	0	1

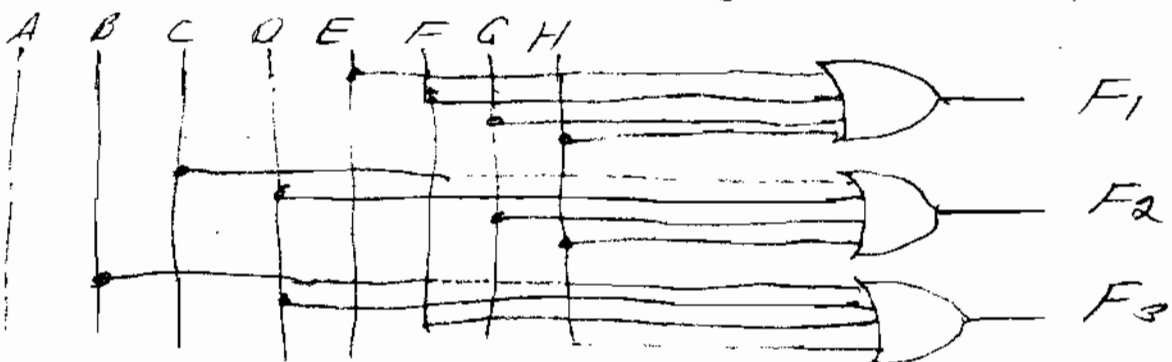
$$F = \bar{B}\bar{C}\bar{D} + A\bar{B}\bar{C}D + \bar{A}CD + B\bar{C}\bar{D} + AC\bar{D}$$

(or other combinations)

12.14

A	B	C	D	E	F	G	H	F <sub>1</sub>	F <sub>2</sub>	F <sub>3</sub>
1	0	0	0	0	0	0	0	0	0	0
1	0	0	0	0	0	0	0	0	0	0
1	0	0	1	0	0	0	0	0	1	0
1	0	0	0	1	0	0	0	0	1	1
1	0	0	0	0	1	0	0	0	1	0
1	0	0	0	0	0	1	0	0	1	1
1	0	0	0	0	0	0	1	0	1	0
1	0	0	0	0	0	0	0	1	1	0
0	0	0	0	0	0	0	0	1	1	1

