EE 341 - Exam 3 November 22, 2004

Name:

Closed book. Show all work. Partial credit will be given. No credit will be given if an answer appears with no supporting work. You may use one page of notes and a calculator.

1. Consider the following system:



The frequency response of the filter is

$$H(\omega) = 1 - e^{-j\omega/2}$$

The input x(t) is:

$$x(t) = 5 + 2\cos(\pi t) + 3\sin(2\pi t)$$

(a) Find $X(\omega)$, the Fourier transform of x(t).

(b) Find $Y(\omega)$.

(c) Find y(t).

2. Consider the following system:



(a) Let T = 0.001 sec. Sketch the frequency response $|H(\omega)|$ of the low pass filter which will make it an ideal reconstruction filter.

(b) Let $x(t) = 5 + 2\cos(800\pi t) + 3\sin(1500\pi t)$. Sketch $|X(\omega)|$, the magnitude of the Fourier transform of x(t).

(c) Sketch $|X_s(\omega)|$, the Fourier transform of the sampled signal $x_s(t)$.

(d) Sketch $|Y(\omega)|$, the magnitude of the Fourier transform of y(t).

(e) Find y(t).

3. Consider the following system:



The input to the system is

$$x(t) = \operatorname{sinc}\left(\frac{3t}{\pi}\right)$$

The impulse response $h_2(t)$ is

$$h_2(t) = \operatorname{sinc}\left(\frac{4t}{\pi}\right)$$

(a) Find $H_2(\omega)$, the Fourier transform of $h_2(t)$

(b) Find $X(\omega)$, the Fourier transform of x(t)

(c) Sketch $R(\omega)$

(d) Sketch $S(\omega)$

(e) Sketch $V(\omega)$

(f) Sketch $Y(\omega)$

(g) Find y(t).