

Binary, Hex and Decimal Numbers (4-bit representation)

Binary	Hex	Decimal
0000	0	0
0001	1	1
0010	2	2
0011	3	3
0100	4	4
0101	5	5
0110	6	6
0111	7	7
1000	8	8
1001	9	9
1010	A	10
1011	B	11
1100	C	12
1101	D	13
1110	E	14
1111	F	15

What does a number represent?

Binary numbers are a code, and represent what the programmer intends for the code.

0x72

Some possible codes:

'r' (ASCII)

INC (HC12 instruction)

2.26V (Input from A/D converter)

114_{10} (Unsigned number)

114_{10} (Signed number)

Set temperature in room to 69 F

Set cruise control speed to 120 mph

Binary to Unsigned Decimal:**Convert Binary to Unsigned Decimal** 1111011_2

$$1 \times 2^6 + 1 \times 2^5 + 1 \times 2^4 + 1 \times 2^3 + 0 \times 2^2 + 1 \times 2^1 + 1 \times 2^0$$

$$1 \times 64 + 1 \times 32 + 1 \times 16 + 1 \times 8 + 0 \times 4 + 1 \times 2 + 1 \times 1$$


 123_{10} Hex to Unsigned Decimal**Convert Hex to Unsigned Decimal** $82D6_{16}$

$$8 \times 16^3 + 2 \times 16^2 + 13 \times 16^1 + 6 \times 16^0$$

$$8 \times 4096 + 2 \times 256 + 13 \times 16 + 6 \times 1$$

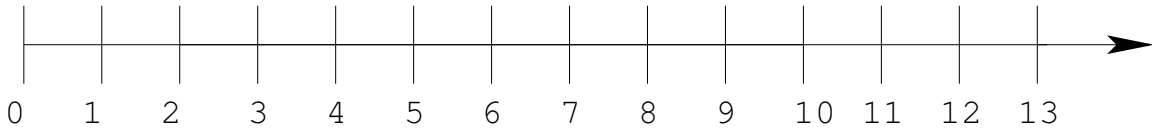
 33494_{10}

Unsigned Decimal to Hex**Convert Unsigned Decimal to Hex**

Division	Q	R	
		Decimal	Hex
721/16	45	1	1 
45/16	2	13	D
2/16	0	2	2

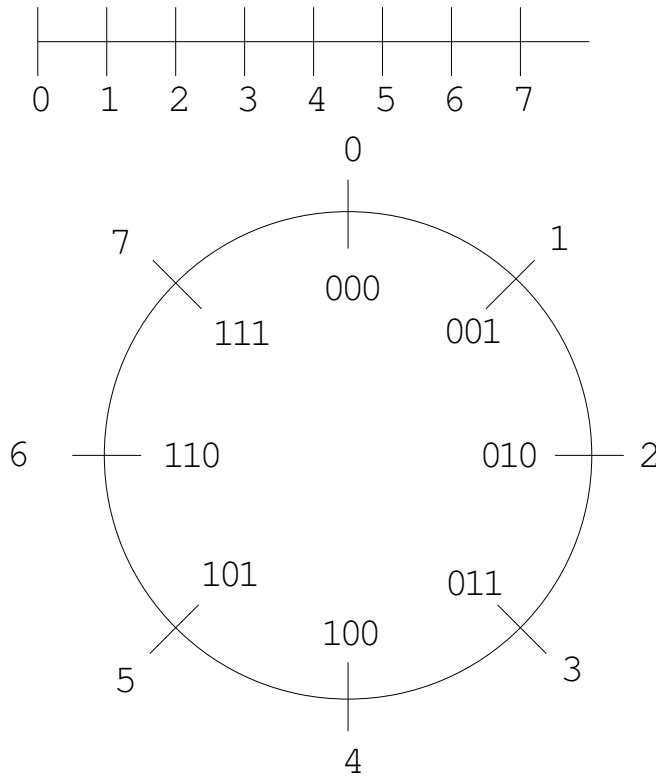
$$721_{10} = 2D1_{16}$$

Unsigned Number Line: Numbers go from 0 to ∞

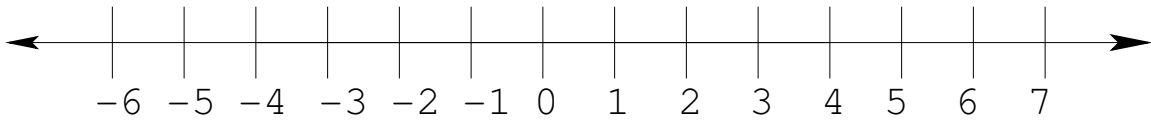


Unsigned Number Line

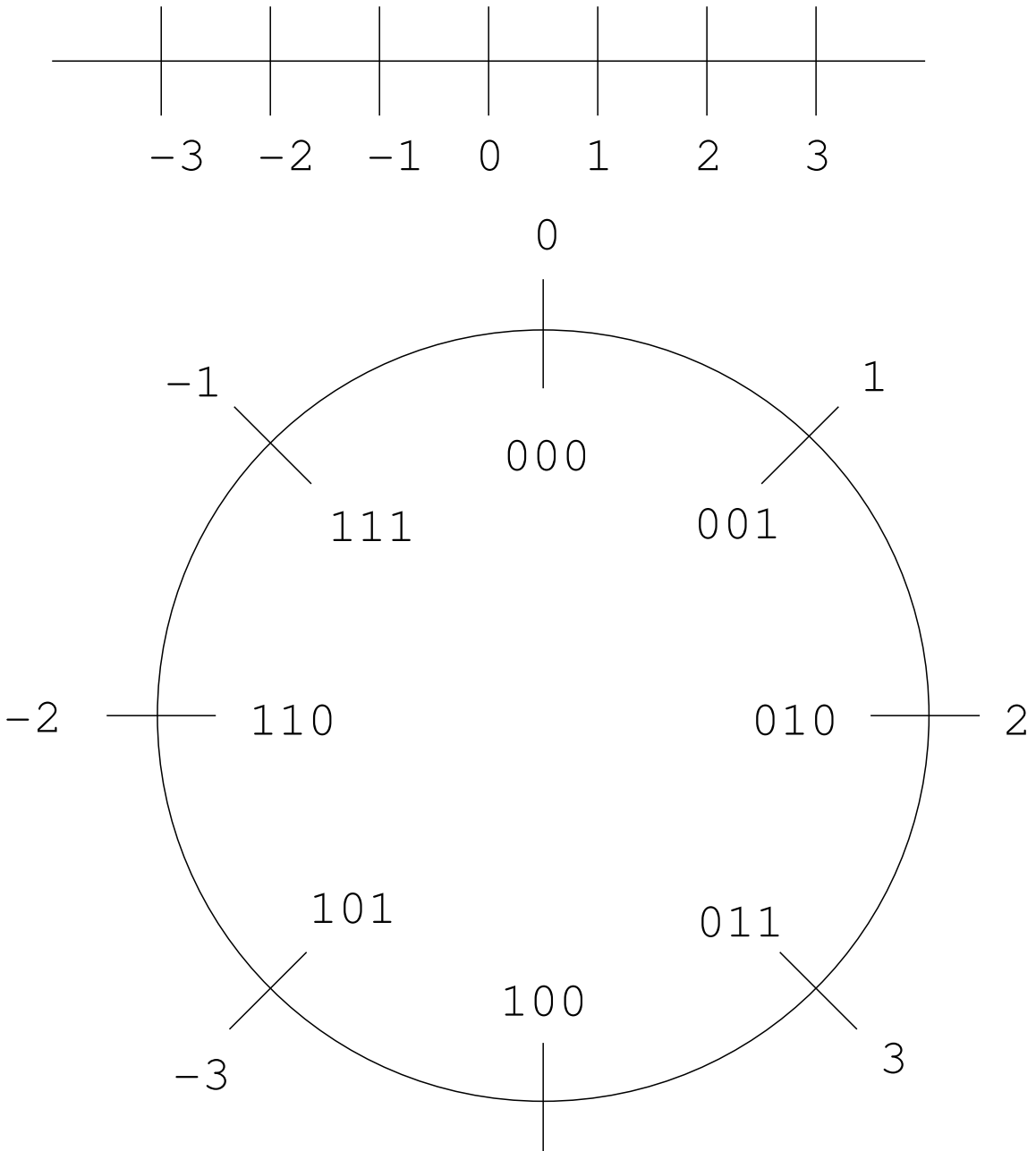
Unsigned Number Wheel: Numbers go from 0 to $2^N - 1$