$$F_1 = E + F + G + H, \quad F_2 = C + D + G + H, \quad F_3 = B + D + F + H$$



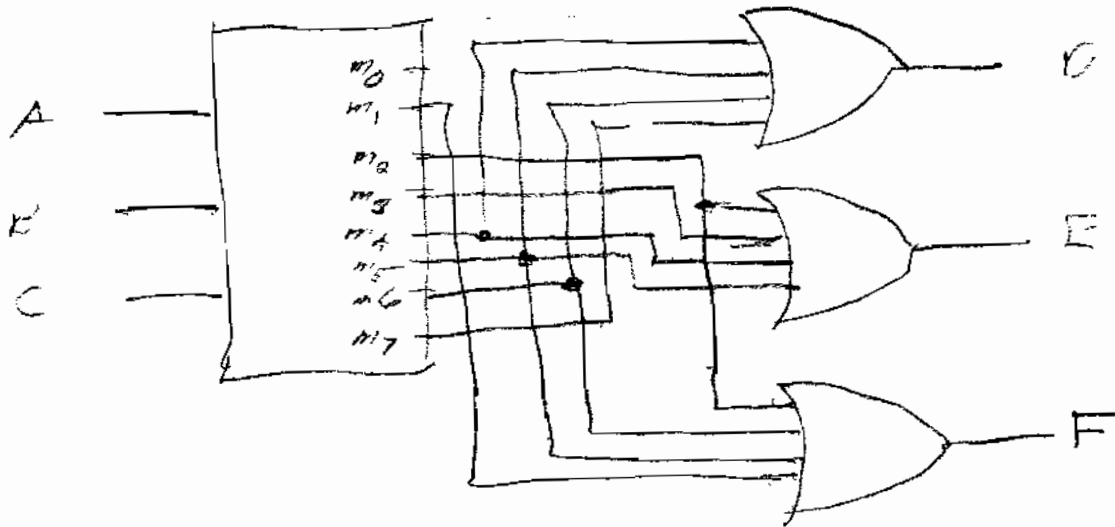
12.17

A	B	C	D	E	F
0	0	0	0	0	0
0	0	1	0	0	1
0	1	0	0	1	1
0	1	1	0	1	0
1	0	0	1	1	0
1	0	1	1	1	1
1	1	0	1	0	1
1	1	1	1	0	0

$$D = m_4 + m_5 + m_6 + m_7$$

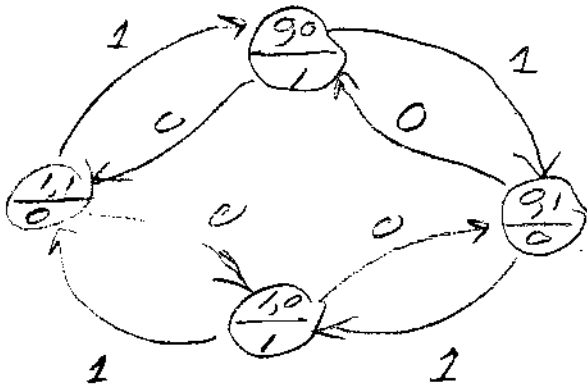
$$E = m_2 + m_3 + m_4 + m_5$$

$$F = m_1 + m_2 + m_5 + m_6$$

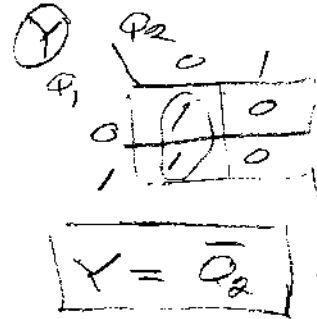
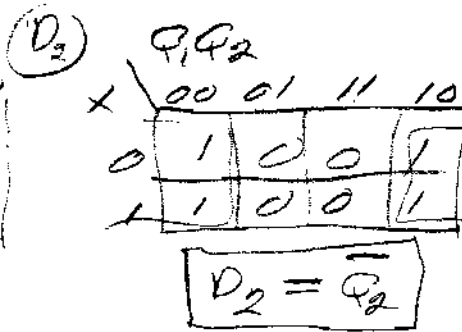
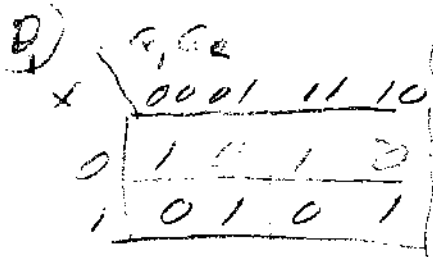




12.42



X	Present		Next		Y	D <sub>1</sub>	D <sub>2</sub>
	Q <sub>1</sub>	Q <sub>2</sub>	Q <sub>1</sub> <sup>+</sup>	Q <sub>2</sub> <sup>+</sup>			
0	0	0	1	1	1	1	1
0	0	1	0	0	0	0	0
0	1	0	0	1	1	0	1
0	1	1	1	0	0	1	0
1	0	0	0	1	1	0	1
1	0	1	1	0	0	1	0
1	1	0	1	1	1	1	1
1	1	1	0	0	0	0	0

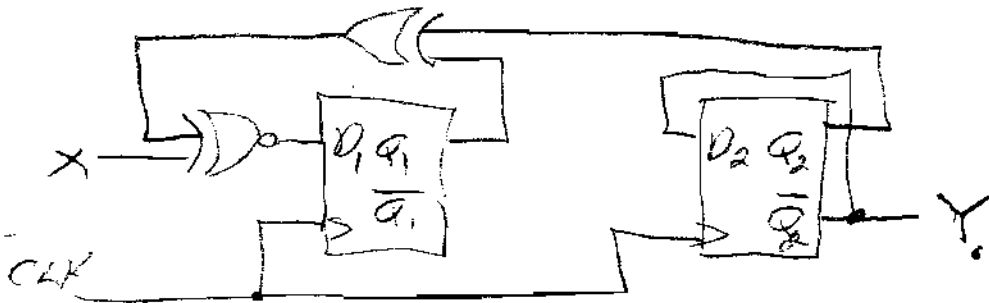


$D_2 = \overline{Q_2}$

$Y = \overline{Q_2}$

$$D_1 = \overline{X} \overline{Q_1} \overline{Q_2} + \overline{X} \overline{Q_1} Q_2 + \overline{X} Q_1 \overline{Q_2} + \overline{X} Q_1 Q_2 = \overline{X} (\overline{Q_1} \overline{Q_2} + \overline{Q_1} Q_2 + Q_1 \overline{Q_2} + Q_1 Q_2)$$

$$D_1 = \overline{X} \cdot (\overline{Q_1} \oplus Q_2) + X (Q_1 \oplus Q_2) = X \oplus (Q_1 \oplus Q_2)$$



Modulo 3 counter using D flip-flops

Present	Next	D <sub>1</sub> D <sub>0</sub>
Q <sub>1</sub> Q <sub>0</sub>	Q <sub>1</sub> <sup>+</sup> Q <sub>0</sub> <sup>+</sup>	
00	01	01
01	10	10
10	00	00

$D_1 = \overline{Q_1} Q_0$  ;  $D_0 = \overline{Q_1} \overline{Q_0}$

