

EE 231
Exam 2
October 15, 2008

Name: _____

Show all work. Partial credit will be given. No credit will be given if an answer appears with no supporting work.

1. Consider the following Boolean function: $F(w, x, y, z) = \sum(1, 3, 5, 7, 8, 9, 11, 15)$.

(a) Find all the prime implicants of the function, and indicate which are essential.

		yz			
	wx	00	01	11	10
00	0	0	1	3	2
01	4	0	5	7	6
11	12	0	13	15	14
10	8	1	9	11	10

- $F(w, x, y, z) = yz = \sum(3, 7, 11, 15)$ (essential)
- $F(w, x, y, z) = w'z = \sum(1, 3, 5, 7)$ (essential)
- $F(w, x, y, z) = wx'y' = \sum(8, 9)$ (essential)
- $F(w, x, y, z) = x'z = \sum(1, 3, 9, 11)$ (not essential)

(b) Use a Karnaugh map to simplify the function.

$F(w, x, y, z) = yz + w'z + wx'y'$

2. Simplify the Boolean function $F(w, x, y, z) = \sum(0, 1, 5, 6, 9)$ with the don't-care conditions $d(w, x, y, z) = \sum(2, 8, 10, 13, 15)$.

		yz			
	wx	00	01	11	10
00	0	1	1	0	x
01	4	0	1	0	1
11	12	0	x	x	0
10	8	x	1	0	x

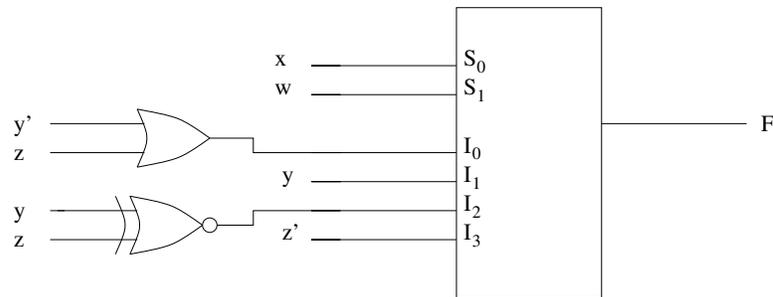
$F(w, x, y, z) = x'y' + y'z + w'yz'$

or

		yz			
	wx	00	01	11	10
00	0	1	1	0	x
01	4	0	1	0	1
11	12	0	x	x	0
10	8	x	1	0	x

$F(w, x, y, z) = x'z' + y'z + w'yz'$

3. Consider the following circuit constructed with a 4-to-1 multiplexer. Determine a Boolean expression for the output F .



w	x	y	z	F
0	0	0	0	1
0	0	0	1	1
0	0	1	0	0
0	0	1	1	1
0	1	0	0	0
0	1	0	1	0
0	1	1	0	1
0	1	1	1	1
1	0	0	0	1
1	0	0	1	0
1	0	1	0	0
1	0	1	1	1
1	1	0	0	1
1	1	0	1	0
1	1	1	0	1
1	1	1	1	0

		yz			
		00	01	11	10
wx	00	0 1 1	1 1 1	3 1 1	2 0
	01	4 0	5 0	7 1	6 1
11	12 1	13 0	15 0	14 1	
10	8 1	9 0	11 1	10 0	

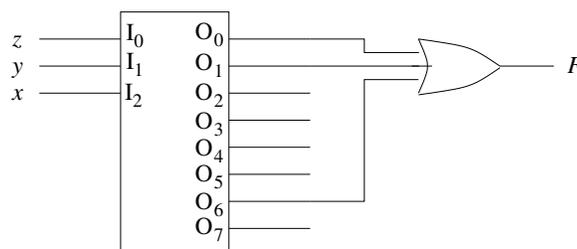
$F = w'x'y' + wy'z' + w'yz + xyz' + x'yz$ or $F = w'x'y' + wy'z' + w'yz + xyz' + w'x'z$
or

When w is low and x is low ($w'x'$), the output is I_0 ($y' + z$); when $w'x$ the output is I_1 (y), when wx' the output is I_2 ($(y \oplus z)'$); when wx the output is I_3 (z'), so

$F = w'x'(y' + z) + w'x(y) + wx'(y \oplus z)' + wx(z')$

4. Design a circuit which implements the function $F = x'y' + xyz'$ using a 3-to-8 decoder and some OR gates.

$F(x, y, z) = x'y'(z' + z) + xyz' = x'y'z' + x'y'z + xyz' = \sum(0, 1, 6)$



5. Design a division detector device that receives a 4-bit binary number $A_3A_2A_1A_0$ and outputs a 1 whenever the input is evenly divisible by either 4 or 5.

- (a) Find the truth table for the device
- (b) Use a Karnaugh map to find a reduced sum-of-products form for the device.

A_3	A_2	A_1	A_0	F
0	0	0	0	1
0	0	0	1	0
0	0	1	0	0
0	0	1	1	0
0	1	0	0	1
0	1	0	1	1
0	1	1	0	0
0	1	1	1	0
1	0	0	0	1
1	0	0	1	0
1	0	1	0	1
1	0	1	1	0
1	1	0	0	1
1	1	0	1	0
1	1	1	0	0
1	1	1	1	1

		A_1A_0			
		00	01	11	10
A_3A_2	00	0 1	1 0	3 0	2 0
	01	4 1	5 1	7 0	6 0
	11	12 1	13 0	15 1	14 0
	10	8 1	9 0	11 0	10 1

$$F(A_3, A_2, A_1, A_0) = A_2'A_1' + A_3'A_2A_1' + A_3A_2'A_0' + A_3A_2A_1A_0$$