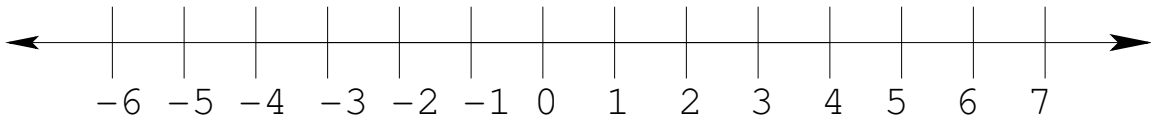
Signed Number Line: Numbers go from $-\infty$ to ∞



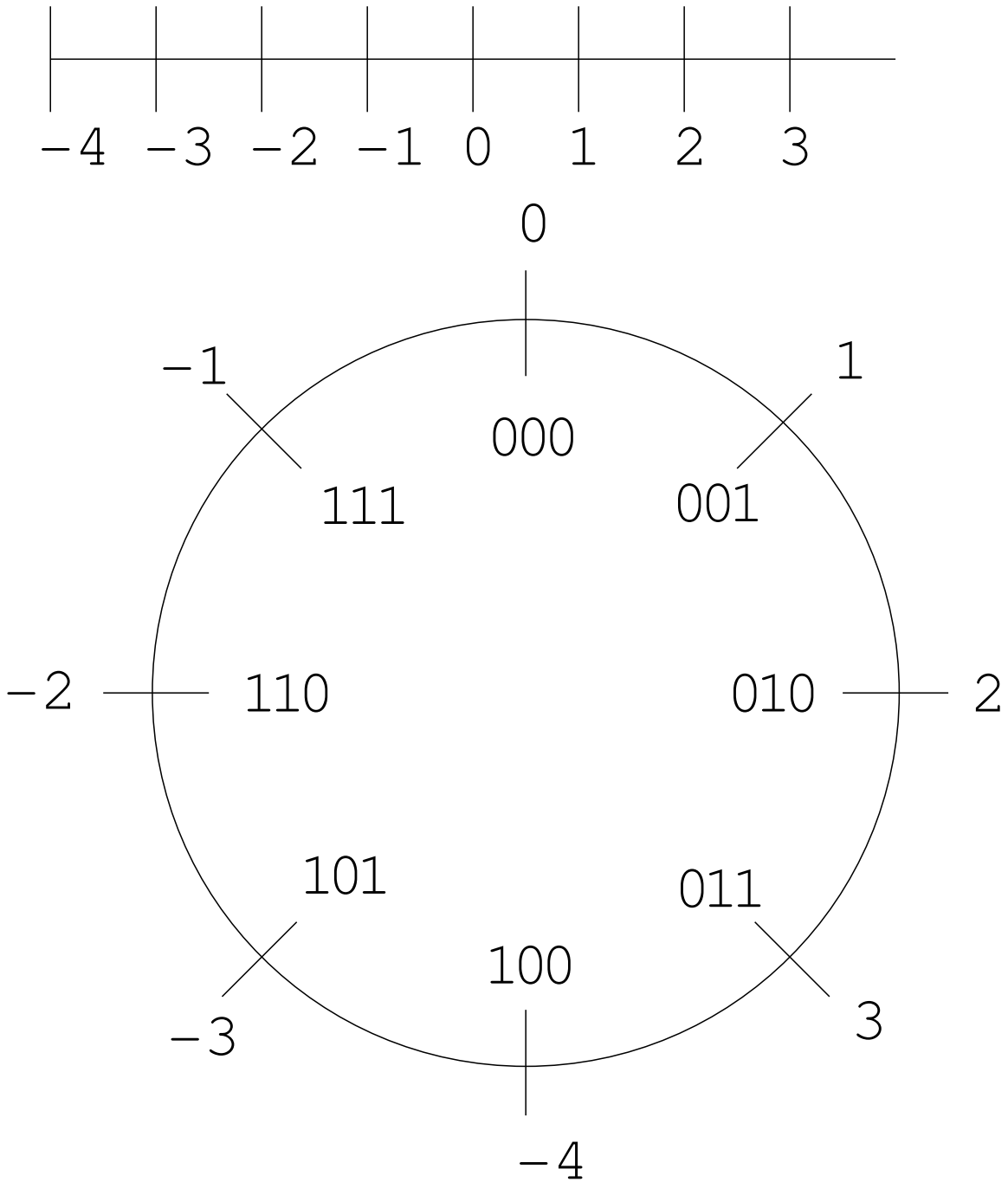
Number Wheel: What to do about 100_2



Signed Number Line: Numbers go from $-\infty$ to ∞

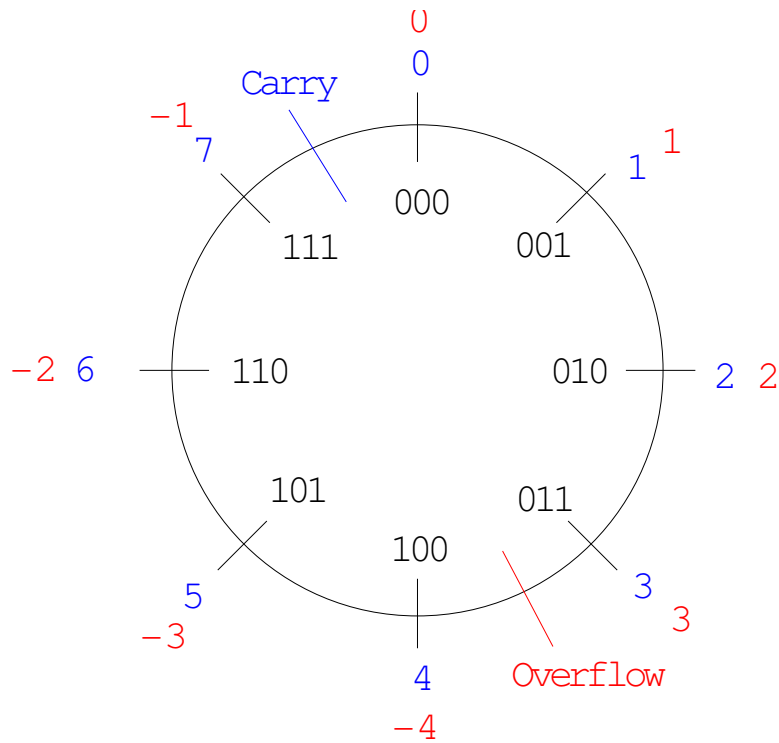


Number Wheel: Numbers go from $-2^{(N-1)}$ to $2^{(N-1)} - 1$



Number Wheel: Carry and Overflow

- Carry applies to unsigned numbers — when adding or subtracting, result is incorrect.
- Overflow applies to signed numbers — when adding or subtracting, result is incorrect.



Blue: Unsigned Numbers

Red: Signed Numbers

Binary, Hex and Decimal (Signed & Unsigned) Numbers (4-bit representation)

Binary	Hex	Decimal	
		US	S
0000	0	0	0
0001	1	1	1
0010	2	2	2
0011	3	3	3
0100	4	4	4
0101	5	5	5
0110	6	6	6
0111	7	7	7
1000	8	8	-8
1001	9	9	-7
1010	A	10	-6
1011	B	11	-5
1100	C	12	-4
1101	D	13	-3
1110	E	14	-2
1111	F	15	-1

Signed Number Representation in 2's Complement Form:

If most significant bit is 0 (most significant hex digit 0–7), number is positive.
Get decimal equivalent by converting number to decimal, and using + sign.

