## Dynamics of a SCARA-type Robot

Use the Lagrangian and Lagrange equation to find the dynamic equations for the SCARA-type robot with DH Table shown below.


| Link $i$ | $a_{i}$ | $\alpha_{i}$ | $d_{i}$ | $\theta_{i}$ |
| :---: | :---: | :---: | :---: | :---: |
| 1 | $a_{1}$ | 0 | $d_{1}$ | $\theta_{1}$ |
| 2 | $a_{2}$ | $\pi$ | 0 | $\theta_{2}$ |
| 3 | 0 | 0 | $d_{3}$ | 0 |
| 4 | 0 | 0 | 0 | $\theta_{4}$ |

Clearly write your answer(s) in terms of the general dimensions labeled, and make the following assumptions:

1. all links have symmetric geometry and uniformly distributed mass,
2. link 1 can be represented by a rectangular parallelopiped of mass $m_{1}$ and dimensions shown,
3. link 2 can be represented by a rectangular parallelopiped of mass $m_{2}$ and dimensions shown, and
4. links 3 and 4 can be represented by slender rods of equal length and equal mass $m_{3}$.