Example for 8-bit number:

$$\begin{aligned} 3A_{16} &\rightarrow + (3 \times 16^1 + 10 \times 16^0)_{10} \\ &\quad + (3 \times 16 + 10 \times 1)_{10} \\ &\quad + 58_{10} \end{aligned}$$

If most significant bit is 1 (most significant hex digit 8–F), number is negative.
Get decimal equivalent by taking 2's complement of number, converting to decimal,
and using – sign.

Example for 8-bit number:

$$\begin{aligned} A3_{16} &\rightarrow - (5D)_{16} \\ &\quad - (5 \times 16^1 + 13 \times 16^0)_{10} \\ &\quad - (5 \times 16 + 13 \times 1)_{10} \\ &\quad - 93_{10} \end{aligned}$$

One's Complement Table Makes It Simple To Find 2's Complements

One's Complement Table

0	F
1	E
2	D
3	C
4	B
5	A
6	9
7	8

To take two's complement, add one to one's complement

Take two's complement of D0C3 :

$$2F3C + 1 = 2F3D$$

- Overflow and Carry assume you have a fixed word size
- A carry is generated when you add two unsigned numbers together, and the result is too large to fit in the fixed word size.
- A carry is generated when you subtract two unsigned numbers, and the result should be negative.
- An overflow is generated when you add or subtract two signed numbers, and the fixed-length answer has the wrong sign.

Addition and Subtraction of Binary and Hexadecimal Numbers

ADDITION AND SUBTRACTION OF BINARY AND HEXADECIMAL NUMBER

- 1) **Limit number of digits to specified word size.**

$$\begin{array}{r}
 \text{4-bit word:} \quad 1101 \\
 + \quad 1011 \\
 \hline
 \times 1 \quad 1000
 \end{array}$$

Keep only 4 bits in answer

- 2) **Does not matter if numbers are signed or unsigned – mechanics the same**

Do the operation, then determine if carry and/or overflow bits are set.

$$\begin{array}{r}
 \text{4-bit word:} \quad 1101 \quad \text{Neg} \\
 + \quad 1011 \quad \text{Neg} \\
 \hline
 \times 1 \quad 1000 \quad \text{Neg}
 \end{array}$$

Carry is set, overflow is clear

Condition Code Register Gives Information On Result Of Last Operation

S	X	H	I	N	Z	V	C
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Condition Code Register – 8 FFs

N – Negative : most significant bit of result

Z – Zero : 1 -> result zero, 0 -> result not zero

V – Overflow : 1 -> last operation generated an overfl.

C – Carry : 1 -> last operation generated a carry

Note: Not all HC12 instructions change CCR bits. A bit in the CCR is the result of the last executed instruction which affects that bit. For example, consider the following instruction sequence:

```
aba                ; Add B to A
staa $0900         ; Store A in address $0900
```

The ABA instruction will change the H, N, Z, V and C bits of the CCR. The STAA instruction will change the N and Z bit, and clear the V bit. After the two instructions, the H and C bits will reflect the result of the ABA instruction; the N and Z bits will reflect the result of the STAA instruction (was the number stored negative or zero), and the V bit will be 0.

Overflow occurs only under certain addition and subtraction operations.

S	X	H	I	N	Z	V	C
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Condition Code Register – 8 FFs

N – Negative : most significant bit of result

Z – Zero : 1 -> result zero, 0 -> result not zero

V – Overflow : 1 -> last operation generated an overfl.

C – Carry : 1 -> last operation generated a carry

- If you add a positive and a negative number, an overflow never occurs.
- If you subtract two positive numbers, an overflow never occurs.
- If you subtract two negative numbers, an overflow never occurs.